

1           **Submesoscale processes in the Kuroshio Loop Current: roles in**  
2                           **energy cascade and salt and heat transports**

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11   **Key points:**

- 12           ● Submesoscales in the Kuroshio Loop Current (KLC) are examined using  
13           high-resolution simulation outputs.
- 14           ● Energy exchange between submesoscales and KLC plays an important role in  
15           the local energy budget.
- 16           ● Horizontal salt and heat transports by submesoscales are much larger than  
17           those by KLC eddy shedding.

18

19 **Abstract**

20 The Kuroshio Loop Current (KLC) is an important form of Kuroshio intrusion into  
21 the northeastern South China Sea (NESCS), which has significant influences on  
22 dynamical and biogeochemical processes in the NESCS. Recent studies suggested  
23 that the KLC is a hot spot of submesoscale processes (submesoscales) with  
24 spatiotemporal scales of  $O(1-10)$  km and  $O(1-10)$  days, but submesoscales' roles in  
25 energy cascade and salt and heat transports remain obscure. Here, we investigate this  
26 issue through analyzing outputs from a  $1/48^\circ$  simulation. The kinetic energy exchange  
27 rate between submesoscale and larger-scale processes (KER) is overall positive in the  
28 KLC region, which suggests the dominance of forward cascade. The magnitude of  
29 KER is comparable with the temporal change rate of larger-scale kinetic energy in the  
30 upper 200 m. We also find that magnitude and direction of KER are closely associated  
31 with strain rate and horizontal divergence of background flows, respectively. In  
32 addition, the KLC region shows elevated submesoscale salinity and heat diffusivities  
33 with magnitudes reaching  $O(10^2)$   $\text{m}^2\text{s}^{-1}$ . During the KLC period, horizontal mixing by  
34 submesoscales can transport  $0.90 \times 10^{13}$  kg salt and  $0.71 \times 10^{20}$  J heat westward into the  
35 NESCS interior, which are an order of magnitude larger than those caused by the  
36 KLC eddy shedding. These results suggest that submesoscales play important roles  
37 not only in energy cascade but also in salt and heat transports in the KLC region.  
38 Therefore, the roles of submesoscales should be taken into account when studying  
39 energy, salt, and heat budgets in the NESCS.

41 **Plain Language Summary**

42 As the western boundary current of the North Pacific subtropical gyre, the Kuroshio  
43 can intrude into the northeastern South China Sea (NESCS) in the form of Kuroshio  
44 Loop Current (KLC), which modulate the tracer and energy budgets of NESCS  
45 through shedding eddies. Although previous studies have reported that the KLC  
46 region is abundant with submesoscale processes (submesoscales) with spatiotemporal  
47 scales of  $O(1-10)$  km and  $O(1-10)$  days, their roles in cross-scale energy transfer and  
48 salt and heat transports are poorly known. In this study, the above issues are examined  
49 through an analysis of outputs from a  $1/48^\circ$  ocean simulation. We find that  
50 larger-scale processes in this region generally feed submesoscales through a forward  
51 energy transfer in upper 200 m, whose rate is comparable in magnitude with the  
52 temporal change rate of larger-scale kinetic energy. Furthermore, the horizontal  
53 mixing effect of submesoscales can transport a huge amount of heat and salt westward  
54 into the NESCS interior during the KLC period. The salt and heat transports are an  
55 order of magnitude larger than those caused by the KLC eddy shedding. The above  
56 results suggest that submesoscales associated with the KLC play important roles in  
57 the energy, heat, and salt budgets in the NESCS.

58

59

## 60 **1 Introduction**

61 Oceanic submesoscale processes (submesoscales hereafter) typically refer to  
62 the dynamic processes with spatial and temporal scales of  $O(1-10\text{ km})$  and  $O(1-10$   
63 days), respectively (McWilliams, 2016; Thomas et al., 2008). Dynamically,  
64 submesoscales are characterized by order one Rossby numbers ( $Ro$ ) and  
65 correspondingly, they can break the constrain of geostrophic balance and thus  
66 generate strong vertical motions (Mahadevan & Tandon, 2006; Yu et al., 2019; Zhang  
67 Z. et al., 2021). As a result, submesoscales can cause large vertical transports of heat,  
68 salt, oxygen, nutrients, and other tracers in the upper ocean, through which they  
69 significantly modulate both the dynamical and biogeochemical processes therein  
70 (Mahadevan et al., 2012; Mahadevan, 2016; Su Z. et al., 2018; Thompson et al., 2016).  
71 In addition, because of their mediate spatiotemporal scale and strong ageostrophic  
72 nature, submesoscales are demonstrated to behave as an important conduit connecting  
73 the oceanic balanced and unbalanced motions. Therefore, they play an irreplaceable  
74 role in the oceanic energy cascade that maintains the balance of ocean energy  
75 reservoir (Capet et al., 2008; D'Asaro et al., 2011; Gula et al., 2016; Qiu et al., 2022;  
76 Zhang Z. et al., 2023).

77 The South China Sea (SCS) is the largest marginal sea of the northwestern  
78 Pacific, which is linked to the northwestern Pacific through the Luzon Strait (Figure  
79 1a). Due to the intrusion of the Kuroshio, strong monsoon winds, and complex  
80 topography, the SCS is abundant with rich multi-scale dynamic processes, including  
81 large scale circulation (Gan et al., 2016; Su J., 2004), mesoscale eddies (Wang, 2003;

82 Zhang Z. et al., 2016, 2017), small-scale internal waves (Alford et al., 2015; Huang et  
83 al., 2016), and microscale turbulent mixing (Tian et al., 2009; Yang et al., 2016). Both  
84 recent observation and simulation studies have revealed that submesoscales in the  
85 SCS are also very active (e.g., Cao et al., 2022; Dong & Zhong, 2018; Li et al., 2019;  
86 Lin et al., 2020; Zhang J. et al., 2021; Zhang X. et al., 2022; Zhang Z. et al., 2020;  
87 Zhong et al., 2017). Given the potential importance of submesoscales to material  
88 transport, energy cascade, and biogeochemical processes in the SCS, they have  
89 received more and more attentions in recent years.

90       When the nascent Kuroshio flows northward through the Luzon Strait, its  
91 main axis often bends clockwise and intrudes into the northeastern SCS (NESCS) in  
92 the form of the Kuroshio Loop Current (KLC) in winter (Shaw, 1989; Sheremet, 2001;  
93 Sun et al., 2020; Figure 1a). As the KLC develops, it can finally shed an anticyclonic  
94 mesoscale eddy in the NESCS, which can further induce a cyclonic mesoscale eddy in  
95 the trailing (Zhang Z. et al., 2017). The anticyclonic eddy shedding from the KLC can  
96 transport a considerable amount of warmer, saltier, and oligotrophic Kuroshio water  
97 into the NESCS that significantly modulate the tracer budgets therein (Zhang Z. et al.,  
98 2017). Recently, through analyzing submesoscale permitting simulation outputs, the  
99 study of Zhang Z. et al. (2020) have pointed out that the KLC region is a hotspot of  
100 submesoscales. These submesoscales are suggested to be generated by the  
101 combination of mixed-layer baroclinic instability and strain-induced frontogenesis.  
102 The authors further argued that after generation, the submesoscales may transfer part  
103 of their kinetic energy (KE) inversely to mesoscale eddies. The above simulation

104 results have been to a large degree verified by Zhang J. et al. (2021) based on the  
105 analysis of long-term moored observations. Besides, the most recent observation  
106 study of Zhang X. et al. (2022) have revealed that interactions between the KLC and  
107 the complex topography in the Luzon Strait and the region southwest of Taiwan can  
108 generate submesoscale coherent vortices, which means the occurrence of forward  
109 energy cascade.

110         Although submesoscales in the NESCS (the KLC region in particular) have  
111 been investigated by a couple of studies, the following two issues remain to be  
112 revealed. First, the spatiotemporal characteristics of submesoscale energy cascade and  
113 its role in modulating the KLC are still obscure. Second, during the development or  
114 steady stage of the KLC (before the eddy shedding), whether and to what degree can  
115 the horizontal mixing effect of the submesoscales surrounding the KLC contribute to  
116 the NESCS-Pacific water exchange remain unknown. Here, these two scientific issues  
117 are explored by an analysis of the outputs from a submesoscale permitting simulation  
118 (~2-km resolution). The remainder of the paper is organized as follows. Section 2  
119 describes the data and methods. Section 3 shows general characteristics of the KLC  
120 and submesoscales in the study region. Section 4 reveals the energy cascade (refers  
121 only to KE cascade hereafter) associated with submesoscales. In section 5, the salt  
122 and heat transports caused by submesoscales are quantitatively evaluated. Finally,  
123 summary and discussion of the study are given in section 6.

## 124 **2 Data and methods**

## 125           **2.1 High-resolution simulation outputs**

126           The outputs from the MITgcm (Massachusetts Institute of Technology General  
127   Circulation Model) LLC4320 simulation were used in this study to investigate the  
128   energy cascade and salt transport associated with submesoscales. The LLC4320  
129   simulation is forced by the 6-hourly ECMWF (European Centre for Medium-Range  
130   Weather Forecasts) atmospheric analysis as well as the 16 main tidal components.  
131   Horizontally, it has a  $1/48^\circ$  ( $\sim 2$  km) resolution and in the vertical, it contains 90 layers  
132   whose resolution ranges from 1 to 20 m in the upper 200 m (focus of this study). The  
133   time range of LLC4320 is from September 13, 2011 to November 14, 2012 (14  
134   months) and the outputs are stored with an hourly interval. With an effective  
135   resolution of  $\sim 10$  km, the LLC4320 simulation can, to a certain degree, resolve  
136   submesoscales at the low and mid latitudes, particularly the larger ones generated by  
137   mixed-layer baroclinic instabilities (Dong et al., 2020).

138           Until now, the LLC4320 simulation has been used by a number of studies to  
139   investigate the submesoscales in both global and regional scopes (e.g., Miao et al.,  
140   2021; Qiu et al., 2018; Rocha et al., 2016; Su Z. et al., 2018; Zhang Z. et al., 2023).  
141   Recently, the LLC4320 data was also applied to submesoscale researches in the SCS,  
142   and its performance has been validated by multiple in situ observations (Cao et al.,  
143   2019; Lin et al., 2020). Here, hourly LLC4320 data in the NESCS are extracted and  
144   analyzed ( $115\text{--}123^\circ\text{E}$ ,  $17\text{--}24^\circ\text{N}$ ; red box in Figure 1a). In order to remove the tidal  
145   and inertial signals, the hourly data were firstly 48-hour low-pass filtered  
146   (fourth-order Butterworth) and then averaged on a daily basis.

147           In Figures 1b–c, we compare the mean sea surface height (SSH) and surface  
148 geostrophic currents in winter (i.e., December, January, and February) from the  
149 LLC4320 data with those from the altimeter data. Here, the altimeter data are the  
150 multiple-satellite-merged gridded products from AVISO with temporal and spatial  
151 resolutions of 1 day and  $1/4^\circ$ , respectively. Given that the free run LLC4320  
152 simulation cannot reproduce the real KLC in the same period (i.e., 2011–2012), the  
153 climatologically winter mean altimeter data during the strong KLC periods between  
154 1999–2000, 2011–2012, 2016–2017, and 2017–2018 (Sun et al., 2020) are used for  
155 comparison. It reveals that both the LLC4320 and altimeter SSHs (and surface  
156 geostrophic currents) display an evident KLC in the NESCS in winter. The KLC  
157 pattern in the LLC4320 is overall similar to the altimeter result, although its size and  
158 strength are slightly weaker. The reasonable simulation of the KLC in the LLC4320  
159 lays the basis to perform the analysis in this study.

## 160           **2.2 Method of scale separation**

161           In this study, a period 15 days was used as the separation time scale between  
162 submesoscales and meso- to large-scale processes. Specifically, we obtained the  
163 meso- to large-scale (larger-scale for short hereafter) and submesoscale signals by  
164 performing the 15-day low-pass and high-pass filters to the subinertial LLC4320 daily  
165 data, respectively. The 15-day separation scale was chosen because the recent  
166 observations from a submesoscale mooring array have suggested that the subinertial  
167 velocity and temperature anomalies (with periods shorter than 15 days) are closely  
168 related to the submesoscales with large Rossby number and vertical velocity (Zhang Z.

