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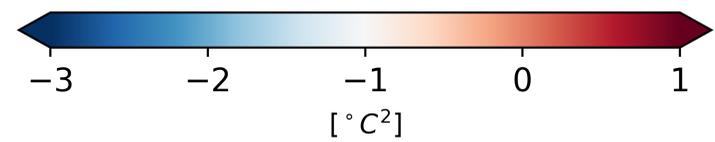
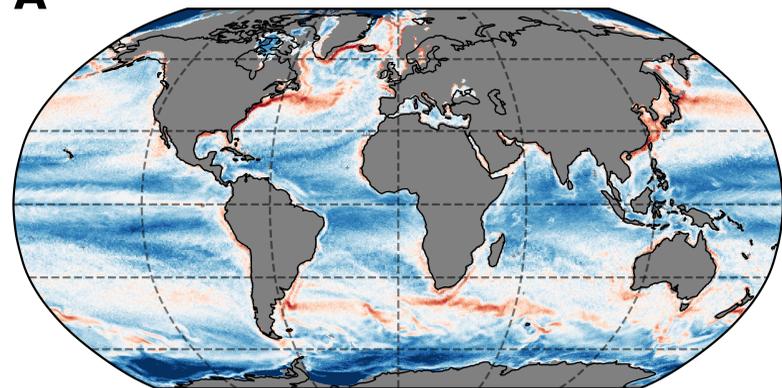
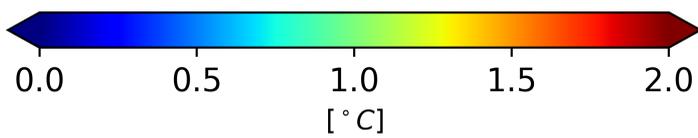
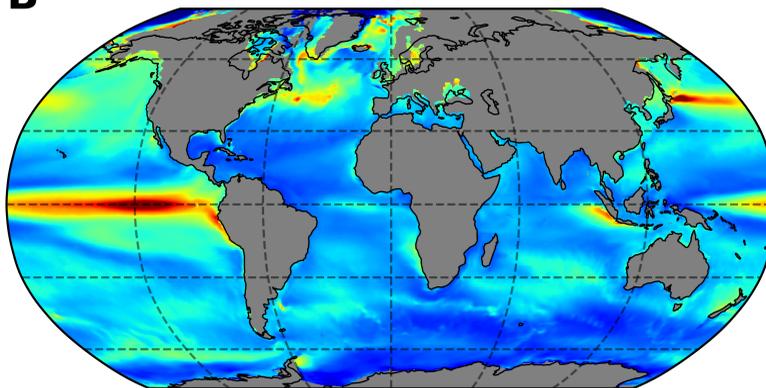
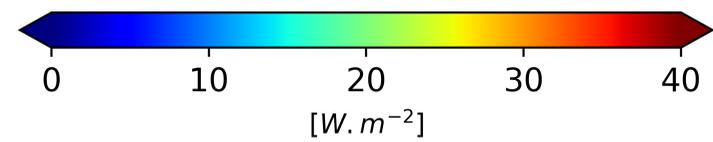
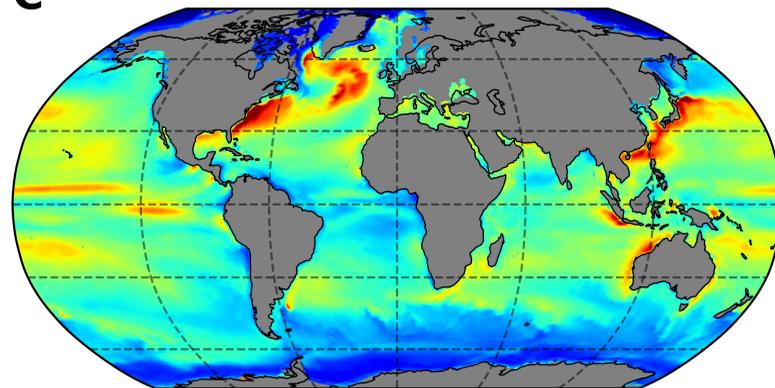