169 et al., 2021). The temporal separations were used rather than spatial scale because  
 170 spatial filters can result in large errors near the topography (e.g., coast and islands).  
 171 More recently, through analysing high-resolution simulation data in the NESCS,  
 172 Zhang J. et al. (2021) found a good statistical consistency between the submesoscale  
 173 quantities calculated from 15-day temporal and 80-km spatial high-pass filters.  
 174 Therefore, we finally choose 1–15 days time scale to define submesoscales in the  
 175 NESCS.

### 176 **2.3 Kinetic energy exchange rate**

177 In this study, the coarse-graining approach was adopted to calculate the KE  
 178 exchange rate (KER hereafter) between the submesoscales and larger-scale processes.  
 179 Coarse-graining approach was early established to deal with turbulence problems  
 180 (Eyink, 2005; Germano, 1992; Leonard, 1975) and recently, it has been successfully  
 181 applied to investigate oceanic energy cascade issues based on both simulation and  
 182 observation data (e.g., Aluie et al., 2018; Naveira Garabato et al., 2022; Schubert et al.,  
 183 2020; Srinivasan et al., 2022). The advantage of coarse-graining approach is that its  
 184 calculation is not affected by statistical homogeneity or isotropy assumption adopted  
 185 in the traditional turbulence theory (Aluie et al., 2018). The KER in the  
 186 coarse-graining approach is defined as

$$187 \quad KER = -\left[ \overline{(uu - \bar{u} \bar{u})} \bar{u}_x + \overline{(uv - \bar{u} \bar{v})} (\bar{u}_y + \bar{v}_x) + \overline{(vv - \bar{v} \bar{v})} \bar{v}_y \right] - \left[ \overline{(uw - \bar{u} \bar{w})} \bar{u}_z + \overline{(vw - \bar{v} \bar{w})} \bar{v}_z \right] \quad (1)$$

188 In Eq. (1),  $u$ ,  $v$ , and  $w$  are zonal, meridional, and vertical velocity, respectively;  
 189 Overbar denotes a larger-scale average; Subscripts  $x$ ,  $y$ , and  $z$  denote zonal,  
 190 meridional, and vertical partial derivatives, respectively. The first and second

191 right-hand terms represent the horizontal energy flux and vertical energy flux,  
192 respectively. Physically, KER represents the KE exchange between scales finer and  
193 coarser than a certain scale, whose positive and negative values represent forward and  
194 inverse energy cascade, respectively. Here, the 15-day separation scale was used to  
195 calculate the KER between larger-scale processes and submesoscales (see section 2.2).  
196 Given that in the upper 200 m layer where submesoscales are active, the vertical  
197 energy flux is one order of magnitude smaller than the horizontal energy flux (Figure  
198 S1), only the horizontal term of the KER was finally analyzed in the study.

#### 199 **2.4 Submesoscale salt and heat fluxes and diffusivities**

200 The submesoscale salt flux ( $\mathbf{SF}$ ) on each isopycnal is calculated using

$$201 \quad \mathbf{SF} = \overline{\mathbf{u}'S'}. \quad (2)$$

202 where overbar denotes 15-day running mean, and  $\mathbf{u}'$  and  $S'$  denote velocity and  
203 salinity anomalies caused by submesoscales on each specific isopycnal, respectively.  
204 After obtaining the  $\mathbf{SF}$  vector, we further decomposed it into a rotational  
205 component and a divergent component using Helmholtz decomposition (e.g., Jayne &  
206 Marotzke, 2002). For a specific region with scale much larger than submesoscales, the  
207 rotational component of  $\mathbf{SF}$  transports as much salt to this region as it does out of  
208 that region. As a result, it plays no role in the salt budget in this region. Given that it is  
209 the divergent component of  $\mathbf{SF}$  ( $\mathbf{SF}_D$ ) that eventually determines the salinity  
210 budget, we only focus on the  $\mathbf{SF}_D$  in this study. Based on the  $\mathbf{SF}_D$ , we then  
211 calculated the isopycnal submesoscale salt diffusivity  $K_S$  using

212 
$$K_s = -\mathbf{SF}_D \cdot \nabla \bar{S} / |\nabla \bar{S}|^2. \quad (3)$$

213 where  $\nabla \bar{S}$  is the larger-scale salinity gradient.

214 In order to evaluate the role of submesoscales in salt transport, we calculated  
 215 the submesoscale salt transport per unit depth (STD) across the Kuroshio main axis  
 216 (Ku) using

217 
$$\text{STD} = \int_{Ku} \mathbf{SF}_D \cdot \mathbf{n} \, dl. \quad (4)$$

218 Here,  $\mathbf{n}$  represents the normal unit vector of  $dl$  and the integration is along the Ku,  
 219 which is defined as the SSH contour with the highest average salinity at 150 m where  
 220 the vertical salinity maximum occurs. Based on STD, we can further calculate the  
 221 vertically integrated salt transport (IST) across the Ku using

222 
$$\text{IST} = \int_{-D_\sigma}^0 \text{STD} \, dz. \quad (5)$$

223  $D_\sigma$  is the depth of the  $24.3 \sigma_0$  isopycnal (approximately 150–200 m in the KLC  
 224 region), below which the influence of submesoscales is negligible. Because we only  
 225 focus on the salt transport across the Luzon Strait, the part of Ku east of 120.8 °E  
 226 (solid orange line in Figure 1a) is not taken into account.

227 Similarly, we can also calculate the submesoscale heat flux ( $\mathbf{HF}$ ) on each  
 228 isopycnal using

229 
$$\mathbf{HF} = \rho_0 C_p \overline{\mathbf{u}' \theta'}. \quad (6)$$

230 Here,  $\theta'$  denotes potential temperature anomalies caused by submesoscales on each  
 231 specific isopycnal,  $\rho_0 = 1025 \text{ kg/m}^3$  is the referenced density, and  
 232  $C_p = 3997 \text{ J}/(^{\circ}\text{C} \cdot \text{kg})$  is the thermal capacity. Through replacing salinity with  
 233 potential temperature in Eq. (3–5), we can obtain isopycnal submesoscale heat

234 diffusivity  $K_\theta$ , submesoscale heat transport per unit depth (HTD), and vertically  
235 integrated heat transport (IHT).

### 236 **3 General features of the KLC and submesoscales**

237 In Figure 2, we show the distributions of the simulated surface Rossby number  
238 ( $Ro$ ) calculated using  $Ro = \zeta / f$ , where  $\zeta = v_x - u_y$  is the relative vorticity and  $f$  is  
239 the planetary vorticity. It clearly shows that when the northward-flowing Kuroshio  
240 passes by the Luzon Strait, it bends clockwise to form the KLC in the region  
241 southwest of Taiwan. The KLC began forming in late December 2011, reached  
242 maturity in February and March 2012, and gradually decayed until its disappearance  
243 in early May. Corresponding to the strong anticyclonic currents of the KLC, it shows  
244 nearly universal negative  $Ro$  within its core. The large values of  $Ro$  occur at the  
245 periphery of the KLC, whose magnitudes reach order one. The distributions of the  
246 large  $Ro$  values manifest as elongated filaments, fronts, and coherent vortices,  
247 indicating the occurrence of submesoscales.

248 In Figures 3a and 3b, we compare the depth-time distributions of the  
249 larger-scale and submesoscale KE averaged over the KLC region (i.e., the pink solid  
250 box in Figure 2c). Corresponding to the occurrence of the KLC between late  
251 December 2011 and early May 2012, the larger-scale KE was significantly elevated  
252 throughout the upper 200 m (Figure 3a). Although the KE of the KLC is surface  
253 intensified, its influence depth can reach 200 m. Actually, recent moored observations  
254 revealed that velocity signals of the KLC can penetrate to as deep as 2000 m in the

255 NESCS (Sun et al., 2020). The submesoscale KE overall has a good correspondence  
256 with the larger-scale KE, which showed elevated values during the KLC period  
257 between January to April 2012 (purple box in Figures 3b–c). Compared with the  
258 larger-scale KE, the submesoscale KE decreases more rapidly with depth and its  
259 magnitude is one order of magnitude smaller. Similar to the submesoscale KE, the  
260 root-mean-squared  $Ro$  (RMS- $Ro$ ) of submesoscales was also elevated during the KLC  
261 period, whose magnitude reached 0.2–0.3 at the sea surface.

262 Mixed-layer depth (MLD) and strain rate of background flows  
263 ( $\bar{\alpha} = \sqrt{(\bar{v}_y - \bar{u}_x)^2 + (\bar{v}_x + \bar{u}_y)^2}$ ) are key factors that determine the intensity of  
264 mixed-layer instability and strain-induced frontogenesis, respectively. In order to  
265 better understand the temporal modulations of submesoscale activities, in Figure 4,  
266 we compare the time series of upper 100-m-averaged submesoscale KE in the KLC  
267 region and region-averaged MLD and  $\bar{\alpha}$ . It shows that in the KLC region, the  
268 submesoscale KE is well correlated with  $\bar{\alpha}$  with the Pearson correlation coefficient  
269 ( $R$ ) reaching 0.46 (Figure 4a;  $R = 0.094$  for the 95% confidence level). With respect to  
270 the MLD, however, it is weakly correlated with the submesoscale KE at the  
271 intra-seasonal time scale with  $R = 0.14$  (Figure 4b). This is different from previous  
272 results found in open oceans that submesoscale quantities have good correlations with  
273 MLD at the seasonal time scale corresponding to the seasonal modulation of  
274 mixed-layer instability (e.g., Dong et al., 2020; Puzina et al., 2021; Thompson et al.,  
275 2016; Yu et al., 2019). The results found here suggest that submesoscales in the KLC  
276 may primarily be generated by strain-induced frontogenesis while the role of

277 mixed-layer instability may be secondary. To test the sensitivity of the above  
278 correlations regarding the time and area averages, we change the averaging window  
279 of the time series to 5 and 20 days and change the averaging area to a smaller KLC  
280 region (purple dashed box in Figure 2c). The results show that the values of  $R$  only  
281 have slight changes and they were not sensitive to the slight changes of time and  
282 space averaging windows (Figures S2 and S3).

283       Regarding the submesoscales in the KLC region, there are two things that  
284 deserve to be noted. First, strong submesoscales also occurred in early and mid  
285 December 2011, although the KLC did not form yet (Figures 2a and 3b–c). During  
286 that period, the MLD quickly deepened due to ocean’s heat loss to atmosphere (Figure  
287 3), which means quick accumulation of available potential energy within the mixed  
288 layer. Therefore, the strong submesoscales in December were likely generated by  
289 enhanced mixed-layer instability at that time (Boccaletti et al., 2007; Callies et al.,  
290 2016). Second, although the strength of submesoscales decreases rapidly with depth,  
291 their influence depth can reach 100 m, which is larger than the MLD (i.e., maximum  
292 of 50 m in winter). This phenomenon is consistent with recent submesoscale resolving  
293 in situ observations (e.g., Yu et al., 2019; Zhang Z., 2021).

## 294 **4 Energy cascade associated with submesoscales**

### 295 **4.1 Spatiotemporal characteristics of submesoscale energy cascade**

296       In order to study submesoscale energy cascade in the KLC region, we  
297 calculated the KER using the coarse-graining approach (section 2.3). From the

298 spatiotemporal variations of KER in Figure 5, we find that the KLC and the path of  
299 Kuroshio in the Luzon Strait and east of Taiwan are hotspots of submesoscale energy  
300 cascade, where the magnitude of KER reaches  $O(10^{-6}-10^{-5}) \text{ m}^2 \cdot \text{s}^{-3}$ . Along the path of  
301 the Kuroshio in the Luzon Strait and east of Taiwan, the KER is mainly positive,  
302 indicating the dominance of forward energy cascade. With respect to the KLC region,  
303 although the region-averaged KER is overall positive (Figure 6), its sign and  
304 magnitude are highly non-uniform in aspects of both space and time. Specifically, at  
305 the periphery of the KLC (i.e., along its axis), the KER tends to be positive most of  
306 the time. Within the core of the KLC, the KER was primarily positive in the growth  
307 period of KLC in January but negative values (i.e., inverse cascade) became more  
308 evident during the mature period of KLC, particularly in March.

309         To evaluate the role of KER in the energy budget and thus evolution of KLC,  
310 we compare the region-averaged KER in the KLC region with the material derivative  
311 of the larger-scale KE (i.e.,  $\text{DKE}/\text{Dt}$ ) therein (Figures 6 and 7). The upper 100  
312 m-averaged time series of  $\text{DKE}/\text{Dt}$  in the KLC region shows significant intra-seasonal  
313 variations with period of 10–20 days (Figure 6). At the intra-seasonal time scale, the  
314  $\text{DKE}/\text{Dt}$  is negatively correlated with the KER with  $R$  of -0.39 ( $R = -0.18$  for the 95%  
315 confidence level). For the positive and negative values of KER, they mostly  
316 correspond to decrease and increase of larger-scale KE, respectively. As a result, the  
317 composite mean profile of  $\text{DKE}/\text{Dt}$  during the periods of positive (negative) KER is  
318 negative (positive) throughout the upper 200 m (Figure 7). If the upper 200 m is  
319 considered, the ratios between the RMS values of KER and  $\text{DKE}/\text{Dt}$  during the

320 periods of positive and negative KER reach 0.66 and 0.50, respectively. The above  
321 results demonstrate that submesoscale energy cascade is a leading order process in the  
322 energy budget of the larger-scale KE in the KLC region. In another word,  
323 submesoscales can significantly modulate the intra-seasonal variation of KLC through  
324 direct or inverse energy cascade. Sensitivity analysis shows that the above  
325 correlations are also insensitive to the slight changes of time and space averaging  
326 windows (Figures S4 and S5).

#### 327 **4.2 Roles of strain and divergence**

328 The recent study of Srinivasan et al. (2022) suggested that horizontal  
329 divergence ( $\bar{\delta} = \bar{u}_x + \bar{v}_y$ ) and  $\bar{\alpha}$  (i.e., strain rate) of background flows are two  
330 important factors that determine submesoscale energy cascade (i.e., KER). In order to  
331 understand the roles of  $\bar{\delta}$  and  $\bar{\alpha}$ , we compare their mean spatial distributions in  
332 March 2012 with the corresponding KER at the 5-m depth (Figures 8a–c). It shows  
333 that except for the vicinity of islands, large values of  $\bar{\alpha}$  mainly occur at the  
334 periphery of KLC. Although the sign of KER seems independent of the  $\bar{\alpha}$ , their  
335 magnitudes have similar spatial distributions in the KLC region. That is to say, large  
336 magnitudes of KER tend to occur in regions with strong strain field. By comparing  
337 KER with  $\bar{\delta}$ , we find that the forward (inverse) energy cascade occurs more  
338 frequently in regions with flow convergence (divergence). These results suggest that  
339 the strength and direction of submesoscale energy cascade depend on  $\bar{\alpha}$  and  $\bar{\delta}$ ,  
340 respectively. In order to verify the above phenomenon, we further calculate the spatial

341 correlations between the KER and  $\bar{\delta} / |\bar{\delta}| \times \bar{\alpha}$  using all of the grid points in the  
342 KLC region (Figure 8d). During the KLC period, the  $R$  is nearly always negative, its  
343 values are generally between -0.45 and -0.15 (except for mid April). The mean value  
344 of  $R$  is -0.28, which far exceeds the 95% confidence level (i.e.,  $R = -0.014$ ). Similar  
345 results also apply to other depths in the upper 200 m (Figure S6) except that the  $R$  is  
346 slightly smaller than that at near surface. Therefore, the quantity  $\bar{\delta} / |\bar{\delta}| \times \bar{\alpha}$  is a  
347 useful indicator that can be used to judge the magnitude and sign of submesoscale  
348 energy cascade.

## 349 **5 Salt and heat transports by submesoscales**

350 Previous studies demonstrated that the anticyclonic eddy shedding from KLC  
351 could transport a huge amount of warm and salty water into the NESCS interior  
352 within a short time (e.g., Zhang et al., 2017). However, by this warm and salty water  
353 transport mechanism, no heat nor salt will enter the NESCS interior in absence of  
354 eddy shedding from the KLC. Given that the KLC behaves as a mesoscale salt and  
355 temperature filament, and that there are energetic submesoscales at the periphery of  
356 KLC, it is theoretically expected that submesoscales can contribute to the salt and heat  
357 transports into the NESCS through the horizontal mixing effect. In this section, the  
358 roles of submesoscales in the salt and heat fluxes as well as the corresponding  
359 westward transports across the Luzon Strait are quantitatively evaluated.

### 360 **5.1 Submesoscale salt and heat fluxes and diffusivities**

361 Before discussing submesoscales-induced salt and heat fluxes, we first

362 examine the characteristics of KLC water (i.e., water within the KLC) by comparing  
363 its mean temperature-salinity ( $T$ - $S$ ) diagram with that of the typical Kuroshio water  
364 and the NESCS water (Figure 9). The significant difference between the NESCS  
365 water and the Kuroshio water is that the latter is warmer and saltier in the upper layer  
366 above  $25.55 \sigma_0$  (mean depth at  $\sim 250$  m) but colder and fresher below that. For the  
367 Kuroshio water, the maximum temperature and salinity can reach  $26.7$  °C and  $34.75$   
368 g/kg, respectively, while the respective values for the NESCS water are only  $26$  °C  
369 and  $34.55$  g/kg. In the upper layer, the mean  $T$ - $S$  property of the KLC water is  
370 between the Kuroshio water and NESCS water. At the KLC edge, the  $T$ - $S$  properties  
371 are close to the Kuroshio water but the temperature and salinity are slightly lower on  
372 the same isopycnals. Here, the KLC edge is defined as the SSH contour with the  
373 highest average salinity at  $150$  m (i.e., the main axis of KLC), where the vertical  
374 salinity maximum occurs. As we will discuss below, the slightly lower temperature  
375 and salinity at the KLC edge is associated with the isopycnal mixing or tracer  
376 transport caused by submesoscales.

377         Based on the method in section 2.4, we calculate the divergent component of  
378 the isopycnal salt flux induced by submesoscales ( $SF_d$ ). In Figure 10, we show the  
379 spatial distributions of salinity and  $SF_d$  on the  $23.5 \sigma_0$  isopycnal (i.e., at depth of  
380  $120$ – $150$  m) at different KLC stages. It shows that the KLC edge behaves like a salty  
381 mesoscale filament that is saltier than the waters inside and outside of the KLC, which  
382 is consistent with the result in Figure 9. Due to the combination of large salinity  
383 gradient and energetic submesoscales, it shows large down-gradient  $SF_d$  at the KLC

384 filament. The magnitude of  $|SF_D|$  reaches up to  $O(10^{-2})$  g/kg·m/s, which is overall  
385 two orders of magnitude larger than that in absence of KLC (Figure S7). The large  
386 values of  $|SF_D|$  mainly occur in the southern and western part of the KLC filament  
387 where salinity gradient is strong. Corresponding to the opposite salinity gradient at the  
388 two sides of the KLC filament, direction of the  $SF_D$  is mainly southwestward at the  
389 outer but northeastward at the inner side of the KLC's southwestern edge. Due to the  
390 large down-gradient  $SF_D$  associated with submesoscales, the water at the KLC edge  
391 gradually becomes fresher along its flowing direction. It is also found that after the  
392 Kuroshio flows out of the NESCS and reaches east of Taiwan, its salinity becomes  
393 much lower than that east of Luzon. This salinity reduction along the Kuroshio path  
394 becomes less evident during the leaping-path period of Kuroshio (Figure S7). The  
395 submesoscales also induce elevated and down-gradient  $HF_D$  at the KLC edge whose  
396 magnitude reaches  $O(10^4)$  W/m<sup>2</sup> (Figure S8). The spatial distribution of  $HF_D$  is very  
397 similar to the  $SF_D$ , which is understandable because of the temperature-salinity  
398 compensation on the isopycnal. During the Kuroshio leaping-path period, the  $|HF_D|$   
399 is also significantly weakened (Figure S9). The above results suggest that  
400 submesoscales at the KLC not only take warmer and saltier Kuroshio water into the  
401 NESCS but also significantly modulate the water property of Kuroshio through  
402 isopycnal mixing.

403         Based on Eq. (3) in section 2.4, we calculate the 15-day averaged  
404 submesoscale salt diffusivity  $K_S$  whose time-dependent spatial distributions are  
405 shown in Figure 11. We find that the  $K_S$  is strongly inhomogeneous in aspect of

406 spatial distribution. The large values of  $K_s$  primarily occur in the KLC region where  
407 submesoscales are active. Corresponding to the down-gradient  $SF_D$ , the  $K_s$  is  
408 dominantly positive at the KLC edge. Its magnitude there reaches  $O(10^2)$   $m^2/s$ , which  
409 is 1–2 orders of magnitude larger than that in the NESCS interior. Although negative  
410 values of  $K_s$  also occur, particularly in the interior area of the KLC, their magnitude  
411 is overall smaller than the positive ones (i.e., smaller than  $100 m^2/s$ ). The  
412 submesoscale heat diffusivity  $K_\theta$  also reaches  $O(10^2)$   $m^2/s$  at the KLC edge, and  
413 both its magnitude and spatial distribution are overall similar to  $K_s$  (Figure S10).

## 414 **5.2 Submesoscales-induced salt and heat transports**

415 Based on the method in section 2.4, we calculated the submesoscale salt and  
416 heat transports across the KLC main axis. The mean vertical profile of submesoscale  
417 salt and heat transports per unit depth (i.e., STD and HTD) during the maturity period  
418 of KLC (i.e., March, 2012) is shown in Figure 12a. Both the salt and heat transports  
419 are from the KLC to the NESCS (i.e., positive values) throughout the upper 200 m,  
420 whose magnitudes are of  $O(10^4)$   $g/kg \cdot m^2/s$  and  $O(10^{11})$   $W/m/s$ , respectively. Although  
421 submesoscales are generally surface intensified, the maximum submesoscale salt  
422 transport occurs at 50 m with magnitude reaching  $5.3 \times 10^4$   $g/kg \cdot m^2/s$ , which is 26  
423 times larger than that at sea surface (i.e.,  $0.2 \times 10^4$   $g/kg \cdot m^2/s$ ). Similar to the vertical  
424 structure of the STD, the HTD is also subsurface intensified, but the maximum value  
425 of HTD appears at a deeper depth (i.e., 90 m).

426 Different from the salt and heat transports, the mean  $K_s$  and  $K_\theta$  at the KLC

427 main axis are surface intensified, whose magnitudes sharply decrease from  $\sim 450 \text{ m}^2/\text{s}$   
428 at surface to  $\sim 250 \text{ m}^2/\text{s}$  at 50 m depth. In the layer between 50–200 m the  $K_s$  and  
429  $K_\theta$  are overall between 100 and  $250 \text{ m}^2/\text{s}$ . The difference between submesoscale  
430 salt/heat transport and diffusivity is understandable because the former not only  
431 depends on diffusivity but also depends on the horizontal salt/heat gradient, which is  
432 subsurface intensified in the KLC region. Note that submesoscale salt/heat transport  
433 also exists in the leaping-path stage of Kuroshio (i.e., non-KLC periods) in the Luzon  
434 Strait, although its magnitude is smaller (Figures S7 and S9).

435 In Figure 13, we show the time series of the vertically integrated submesoscale  
436 salt transport (IST) and heat transport (IHT) across the Ku near the Luzon Strait  
437 (including both KLC and non-KLC periods). We find that the IST and IHT are  
438 predominately positive throughout the year, which suggests down-gradient salt and  
439 heat transports from the Kuroshio into the NESCS. The IST and IHT were  
440 significantly enhanced during the main KLC period between January and April, 2012  
441 and their magnitudes were largest in March 2012 when the KLC was at its mature  
442 stage. The time-mean IST during the KLC period reached  $1.78 \times 10^6 \text{ g/kg} \cdot \text{m}^3/\text{s}$ , which  
443 is 370% larger than the mean value during the non-KLC period ( $3.80 \times 10^5 \text{ g/kg} \cdot \text{m}^3/\text{s}$ ).  
444 Meanwhile, the time-mean IHT during the KLC period is 240% of that during  
445 non-KLC periods ( $8.65 \times 10^{12} \text{ W}$  vs.  $2.56 \times 10^{12} \text{ W}$ ). The larger IST and IHT during the  
446 KLC period are attributed to the combination of stronger submesoscales and longer  
447 integral along the Ku.