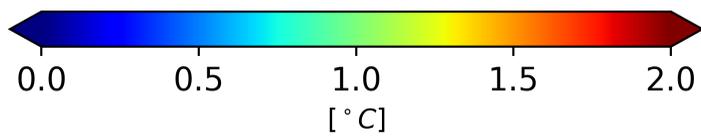
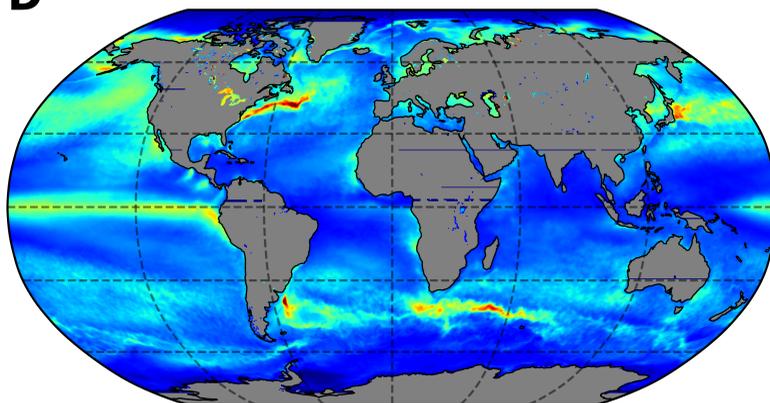
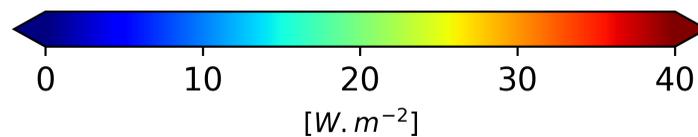
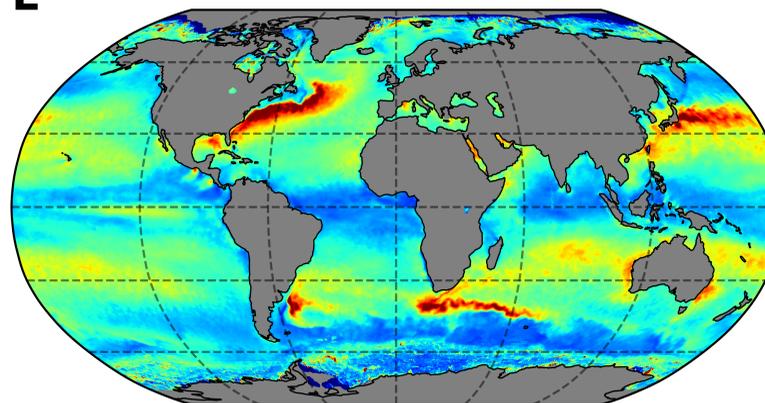
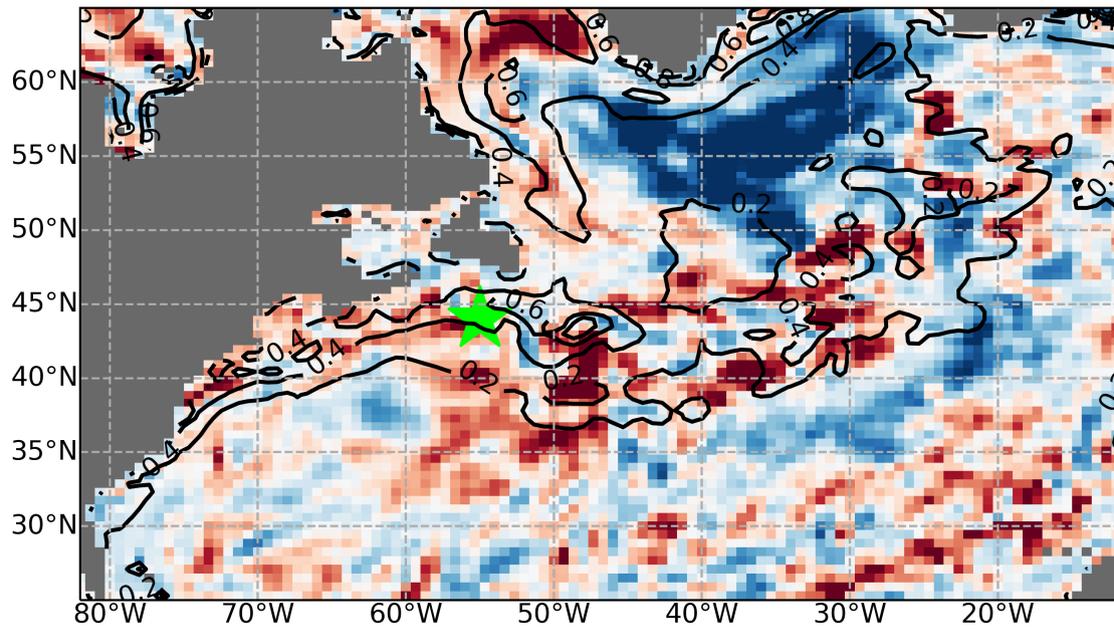
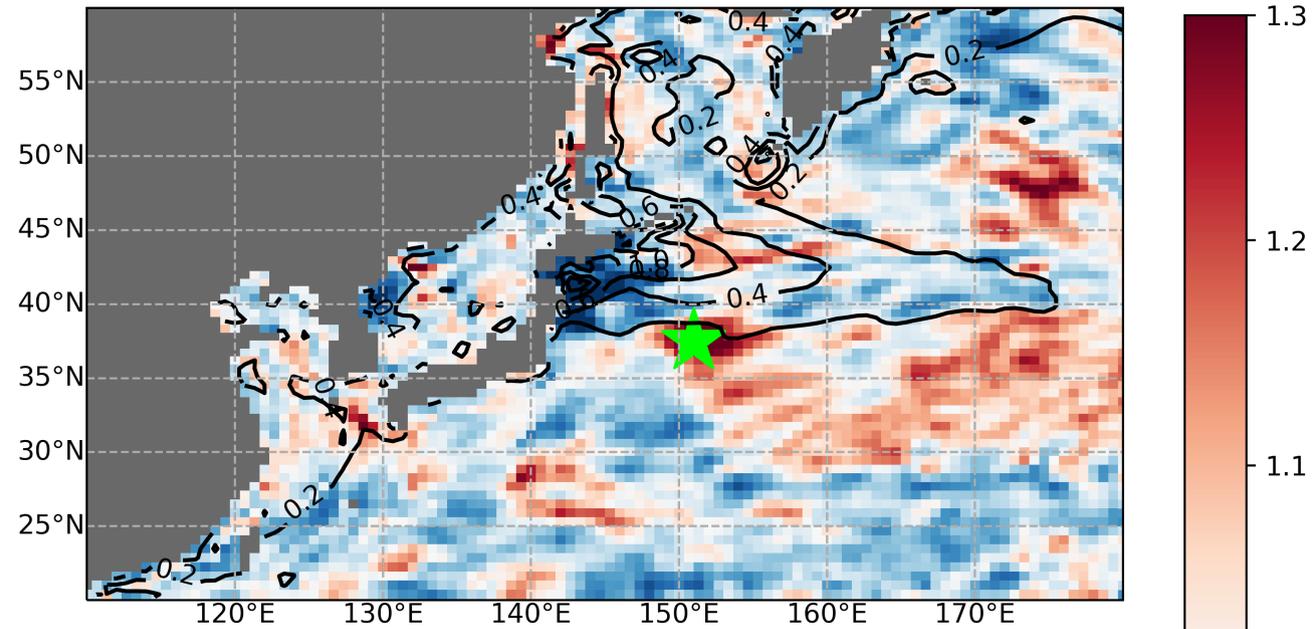
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Figure 2.