448 We need to note that the lifespan of the simulated KLC by the LLC4320 is

449 longer than the true KLCs observed by altimeter data, which has a mean lifespan of  
450 ~57 days (Zhang Z. et al., 2017; Sun et al., 2020). If we multiply the  
451 simulation-derived mean IST and IHT during the KLC period by the 57-day period  
452 (i.e., the mean lifespan of KLCs in the real ocean), we can roughly estimate that  
453 submesoscales associated with a KLC event can transport  $0.90 \times 10^{13}$  kg salt and  
454  $0.71 \times 10^{20}$  J heat into the NESCS. Zhang et al. (2017) analyzed the radius and  
455 temperature/salinity anomaly of the anticyclonic eddy shedding from the KLC based  
456 on the observation. According to the observational study, we can estimate that in  
457 terms of annual mean, the KLC eddy shedding can transport  $1.90 \times 10^{12}$  kg salt and  
458  $2.08 \times 10^{19}$  J heat into the NESCS, which are an order smaller than that associated with  
459 submesoscale IST and IHT during the KLC period, respectively. If the non-KLC  
460 period is also considered, we can roughly estimate that the westward salt and heat  
461 transports caused by submesoscales throughout the year (between October 1th, 2011  
462 and September 30th, 2012) are as high as  $2.77 \times 10^{13}$  kg and  $1.69 \times 10^{21}$  J, respectively.  
463 The above results demonstrate that when the Kuroshio is at the loop or leaping state  
464 (excluding leaking intrusion state), horizontal mixing effect of submesoscales is the  
465 dominant salt and heat transports mechanism from the Kuroshio to the NESCS while  
466 the role of KLC eddy shedding is secondary. Note that the above heat and salt  
467 transport values are very rough estimates, which need to be confirmed by  
468 high-resolution in situ observations in the future.

## 469 **6 Summary and discussion**

470 In this study, outputs of the  $1/48^\circ$  LLC4320 simulation were used to

471 investigate energy cascade and salt transport associated with submesoscales in the  
472 KLC region of the NESCS. The simulation results show that active submesoscales  
473 with  $O(1) Ro$  occurred in the upper 200 m in the KLC between January and April  
474 2012. The simulated submesoscale KE in the KLC region is well correlated with the  
475 background strain rate ( $\bar{\alpha}$ ) but poorly correlated with MLD, which suggests  
476 strain-induced frontogenesis may play a more important role than mixed-layer  
477 instability in the generations of these submesoscales during the KLC period.

478         The KLC region is a hotspot of submesoscale energy cascade with elevated  
479 KER values compared with other regions in the NESCS. Overall, KER is dominated  
480 by positive values or forward energy cascade in the KLC region, particularly along  
481 the main axis of KLC. In the interior area of KLC, however, inverse energy cascade  
482 becomes evident at the growth stage of KLC. The ratio between KER and material  
483 derivative of the larger-scale KE exceeds 0.5 in the upper 200 m and their time series  
484 have a good correlation, demonstrating that submesoscale energy cascade plays an  
485 important role in modulating the energy budget and thus evolution of KLC. We also  
486 find that the sign and magnitude of KER are to a large degree associated with the  
487 horizontal divergence ( $\bar{\delta}$ ) and  $\bar{\alpha}$ , respectively. As a result, KER has a significantly  
488 negative correlation with the parameter  $\bar{\delta} / |\bar{\delta}| \times \bar{\alpha}$ , which provides a great index to  
489 infer submesoscale energy cascade from larger-scale current velocity in the future.

490         The active submesoscales in the KLC region result in large down-gradient salt  
491 and heat fluxes (i.e.,  $SF_D$  and  $HF_D$ ) and positive horizontal diffusivities (i.e.,  $K_s$   
492 and  $K_\rho$ ). At the KLC edge, magnitudes of  $SF_D$  and  $HF_D$  reach  $O(10^{-2})$  m/s and

493  $O(10^4)$  W/m<sup>2</sup>, respectively, which are 1–2 orders larger than those in the NESCS  
494 interior and those during the non-KLC period. Corresponding to the down-gradient  
495  $SF_D$  and  $HF_D$ , the  $K_s$  and  $K_\theta$  are overall positive at the KLC edge with values  
496 reaching  $O(10^2)$  m<sup>2</sup>/s. If the real lifespan of KLC is considered, the submesoscale  
497  $SF_D$  and  $HF_D$  associated with a KLC event can roughly transport  $0.90 \times 10^{13}$  kg salt  
498 and  $0.71 \times 10^{20}$  J heat into the NESCS, respectively. The above values are one order  
499 larger than the equivalent salt and heat transports caused by KLC eddy shedding  
500 (Zhang et al., 2017). When the non-KLC period is also included, westward salt and  
501 heat transports induced by submesoscales throughout the year reach  $2.77 \times 10^{13}$  kg and  
502  $1.69 \times 10^{21}$  J, respectively. The above findings demonstrate that when the Kuroshio is  
503 at the loop or leaping state, horizontal mixing effect of submesoscales is the dominant  
504 mechanism for salt and heat transports from the Kuroshio to the NESCS.

505         This study reveals that the KLC can induce active submesoscales in the  
506 NESCS. Interactions between submesoscales and KLC significantly modulate the  
507 variations of KLC in terms of energetics. In addition, the horizontal mixing effect of  
508 submesoscales can indeed transport a huge amount of salt and heat from the Kuroshio  
509 into the NESCS. It suggests that in addition to the well-known KLC itself, the active  
510 submesoscales induced by KLC also significantly modulate the energy, salt, and heat  
511 budgets in the NESCS. Given that the KLC has distinct seasonal-to-decadal variations  
512 (e.g., Sun et al., 2020), how it will modulate the temporal variations of submesoscales  
513 and how these submesoscales further modulate the low-frequency variations of energy  
514 and salt budget in the NESCS also deserves to be studied in the future. We should

515 acknowledge that the analysis in this study mainly relies on the submesoscale  
516 permitting simulation (with resolution of ~2 km), the quantitative roles of  
517 submesoscales in the energy and salt budget issues in the NESCS need to be  
518 examined in the future based on submesoscale resolving observations.

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### 525 **Open Research**

526 The LLC4320 is available at <https://data.nas.nasa.gov/ecco/data.php>. The altimeter data were  
527 downloaded from <https://cds.climate.copernicus.eu/cdsapp#!/search?text=aviso>.

528

529 **References**

- 530 Alford, M. H., Peacock, T., MacKinnon, J. A., Nash, J. D., Buijsman, M. C., Centurioni, L. R., et  
531 al. (2015). The formation and fate of internal waves in the South China Sea. *Nature*,  
532 *521*(7550), 65–69. <https://doi.org/10.1038/nature14399>
- 533 Aluie, H., Hecht, M., & Vallis, G. K. (2018). Mapping the Energy Cascade in the North Atlantic  
534 Ocean: The Coarse-Graining Approach. *Journal of Physical Oceanography*, *48*(2), 225–244.  
535 <https://doi.org/10.1175/JPO-D-17-0100.1>
- 536 Boccaletti, G., Ferrari, R., & Fox-Kemper, B. (2007). Mixed Layer Instabilities and  
537 Restratification. *Journal of Physical Oceanography*, *37*(9), 2228–2250.  
538 <https://doi.org/10.1175/JPO3101.1>
- 539 Callies, J., Flierl, G., Ferrari, R., & Fox-Kemper, B. (2016). The role of mixed-layer instabilities in  
540 submesoscale turbulence. *Journal of Fluid Mechanics*, *788*, 5–41.  
541 <https://doi.org/10.1017/jfm.2015.700>
- 542 Cao, H., Jing, Z., Fox-Kemper, B., Yan, T., & Qi, Y. (2019). Scale Transition From Geostrophic  
543 Motions to Internal Waves in the Northern South China Sea. *Journal of Geophysical*  
544 *Research: Oceans*, *124*(12), 9364–9383. <https://doi.org/10.1029/2019JC015575>
- 545 Cao, H., Meng, X., Jing, Z., & Yang, X. (2022). High-resolution simulation of upper-ocean  
546 submesoscale variability in the South China Sea: Spatial and seasonal dynamical regimes.  
547 *Acta Oceanologica Sinica*, *41*(7), 26–41. <https://doi.org/10.1007/s13131-022-2014-4>
- 548 Capet, X., McWilliams, J. C., Molemaker, M. J., & Shchepetkin, A. F. (2008). Mesoscale to  
549 Submesoscale Transition in the California Current System. Part III: Energy Balance and Flux.  
550 *Journal of Physical Oceanography*, *38*(10), 2256–2269.

551 <https://doi.org/10.1175/2008JPO3810.1>

552 D'Asaro, E., Lee, C., Rainville, L., Harcourt, R., & Thomas, L. (2011). Enhanced Turbulence and  
553 Energy Dissipation at Ocean Fronts. *Science*, 332(6027), 318–322.  
554 <https://doi.org/10.1126/science.1201515>

555 Dong, J., & Zhong, Y. (2018). The spatiotemporal features of submesoscale processes in the  
556 northeastern South China Sea. *Acta Oceanologica Sinica*, 37(11), 8–18.  
557 <https://doi.org/10.1007/s13131-018-1277-2>

558 Dong, J., Fox-Kemper, B., Zhang, H., & Dong, C. (2020). The Seasonality of Submesoscale  
559 Energy Production, Content, and Cascade. *Geophysical Research Letters*, 47(6).  
560 <https://doi.org/10.1029/2020GL087388>

561 Eyink, G. L. (2005). Locality of turbulent cascades. *Physica D: Nonlinear Phenomena*, 207(1–2),  
562 91–116. <https://doi.org/10.1016/j.physd.2005.05.018>

563 Gan, J., Liu, Z., & Hui, C. R. (2016). A Three-Layer Alternating Spinning Circulation in the South  
564 China Sea. *Journal of Physical Oceanography*, 46(8), 2309–2315.  
565 <https://doi.org/10.1175/JPO-D-16-0044.1>

566 Germano, M. (1992). Turbulence: the filtering approach. *Journal of Fluid Mechanics*, 238, 325–  
567 336. <https://doi.org/10.1017/S0022112092001733>

568 Gula, J., Molemaker, M. J., & McWilliams, J. C. (2016). Topographic generation of submesoscale  
569 centrifugal instability and energy dissipation. *Nature Communications*, 7(1), 12811.  
570 <https://doi.org/10.1038/ncomms12811>

571 Huang, X., Chen, Z., Zhao, W., Zhang, Z., Zhou, C., Yang, Q., & Tian, J. (2016). An extreme  
572 internal solitary wave event observed in the northern South China Sea. *Scientific Reports*,

573 6(1), 30041. <https://doi.org/10.1038/srep30041>

574 Jayne, S. R., & Marotzke, J. (2002). The Oceanic Eddy Heat Transport. *Journal of Physical*  
575 *Oceanography*, 32(12), 3328–3345.  
576 [https://doi.org/10.1175/1520-0485\(2002\)032<3328:TOEHT>2.0.CO;2](https://doi.org/10.1175/1520-0485(2002)032<3328:TOEHT>2.0.CO;2)

577 Leonard, A. (1975). Energy Cascade in Large-Eddy Simulations of Turbulent Fluid Flows. In  
578 *Advances in Geophysics* (Vol. 18, pp. 237–248). Elsevier.  
579 [https://doi.org/10.1016/S0065-2687\(08\)60464-1](https://doi.org/10.1016/S0065-2687(08)60464-1)

580 Li, J., Dong, J., Yang, Q., & Zhang, X. (2019). Spatial-temporal variability of submesoscale  
581 currents in the South China Sea. *Journal of Oceanology and Limnology*, 37(2), 474–485.  
582 <https://doi.org/10.1007/s00343-019-8077-1>

583 Lin, H., Liu, Z., Hu, J., Menemenlis, D., & Huang, Y. (2020). Characterizing meso- to  
584 submesoscale features in the South China Sea. *Progress in Oceanography*, 188, 102420.  
585 <https://doi.org/10.1016/j.pocean.2020.102420>

586 Mahadevan, A. (2016). The Impact of Submesoscale Physics on Primary Productivity of Plankton.  
587 *Annual Review of Marine Science*, 8(1), 161–184.  
588 <https://doi.org/10.1146/annurev-marine-010814-015912>

589 Mahadevan, A., & Tandon, A. (2006). An analysis of mechanisms for submesoscale vertical  
590 motion at ocean fronts. *Ocean Modelling*, 14(3–4), 241–256.  
591 <https://doi.org/10.1016/j.ocemod.2006.05.006>

592 Mahadevan, A., D’Asaro, E., Lee, C., & Perry, M. J. (2012). Eddy-Driven Stratification Initiates  
593 North Atlantic Spring Phytoplankton Blooms. *Science*, 337(6090), 54–58.  
594 <https://doi.org/10.1126/science.1218740>

595 McWilliams, J. C. (2016). Submesoscale currents in the ocean. *Proceedings of the Royal Society A:*  
596 *Mathematical, Physical and Engineering Sciences*, 472(2189), 20160117.  
597 <https://doi.org/10.1098/rspa.2016.0117>

598 Miao, M., Zhang, Z., Qiu, B., Liu, Z., Zhang, X., Zhou, C., et al. (2021). On Contributions of  
599 Multiscale Dynamic Processes to the Steric Height in the Northeastern South China Sea as  
600 Revealed by Moored Observations. *Geophysical Research Letters*, 48(14).  
601 <https://doi.org/10.1029/2021GL093829>

602 Naveira Garabato, A. C. N., Yu, X., Callies, J., Barkan, R., Polzin, K. L., Frajka-Williams, E. E., et  
603 al. (2022). Kinetic Energy Transfers between Mesoscale and Submesoscale Motions in the  
604 Open Ocean's Upper Layers. *Journal of Physical Oceanography*, 52(1), 75–97.  
605 <https://doi.org/10.1175/JPO-D-21-0099.1>

606 Puzina, O. S., Kubryakov, A. A., & Mizyuk, A. I. (2021). Seasonal and Vertical Variability of  
607 Currents Energy in the Sub-Mesoscale Range on the Black Sea Shelf and in Its Central Part.  
608 *Physical Oceanography*, 28(1). <https://doi.org/10.22449/1573-160X-2021-1-37-51>

609 Qiu, B., Chen, S., Klein, P., Wang, J., Torres, H., Fu, L.-L., & Menemenlis, D. (2018). Seasonality  
610 in Transition Scale from Balanced to Unbalanced Motions in the World Ocean. *Journal of*  
611 *Physical Oceanography*, 48(3), 591–605. <https://doi.org/10.1175/JPO-D-17-0169.1>

612 Qiu, B., Nakano, T., Chen, S., & Klein, P. (2022). Bi-Directional Energy Cascades in the Pacific  
613 Ocean From Equator to Subarctic Gyre. *Geophysical Research Letters*, 49(8).  
614 <https://doi.org/10.1029/2022GL097713>

615 Rocha, C. B., Gille, S. T., Chereskin, T. K., & Menemenlis, D. (2016). Seasonality of  
616 submesoscale dynamics in the Kuroshio Extension. *Geophysical Research Letters*, 43(21).

617 <https://doi.org/10.1002/2016GL071349>

618 Schubert, R., Gula, J., Greatbatch, R. J., Baschek, B., & Biastoch, A. (2020). The Submesoscale  
619 Kinetic Energy Cascade: Mesoscale Absorption of Submesoscale Mixed Layer Eddies and  
620 Frontal Downscale Fluxes. *Journal of Physical Oceanography*, 50(9), 2573–2589.  
621 <https://doi.org/10.1175/JPO-D-19-0311.1>

622 Shaw, P.-T. (1989). The intrusion of water masses into the sea southwest of Taiwan. *Journal of*  
623 *Geophysical Research*, 94(C12), 18213. <https://doi.org/10.1029/JC094iC12p18213>

624 Sheremet, V. A. (2001). Hysteresis of a Western Boundary Current Leaping across a Gap. *Journal*  
625 *of Physical Oceanography*, 31(5), 1247–1259.  
626 [https://doi.org/10.1175/1520-0485\(2001\)031<1247:HOAWBC>2.0.CO;2](https://doi.org/10.1175/1520-0485(2001)031<1247:HOAWBC>2.0.CO;2)

627 Srinivasan, K., Barkan, R., & McWilliams, J. C. (2022). *A forward energy flux at submesoscales*  
628 *driven by frontogenesis* (preprint). *Oceanography*. <https://doi.org/10.1002/essoar.10509991.1>

629 Su, J. (2004). Overview of the South China Sea circulation and its influence on the coastal  
630 physical oceanography outside the Pearl River Estuary. *Continental Shelf Research*, 24(16),  
631 1745–1760. <https://doi.org/10.1016/j.csr.2004.06.005>

632 Su, Z., Wang, J., Klein, P., Thompson, A. F., & Menemenlis, D. (2018). Ocean submesoscales as a  
633 key component of the global heat budget. *Nature Communications*, 9(1), 775.  
634 <https://doi.org/10.1038/s41467-018-02983-w>

635 Sun, Z., Zhang, Z., Qiu, B., Zhang, X., Zhou, C., Huang, X., et al. (2020). Three-Dimensional  
636 Structure and Interannual Variability of the Kuroshio Loop Current in the Northeastern South  
637 China Sea. *Journal of Physical Oceanography*, 50(9), 2437–2455.  
638 <https://doi.org/10.1175/JPO-D-20-0058.1>

639 Thomas, L. N., Tandon, A., & Mahadevan, A. (2008). Submesoscale processes and dynamics. In  
640 M. W. Hecht & H. Hasumi (Eds.), *Geophysical Monograph Series* (Vol. 177, pp. 17–38).  
641 Washington, D. C.: American Geophysical Union. <https://doi.org/10.1029/177GM04>

642 Thompson, A. F., Lazar, A., Buckingham, C., Naveira Garabato, A. C., Damerell, G. M., &  
643 Heywood, K. J. (2016). Open-Ocean Submesoscale Motions: A Full Seasonal Cycle of Mixed  
644 Layer Instabilities from Gliders. *Journal of Physical Oceanography*, *46*(4), 1285–1307.  
645 <https://doi.org/10.1175/JPO-D-15-0170.1>

646 Tian, J., Yang, Q., & Zhao, W. (2009). Enhanced Diapycnal Mixing in the South China Sea.  
647 *Journal of Physical Oceanography*, *39*(12), 3191–3203.  
648 <https://doi.org/10.1175/2009JPO3899.1>

649 Wang, G. (2003). Mesoscale eddies in the South China Sea observed with altimeter data.  
650 *Geophysical Research Letters*, *30*(21), 2121. <https://doi.org/10.1029/2003GL018532>

651 Yang, Q., Zhao, W., Liang, X., & Tian, J. (2016). Three-Dimensional Distribution of Turbulent  
652 Mixing in the South China Sea. *Journal of Physical Oceanography*, *46*(3), 769–788.  
653 <https://doi.org/10.1175/JPO-D-14-0220.1>

654 Yu, X., Naveira Garabato, A. C., Martin, A. P., Buckingham, C. E., Brannigan, L., & Su, Z. (2019).  
655 An Annual Cycle of Submesoscale Vertical Flow and Restratification in the Upper Ocean.  
656 *Journal of Physical Oceanography*, *49*(6), 1439–1461.  
657 <https://doi.org/10.1175/JPO-D-18-0253.1>

658 Zhang, J., Zhang, Z., Qiu, B., Zhang, X., Sasaki, H., Zhao, W., & Tian, J. (2021). Seasonal  
659 Modulation of Submesoscale Kinetic Energy in the Upper Ocean of the Northeastern South  
660 China Sea. *Journal of Geophysical Research: Oceans*, *126*(11).

661 <https://doi.org/10.1029/2021JC017695>

662 Zhang, X., Zhang, Z., McWilliams, J. C., Sun, Z., Zhao, W., & Tian, J. (2022). Submesoscale  
663 Coherent Vortices Observed in the Northeastern South China Sea. *Journal of Geophysical*  
664 *Research: Oceans*, 127(2), e2021JC018117. <https://doi.org/10.1029/2021JC018117>

665 Zhang, Z., Tian, J., Qiu, B., Zhao, W., Chang, P., Wu, D., & Wan, X. (2016). Observed 3D  
666 Structure, Generation, and Dissipation of Oceanic Mesoscale Eddies in the South China Sea.  
667 *Scientific Reports*, 6(1), 24349. <https://doi.org/10.1038/srep24349>

668 Zhang, Z., Zhao, W., Qiu, B., & Tian, J. (2017). Anticyclonic Eddy Sheddings from Kuroshio  
669 Loop and the Accompanying Cyclonic Eddy in the Northeastern South China Sea. *Journal of*  
670 *Physical Oceanography*, 47(6), 1243–1259. <https://doi.org/10.1175/JPO-D-16-0185.1>

671 Zhang, Z., Zhang, Y., Qiu, B., Sasaki, H., Sun, Z., Zhang, X., et al. (2020). Spatiotemporal  
672 Characteristics and Generation Mechanisms of Submesoscale Currents in the Northeastern  
673 South China Sea Revealed by Numerical Simulations. *Journal of Geophysical Research:*  
674 *Oceans*, 125(2), e2019JC015404. <https://doi.org/10.1029/2019JC015404>

675 Zhang, Z., Zhang, X., Qiu, B., Zhao, W., Zhou, C., Huang, X., & Tian, J. (2021). Submesoscale  
676 Currents in the Subtropical Upper Ocean Observed by Long-Term High-Resolution Mooring  
677 Arrays. *Journal of Physical Oceanography*, 51(1), 187–206.  
678 <https://doi.org/10.1175/JPO-D-20-0100.1>

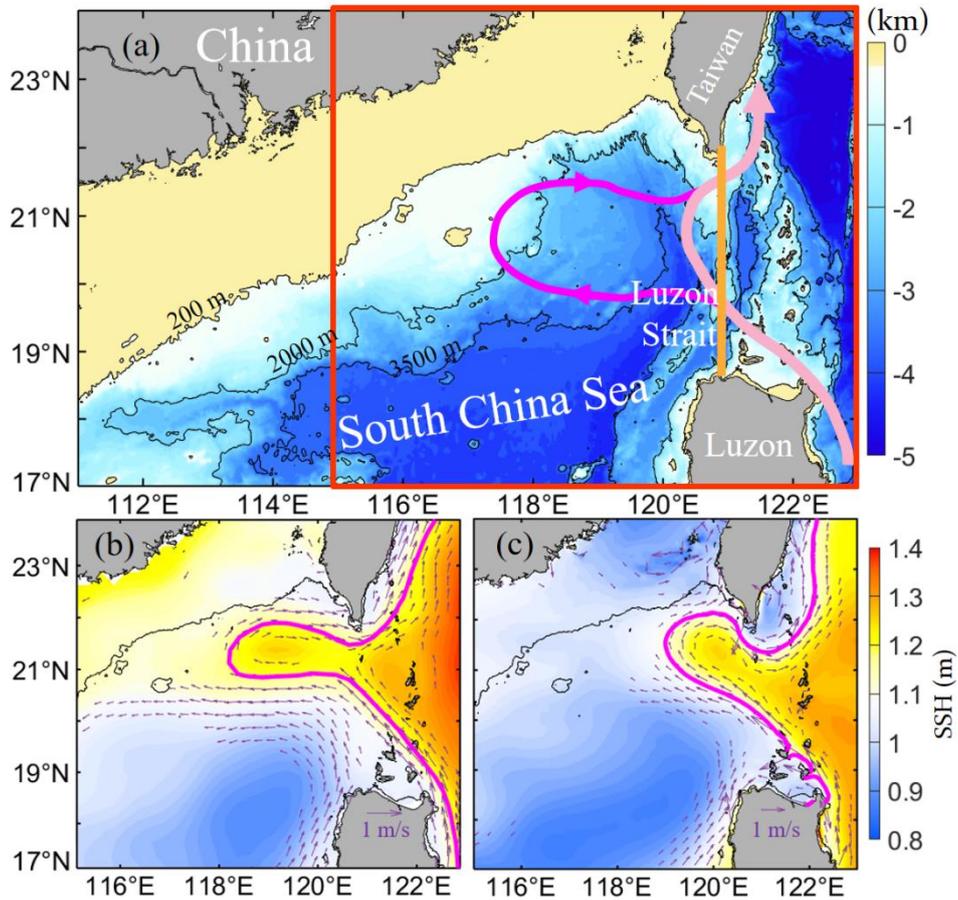
679 Zhang, Z., Liu, Y., Qiu, B., Luo, Y., Cai, W., Yuan, Q., et al. (2023). Submesoscale inverse energy  
680 cascade enhances Southern Ocean eddy heat transport. *Nature Communications*, 14(1), 1335.  
681 <https://doi.org/10.1038/s41467-023-36991-2>