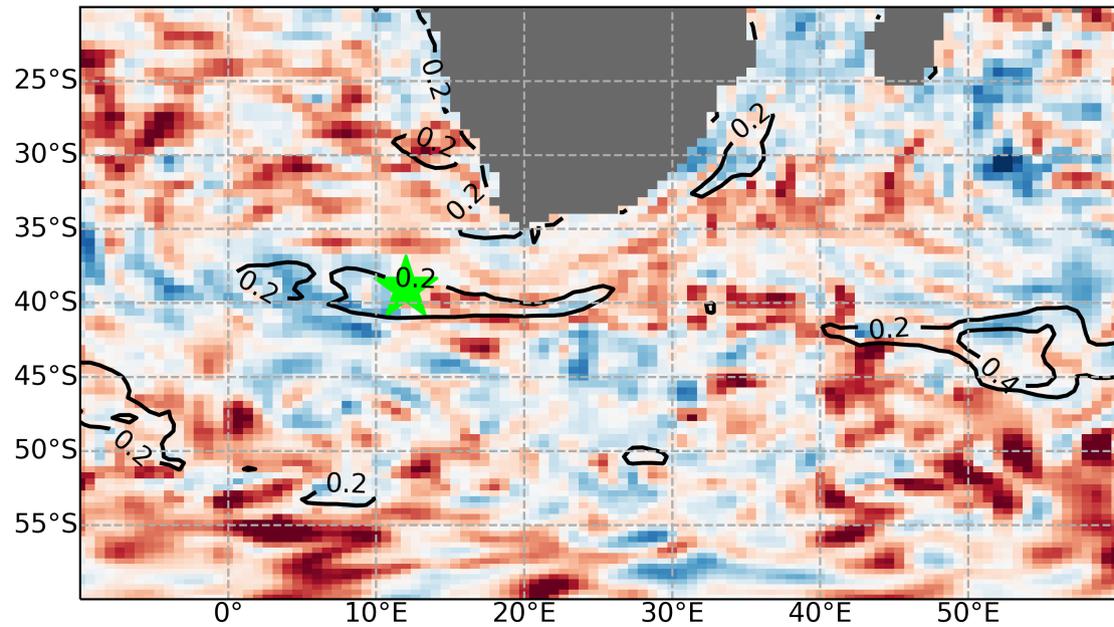
GS



Kuroshio



Agulhas



BMC

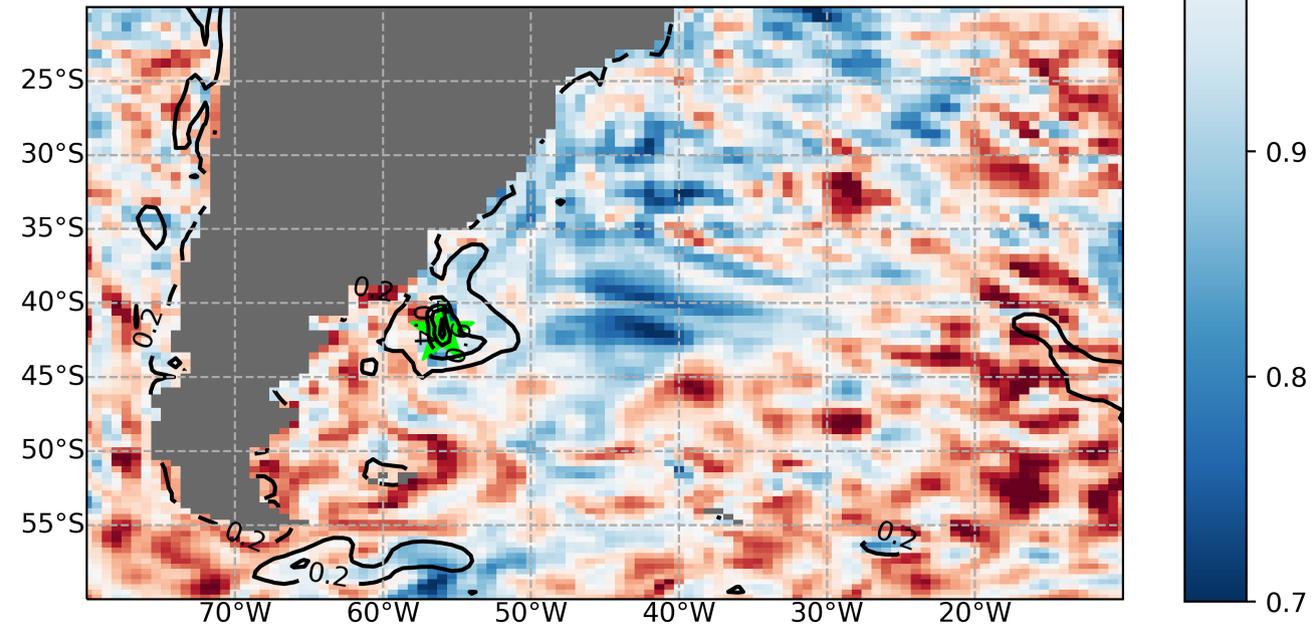
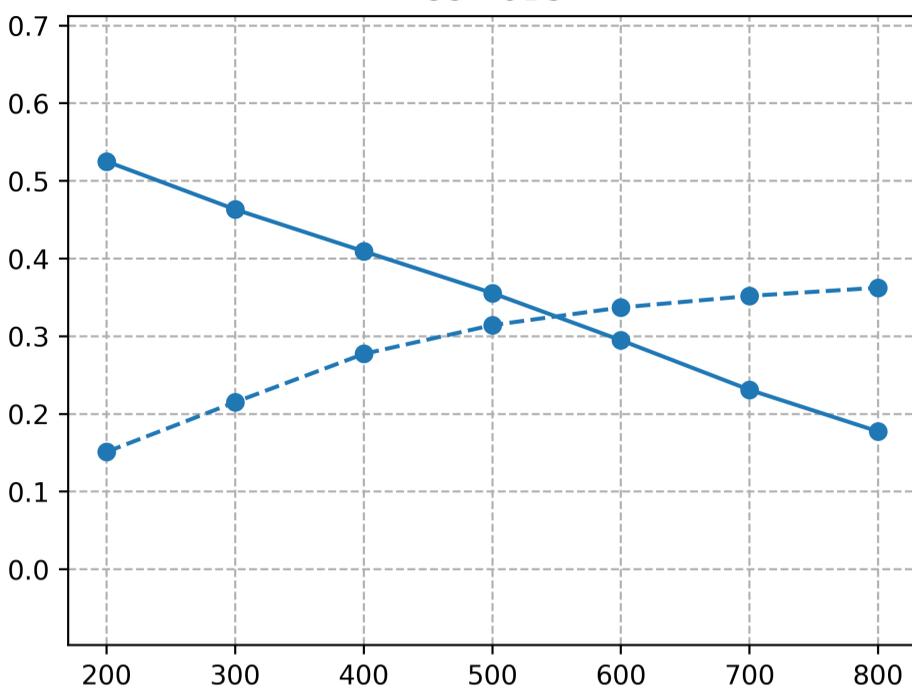
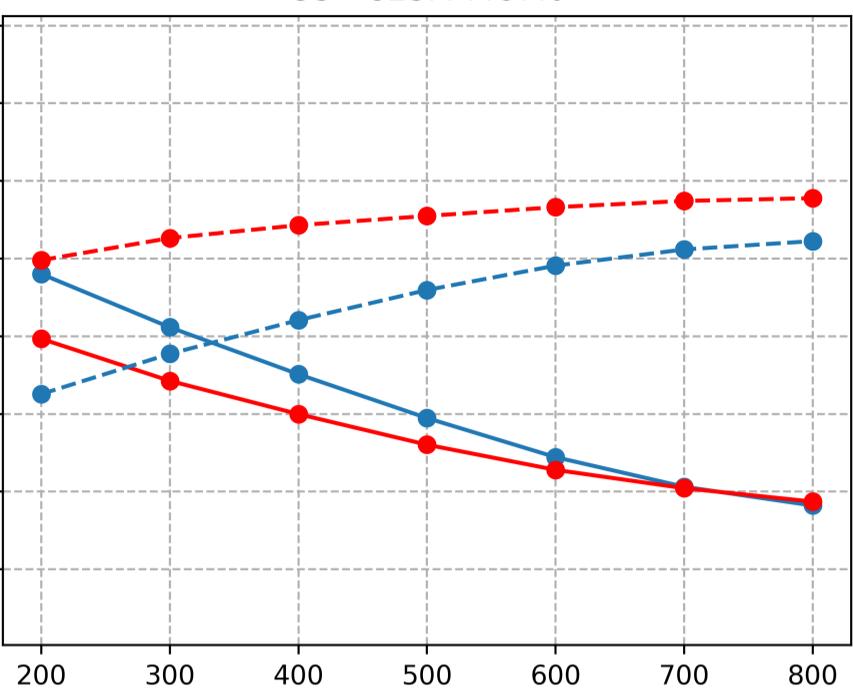


Figure 3.