682 Zhong, Y., Bracco, A., Tian, J., Dong, J., Zhao, W., & Zhang, Z. (2017). Observed and simulated

683 submesoscale vertical pump of an anticyclonic eddy in the South China Sea. *Scientific*

684 *Reports*, 7(1), 44011. <https://doi.org/10.1038/srep44011>

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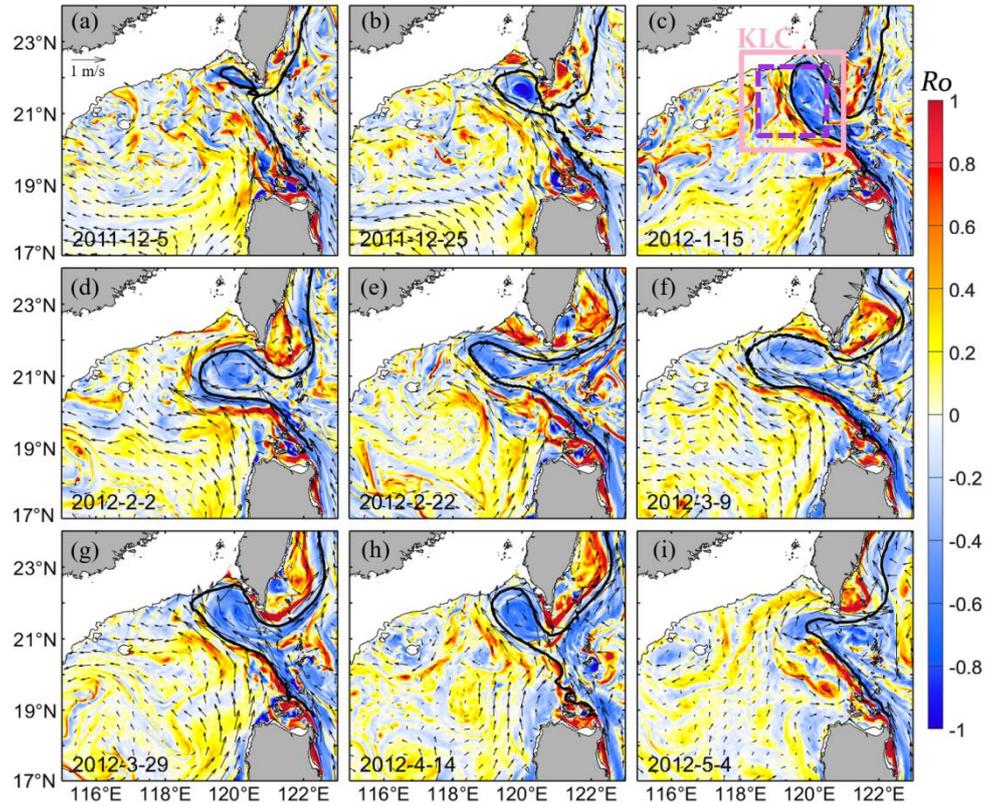


687

688 **Figure 1.** (a) Bathymetry in the northern South China Sea. Purple and pink lines  
 689 represent the looping and leaping paths of Kuroshio, respectively. The isobaths of 200,  
 690 2000, and 3500 m are denoted using black lines. Red box marks the study region, i.e.,  
 691 NESCS. Solid orange line represents the 120.8 °E section. (b) Distribution of  
 692 altimeter observed sea surface height (SSH) averaged in the winters (December,  
 693 January, and February) of 1999–2000, 2011–2012, 2016–2017, 2017–2018 when  
 694 prominent KLC occurred. Purple arrows are the corresponding absolute geostrophic  
 695 velocity at surface with magnitude larger than 0.2 m/s. (c) Same as (b) but for the  
 696 result from the LLC4320 simulation. Purple lines in (b, c) are the SSH contours of

697 1.19 m and 1.12 m, respectively, which roughly depict the path of KLC.

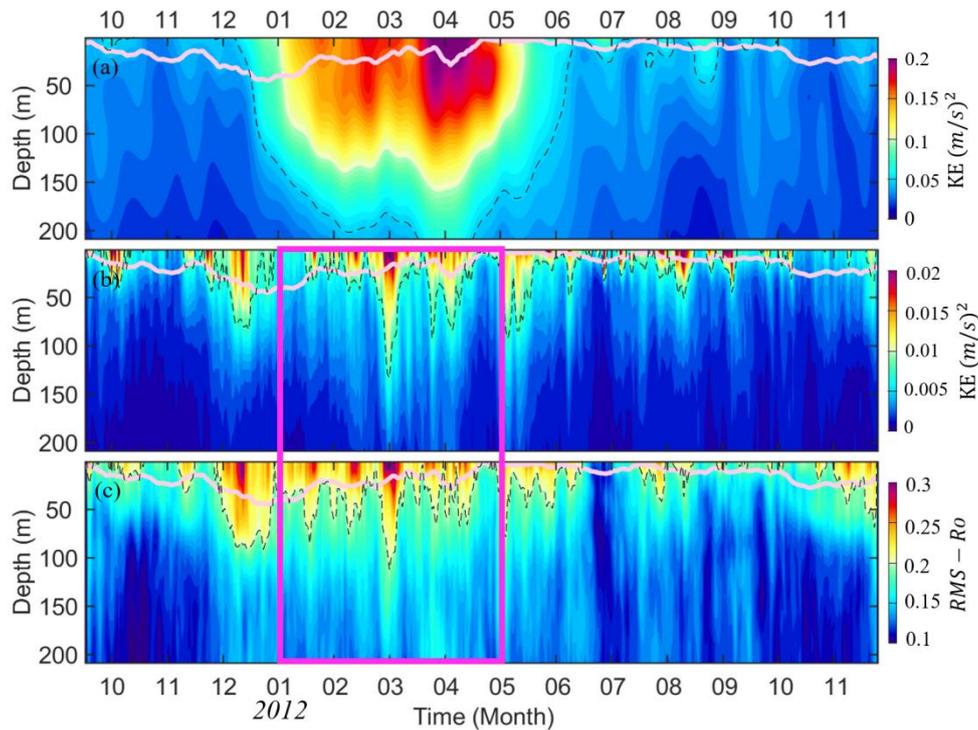
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700 **Figure 2.** Distributions of the daily-averaged Rossby number (color shading) and  
 701 current velocities (black arrows) at 5-m depth from the LLC4320 data. Regions with  
 702 water depth shallower than 200 m are masked using blank. The date is marked on the  
 703 left-bottom corner of each panel. Black thick line denotes the main axis of the KLC,  
 704 which is defined as the SSH contour with highest mean salinity at 150 m. Pink solid  
 705 box marks the KLC region. Purple dashed box marks a smaller KLC region where the  
 706 main part of KLC exists.

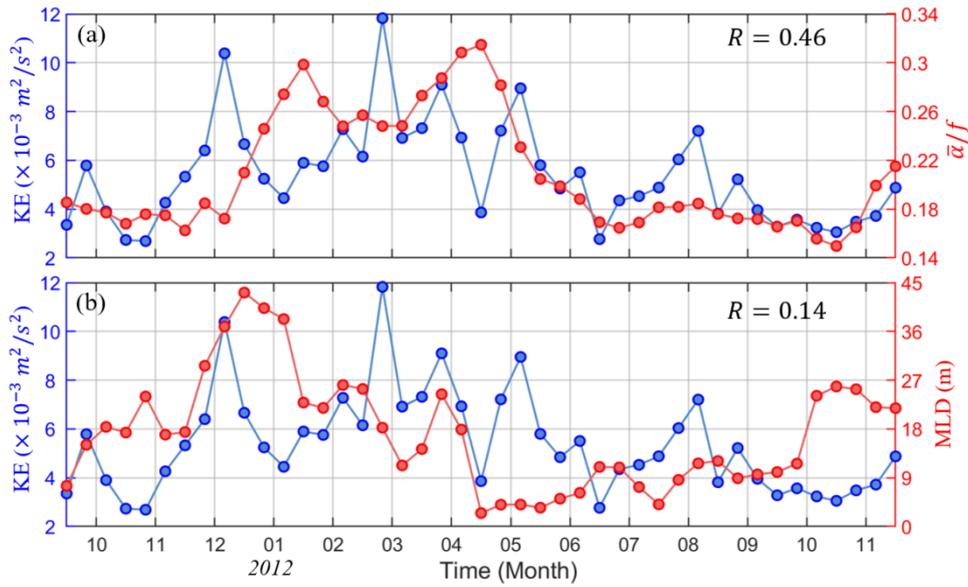
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709 **Figure 3.** Depth-time plot of (a) meso- to large- scale (i.e., larger-scale) KE, (b)  
 710 submesoscale KE, and (c) root-mean-squared submesoscale  $Ro$ . The results are  
 711 averaged over the KLC region denoted by the pink solid box in Figure 2c. Pink solid  
 712 line denotes the base of mixed layer averaged in the KLC region. Black dashed lines  
 713 in (a, b, c) are contours of  $0.05 \text{ m}^2/\text{s}^2$ ,  $0.008 \text{ m}^2/\text{s}^2$ , and 0.2, respectively. Purple square  
 714 in (b, c) denotes the main period of the KLC.

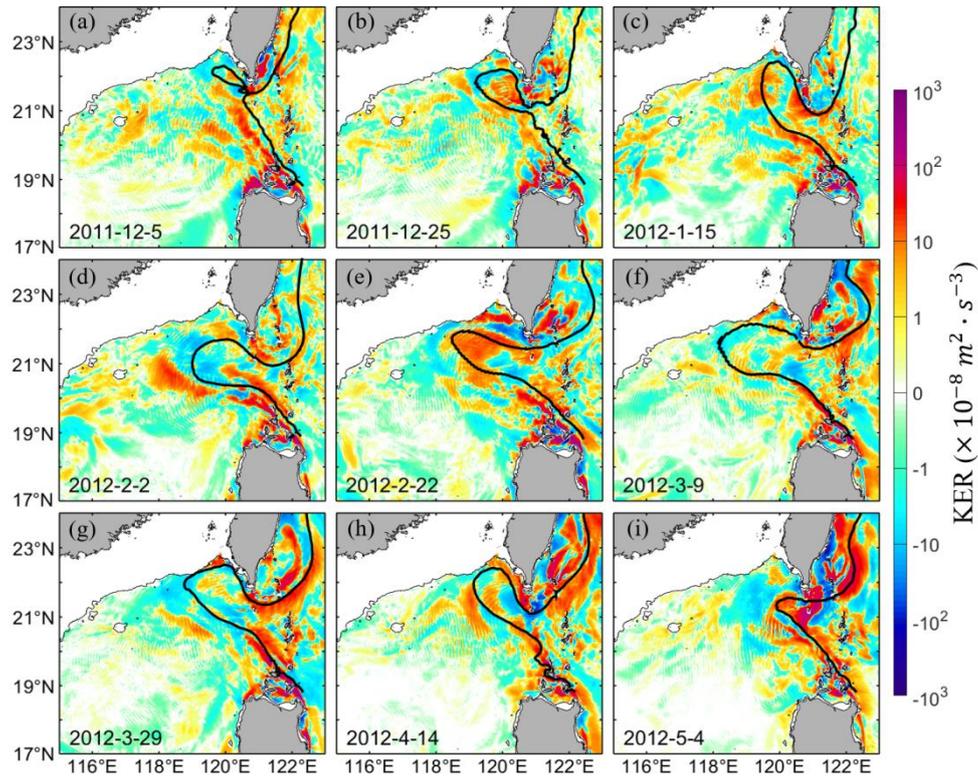
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717 **Figure 4.** (a) Comparison between upper 100-m-averaged submesoscale KE (blue;  
 718 y-axis on the left) and larger-scale strain rate normalized by dividing  $f$  (red; y-axis  
 719 on the right) averaged in the KLC region denoted by the pink solid box in Figure 2c.  
 720 Both the time series are weekly average and their correlation coefficient is marked on  
 721 the right-top corner ( $R = 0.094$  for the 95% confidence level). (b) Same as (a) except  
 722 that the red line denotes the MLD.