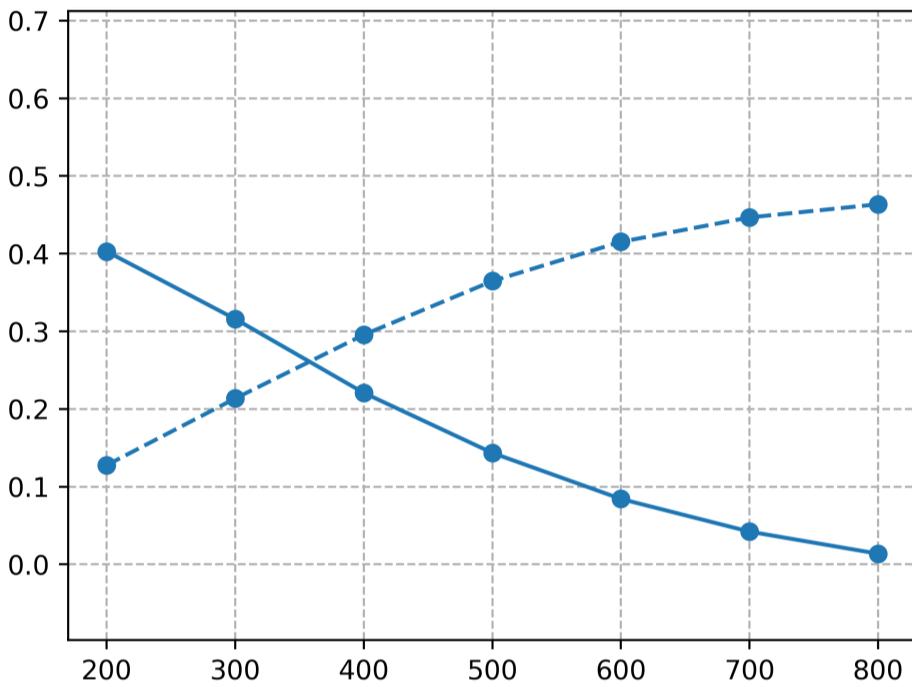
GS - OBS



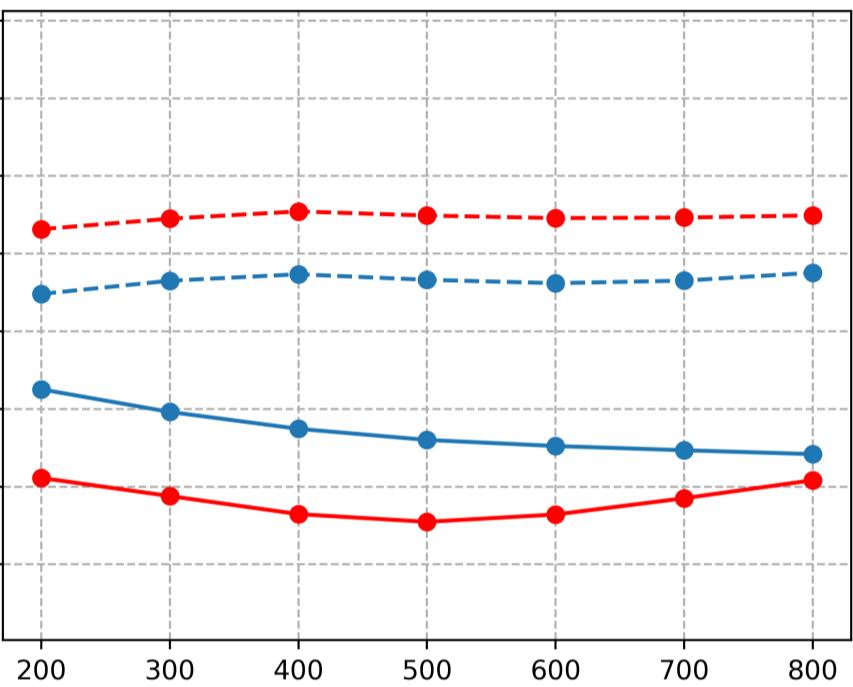
GS - CESM-MOM6



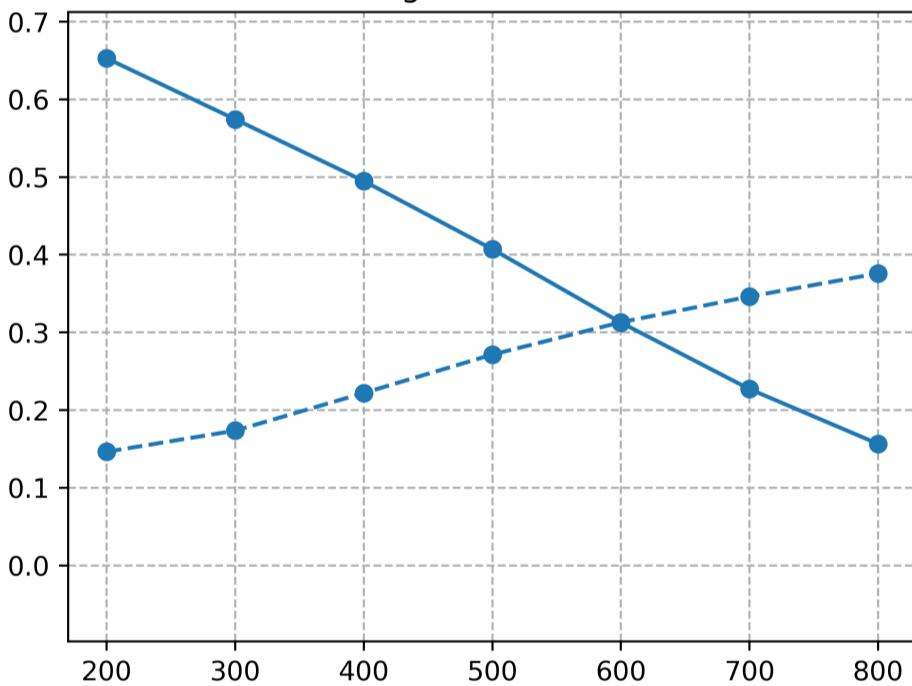
Kuroshio - OBS



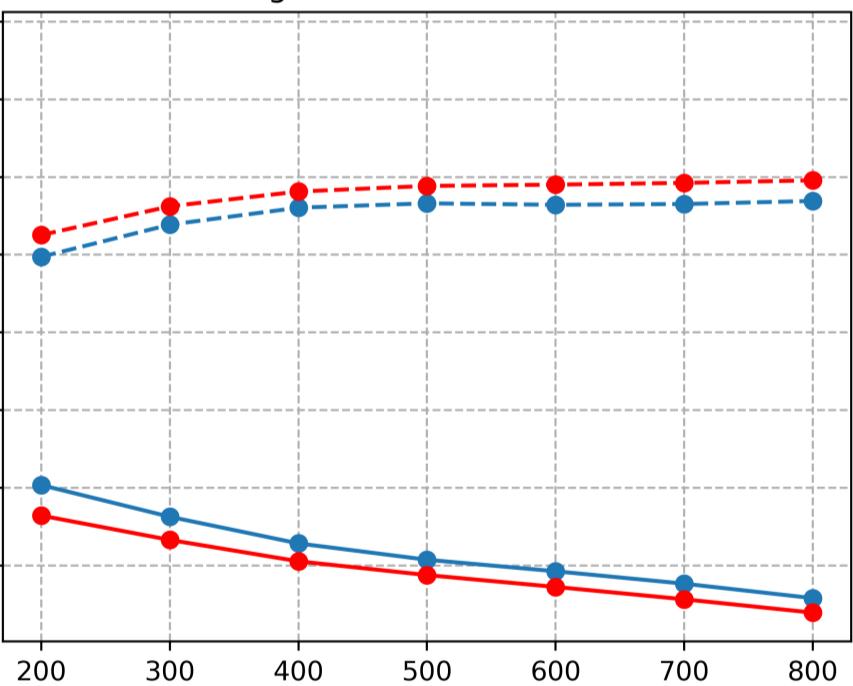
Kuroshio - CESM-MOM6



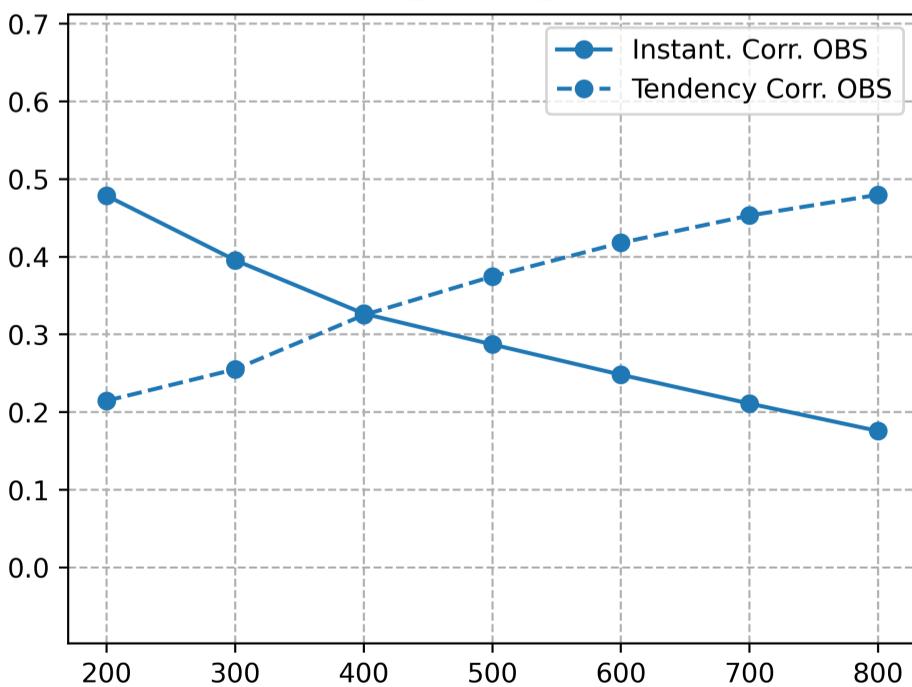
Agulhas - OBS



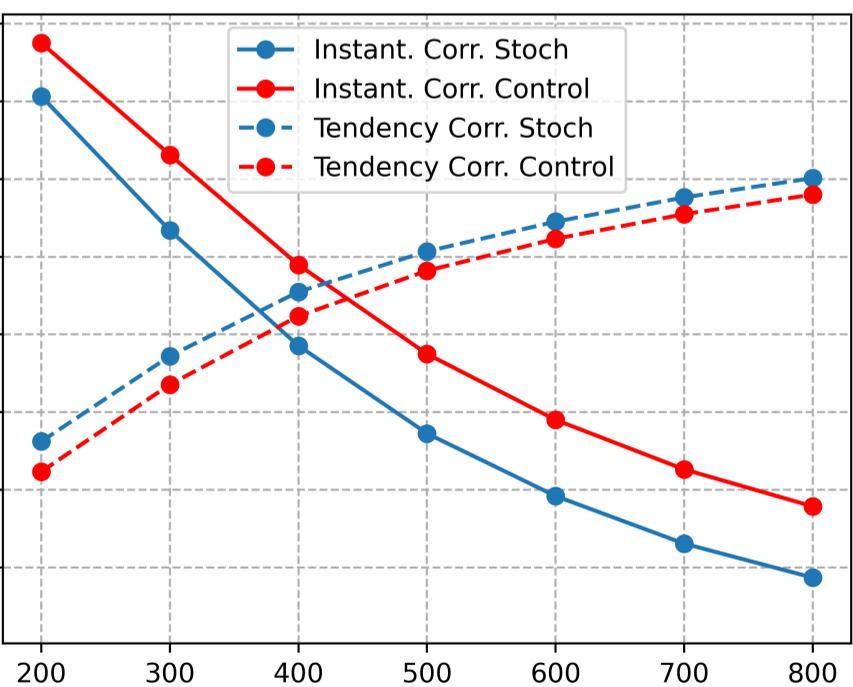
Agulhas - CESM-MOM6



BMC - OBS



BMC - CESM-MOM6



Filter size (in km)



## Abstract

Air-sea flux variability has contributions from both ocean and atmosphere at different spatio-temporal scales. Atmospheric synoptic scales and the air-sea turbulent heat flux that they drive are well represented in climate models, but ocean mesoscales and their associated variability are often not well resolved due to non-eddy-resolving spatial resolutions of current climate models. We deploy a physics-based stochastic subgrid-scale parameterization for ocean density, that reinforces the lateral density variations due to oceanic eddies, and examine its effect on air-sea heat flux variability in a comprehensive coupled climate model. The stochastic parameterization substantially modifies sea surface temperature (SST) and latent heat flux (LHF) variability and their correlations, primarily at scales near the resolution of the ocean model grid. Changes in the SST-LHF anomaly correlations indicate that the ocean-intrinsic component of the air-sea heat flux variability improves with respect to the satellite observational product, especially in western boundary current extensions.

## Plain Language Summary

Variations in air-sea heat fluxes arise from both ocean and atmosphere at different space and time scales. Studies suggest that at large scales, e.g., thousands of kilometers, atmospheric processes drive the ocean variability at the surface, such as sea-surface temperature. However, at smaller spatial scales, e.g., [100–1000] km, the oceans control the atmosphere variability near the air-sea interface. These local air-sea feedbacks influence both oceans and the atmosphere on various levels and are of significant dynamical importance. However, climate models typically use large grid spacing and fail to represent the air-sea interaction mechanism inherent to these small scales. We address this problem by modifying the ocean density using random noise at multiple places in the model before coupling it to the atmosphere. We chose density because it is used for multiple purposes in ocean models, and imperfections in it arise due to the missing subgrid-scale effects that can have a major impact all over the oceans, especially the upper ocean which interacts the most with the atmosphere. The proposed approach led to significant improvement in the air-sea interaction properties at various spatial scales compared to satellite observations.

## 1 Introduction

Air-sea coupling plays a key role in shaping the Earth’s climate and representing it correctly is essential for reducing the uncertainties in climate projections. Theoretical studies and satellite observations suggest that the mechanisms that control this coupling are largely length- and time-scale-dependent. In mid-latitudes and extratropics, synoptic-scale atmospheric weather patterns drive turbulent heat flux (THF) variability at scales larger than or equal to  $\mathcal{O}(10^3)$  km through wind speed fluctuations and air-sea temperature and humidity anomalies. The generated THF anomaly receives a lagged response from the oceans, for example; heat loss from the oceans leading to cooling of the oceans on a timescale of several weeks (Xie, 2004). In contrast, at mesoscales ( $10^1$ – $10^3$  km), persistent and vigorous intrinsic eddy variability in the oceans creates strong SST anomalies and as the wind passes over them, strong air-sea temperature and humidity differences are generated that drive the THF variability (Hausmann et al., 2017). This mechanism is well represented in idealized coupled model studies, such as Hasselmann (1976); Frankignoul and Hasselmann (1977); von Storch (2000), where the atmospheric and oceanic forcings are specified stochastically, and their dominance is tuned using the noise amplitude.

However, most global climate models employ ocean models at a non-eddy-resolving resolution, or eddy-permitting resolution at best, and therefore do not resolve the ocean mesoscale eddies (10-100 km) and the respective impact on the air-sea flux variability.