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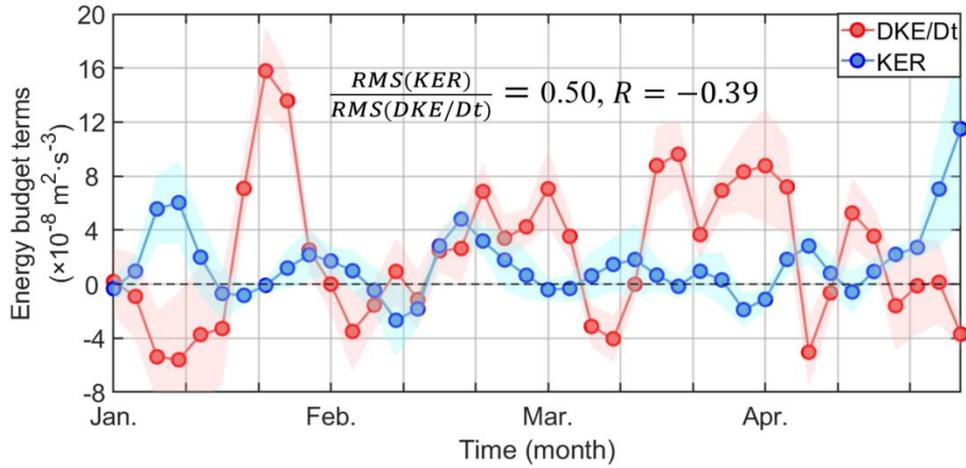


724

725 **Figure 5.** Same as Figure 2 but for the upper 100-m and 15-day averaged KER. Note

726 that values in the color bar is logarithmic.

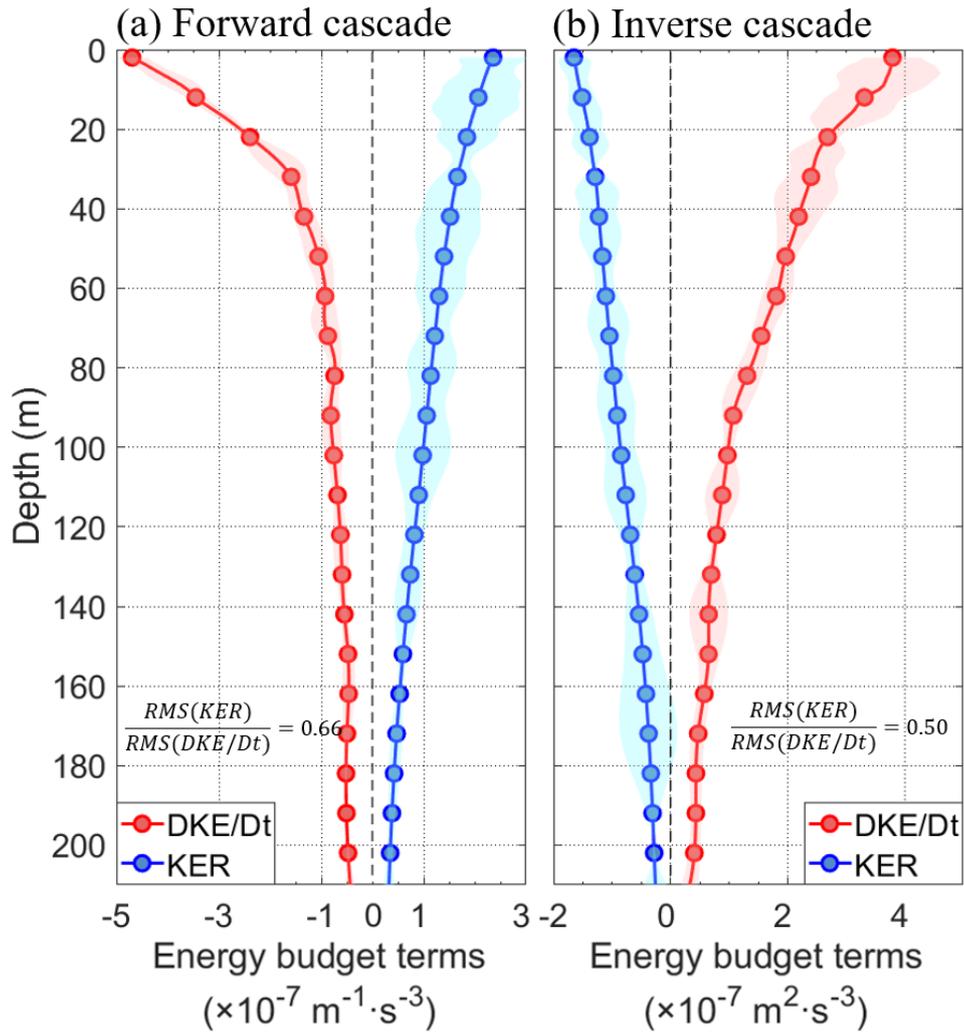
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729 **Figure 6.** Comparison between the upper 100-m-averaged KER (blue) and material  
 730 derivative of larger-scale KE (red; i.e., DKE/Dt) averaged in the KLC region. The  
 731 dots are 3-day averages. Ratio between the RMS values of KER and DKE/Dt and  
 732 correlation coefficient between their time series are marked ( $R = -0.18$  for the 95%  
 733 confidence level). The shadings denote the 95% confidence intervals of the  
 734 corresponding solid lines calculated using bootstrap method.

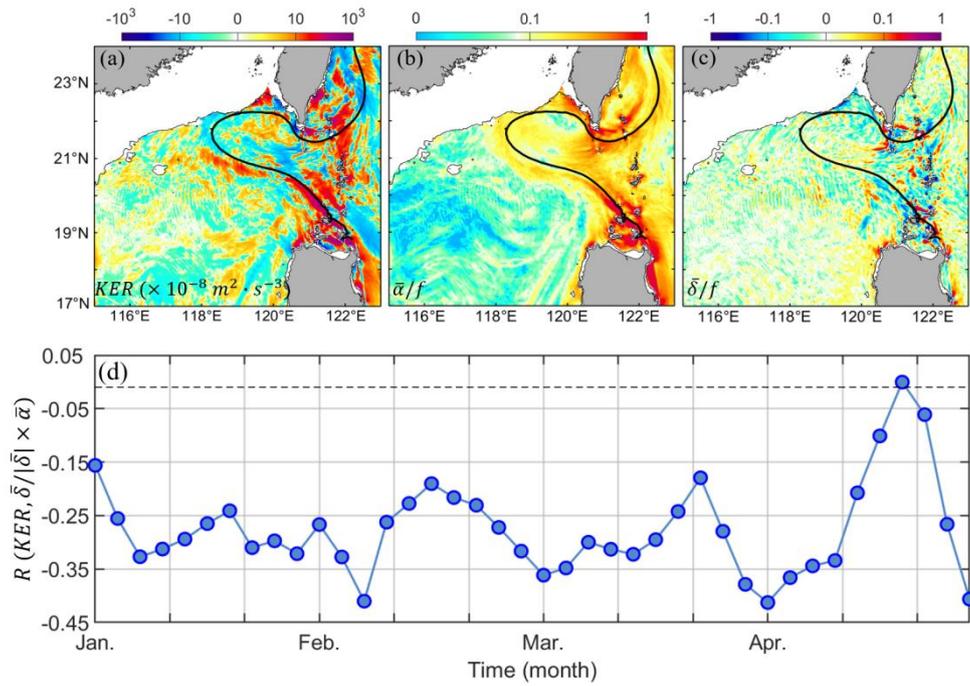
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737 **Figure 7.** (a) Compositely mean vertical profiles of KER (blue) and DKE/Dt (red)  
 738 when forward cascade occurs (i.e.,  $KER > 0$ ) during the KLC period. The results are  
 739 averaged in the KLC region. (b) Same as (a) but for the situation of inverse cascade  
 740 (i.e.,  $KER < 0$ ) The shadings denote the 95% confidence intervals of the corresponding  
 741 solid lines calculated using bootstrap method. Ratio between the RMS values of KER  
 742 and DKE/Dt is marked.

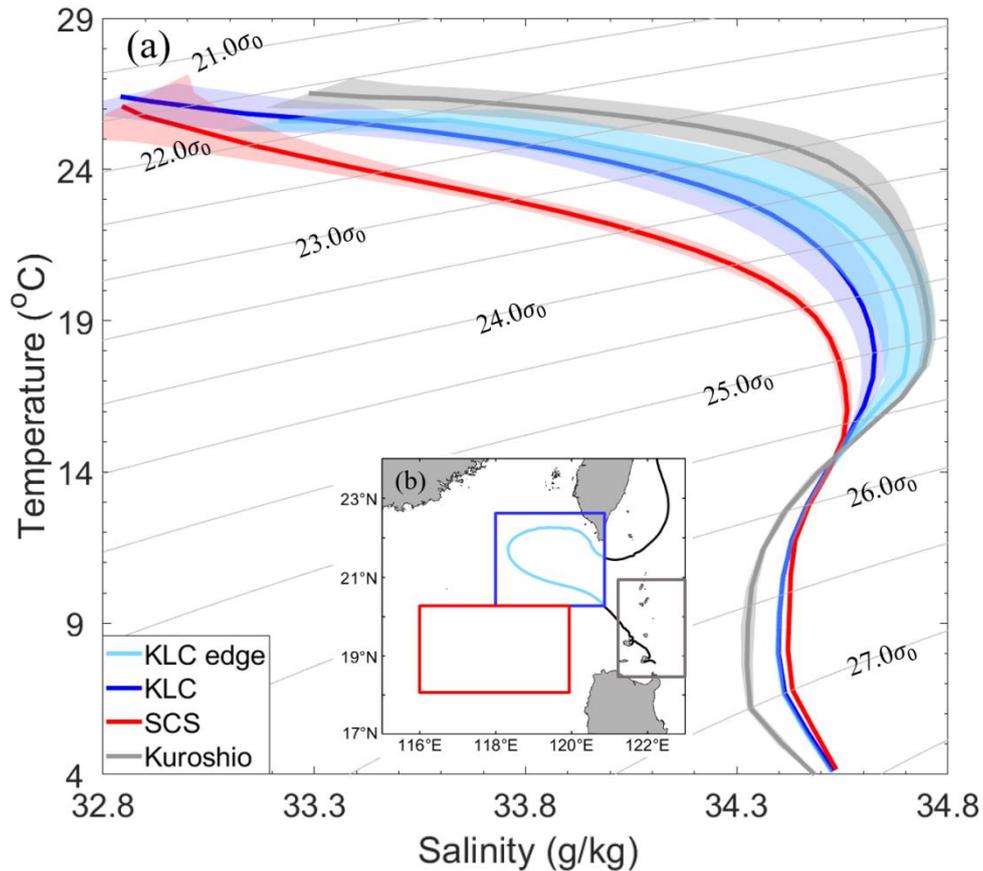
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745 **Figure 8.** Distributions of (a) KER, (b)  $\bar{\alpha}/f$ , and (c)  $\bar{\delta}/f$  at 5-m depth averaged  
 746 in March, 2012. Regions with water depth shallower than 200 m are masked using  
 747 blank. Black thick line denotes the main axis of KLC (same meaning with those in  
 748 Figure 2). Color bars are all expressed in logarithmic scale. (d) Time-dependent  
 749 correlation coefficients between KER and  $\bar{\delta}/|\bar{\delta}| \times \bar{\alpha}$  at 5-m depth calculated using  
 750 all grid points in the KLC region at each time step (i.e., 3-day average). Black dashed  
 751 line represents the 95% confidence level.

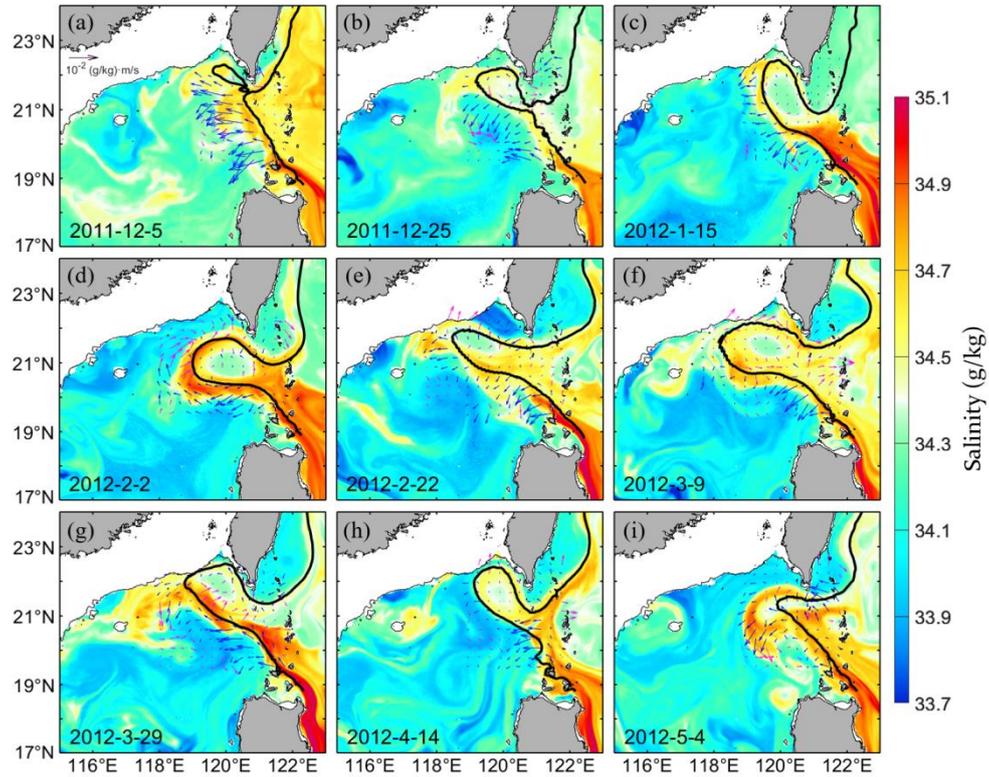
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754 **Figure 9.** *T-S* diagrams of different water masses in the NESCS and Luzon Strait  
 755 derived from the LLC4320 data. Solid lines and color shadings denote the mean *T-S*  
 756 curves and their standard deviations during the KLC period, respectively. Red, gray,  
 757 dark blue, and light blue lines denote the NESCS water, the Kuroshio water, and  
 758 waters in the KLC region and at the KLC edge, respectively. The spatial scopes of  
 759 different water masses are marked using squares or curve in (b) with same colors with  
 760 the corresponding *T-S* curves in (a). The gray oblique lines in (a) are isopycnic lines  
 761 from  $21.0\sigma_0$  to  $27.5\sigma_0$ .

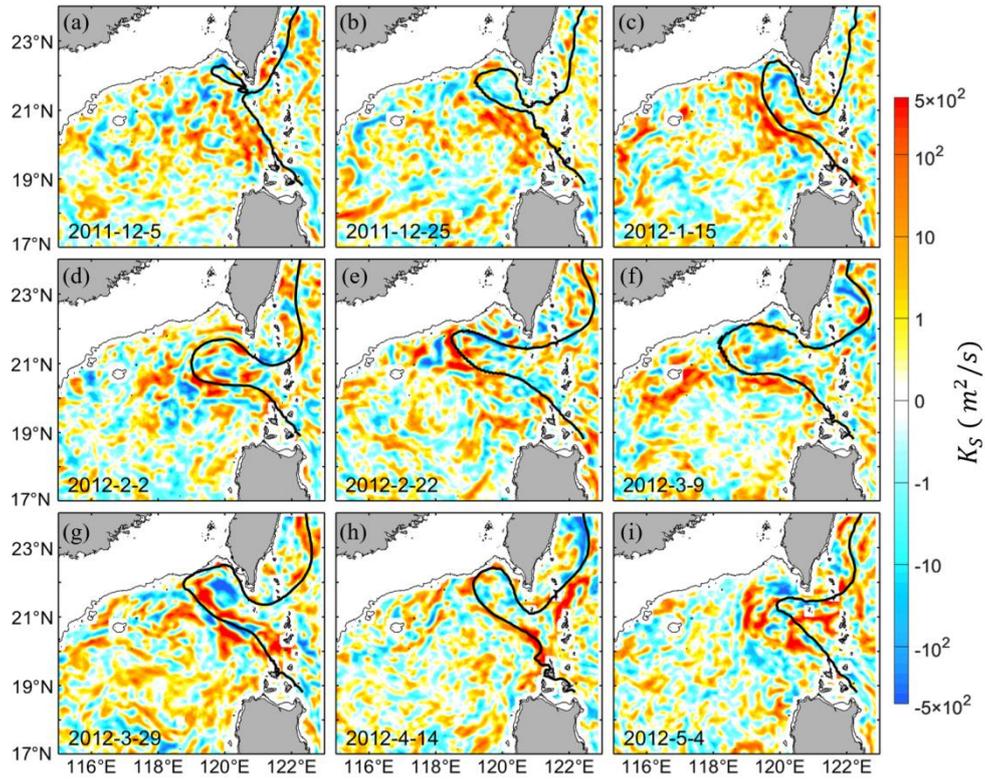
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764 **Figure 10.** Same as Figure 5 but for the 15-day-averaged salinity (color shading) and  
 765 divergence component of submesoscale salt flux ( $SF_D$ ; arrows) on the  $23.5\sigma_0$   
 766 isopycnal. Blue and purple arrows denote that  $SF_D$  has a westward and eastward  
 767 zonal component, respectively.

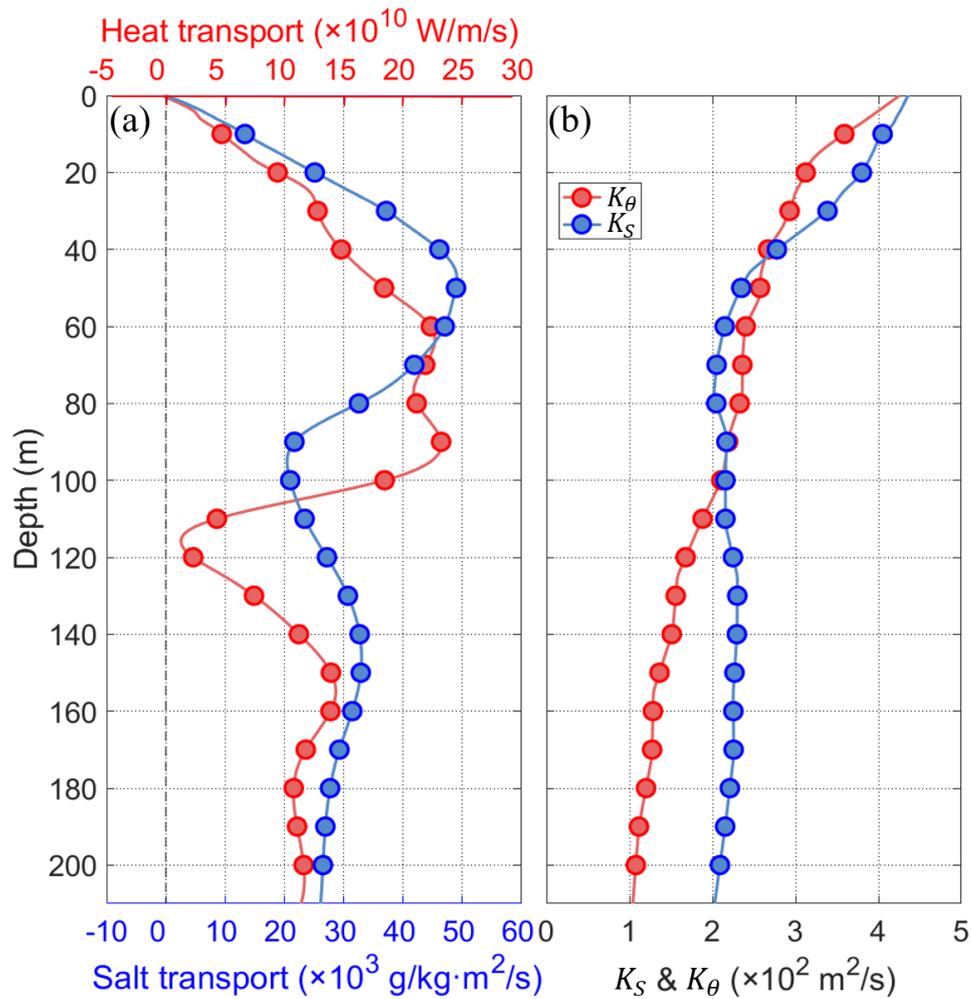
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770 **Figure 11.** Same as Figure 10 but for the submesoscale salt diffusivity (i.e.,  $K_S$ ) on  
 771 the  $23.5\sigma_0$  isopycnal. Note that color bar is expressed in logarithmic scale.

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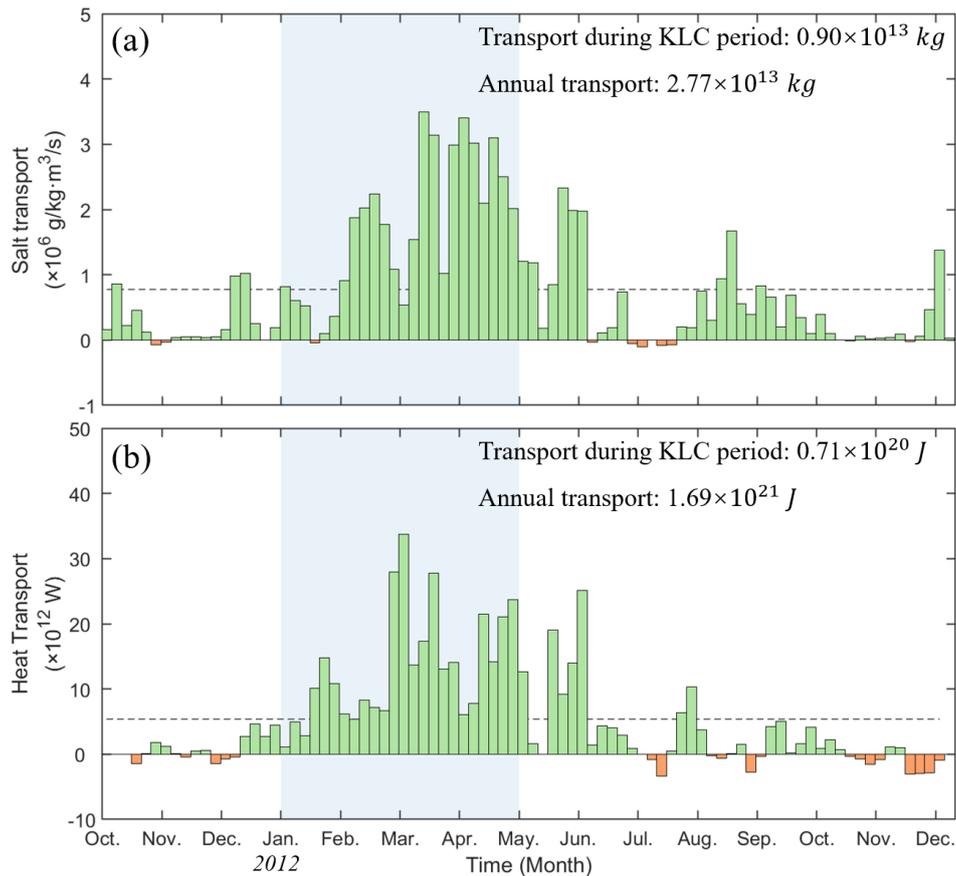
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774 **Figure 12.** (a) Vertical profiles of submesoscales-induced salt and heat transports per  
 775 unit depth (i.e., STD and HTD) westward across the KLC main axis west of 120.8 °E.

776 The results are averaged in March, 2012 when the KLC is at its mature stage. (b)

777 Same as (a) but for the  $K_S$  (blue) and  $K_\theta$  (red) averaged along the KLC main axis.

778



779

780 **Figure 13.** (a) Five-day averaged and vertically integrated submesoscale salt transport  
 781 (i.e., IST) westward across the Kuroshio main axis (i.e., the SSH contour with the  
 782 highest average salinity at 150 m) near the Luzon Strait. Positive and negative values  
 783 denote westward and eastward directions, respectively. Blue shading marks the KLC  
 784 period. The salt transports during the KLC period and throughout the year (between  
 785 October 1th, 2011 and September 30th, 2012) are marked in the upper right corner. (b)  
 786 Same as (a) but for the vertically integrated submesoscale heat transport (i.e., IHT).  
 787 Black dashed lines in (a, b) indicate the mean values throughout the 14-month data  
 788 period (i.e.,  $7.80 \times 10^5 \text{ g/kg}\cdot\text{m}^3/\text{s}$  and  $5.36 \times 10^{12} \text{ W}$ ).