This is clearly problematic because studies have shown that the relative contributions of intrinsic oceanic and atmospheric variability in air-sea flux modulation bear enormous dynamical implications both for the oceans (Ma et al., 2016) and the atmosphere (Kuo et al., 1991; Minobe et al., 2008; Ma et al., 2017; Williams, 2012). The reader is referred to Czaja et al. (2019) for a concise review of the state of knowledge of modeled atmosphere response to mid-latitude SST and their scale dependence. The midlatitude SST fluctuations on scales close to the ocean deformation scale (i.e., 10-100 km) significantly affect the variability of lower atmosphere (reviewed in Small et al. (2008)) and the predictability of the midlatitude weather system (Dunstone et al., 2016). Contemporary studies involving ultra high-resolution of the atmosphere are starting to divulge the physical mechanisms by which such small-scale oceanic variability is communicated to the troposphere above the atmospheric boundary layer (Parfitt et al., 2016; Foussard et al., 2019). These results underscore the importance of parameterizing/resolving such eddy variability at the ocean gridscale in order to reduce the uncertainty in air-sea fluxes and their climatic impacts.

In this work, we employ a stochastic subgrid-scale (SGS) parameterization for ocean density and study its impact on air-sea THF variability in a coupled climate model. Ocean density depends on temperature  $T$ , salinity  $S$ , and pressure  $p$  through a nonlinear equation of state (EOS); SGS fluctuations in  $T$  and  $S$  cause the grid-cell-averaged density to be different from that obtained by evaluating the EOS at the grid-cell-averaged values of  $T$  and  $S$  (pressure fluctuations are sub-dominant). Brankart (2013) first proposed a parameterization for these density errors and discussed their non-trivial global impacts. An alternative parameterization, which is more accurate and more computationally efficient, was proposed by Stanley et al. (2020) and tested in an ocean-only configuration by Kenigson et al. (2022). Whereas Kenigson et al. (2022) only tested the parameterization in the computation of the buoyancy force and associated hydrostatic pressure, we use this parameterization to correct density at three places in the ocean model: the hydrostatic pressure, isopycnal slopes in the Gent-McWilliams parameterization (hereinafter, GM; Gent and McWilliams (1990)), and the mixed-layer lateral buoyancy gradient in the mixed-layer restratification parameterization of Fox-Kemper et al. (2008). In this study, we aim to explore the possibility of employing this stochastic parameterization of the mesoscale eddy effects on density to strengthen the ocean-intrinsic SST variability and its impact on air-sea THF variability.

## 2 Theory and Methods

### 2.1 SGS Density Parameterization

The ocean density correction used in this paper derives from the Taylor expansion of the nonlinear EOS (denoted as  $\hat{\rho}$ ) about the grid-cell average quantities. Following the notations used in Stanley et al. (2020), the corrected grid-cell-mean density (denoted  $\bar{\rho}$ ) is given as,

$$\bar{\rho} = \hat{\rho}(\bar{T}, \bar{S}, \bar{p}) + \frac{\partial_T^2 \hat{\rho}(\bar{T}, \bar{S}, \bar{p})}{2} \sigma_T^2, \quad (1)$$

where  $\bar{T}(x, y, z, t)$  and  $\bar{S}(x, y, z, t)$  are grid-cell-averaged temperature and salinity, respectively, and  $\sigma_T^2(x, y, z)$  is the variance of unresolved SGS temperature. The stochastic parameterization proposed by Stanley et al. (2020) for  $\sigma_T^2$  is

$$\sigma_T^2 = ce^\chi |\delta x \circ \nabla \bar{T}|^2. \quad (2)$$

Here  $\nabla \bar{T}$  is the lateral gradient of the resolved temperature field,  $\delta x$  is the horizontal grid size,  $\circ$  is the Hadamard product,  $\chi(x, y, t)$  is a depth-independent normally-distributed random noise with zero mean and variance  $\sigma_\chi^2$ , and  $c$  is a tunable parameter. Stanley et al. (2020) performed a rigorous offline diagnostic for the parameter  $c$  for different spatial resolutions of the target model and suggested  $c = 0.25$  for our model resolution.

113 However, following Kenigson et al. (2022) we increase this value to  $c = 0.5$  to account  
 114 for the weaker resolved temperature gradients in a coarse-model simulation compared  
 115 to those obtained by coarsening a high-resolution simulation. The log-normal form of  
 116 noise is chosen based on the statistical analysis of the residuals from the deterministic  
 117 form (i.e., Eq. 2 without the term  $e^\chi$ ), and the multiplicative formulation is adopted to  
 118 ensure the parameterization expression is always positive, as we are approximating vari-  
 119 ance. Furthermore,  $\chi$  is uncorrelated in space but has the following AR(1) structure in  
 120 time

$$\chi(x, y, t) = \phi(x, y, t)\chi(x, y, t - \delta t) + \epsilon(x, y, t), \quad (3)$$

121 where  $\epsilon(x, y, t)$  is a zero-mean Gaussian random noise with no correlations in space and  
 122 time. The variance of  $\epsilon$  varies with the AR(1) parameter  $\phi(x, y, t)$  such that the process  
 123 variance  $\sigma_\chi^2$  remains constant; Stanley et al. (2020) found  $\sigma_\chi^2 = 0.39$ . Next,  $\phi(x, y, t)$   
 124 is expressed using the decorrelation time scale ( $\tau$ ) of the local kinetic energy as

$$\phi(x, y, t) = e^{-\frac{\delta t}{\tau(x, y, t)}}, \quad (4)$$

125 where  $\delta t$  is the model baroclinic time step and  $\tau$  is equal to

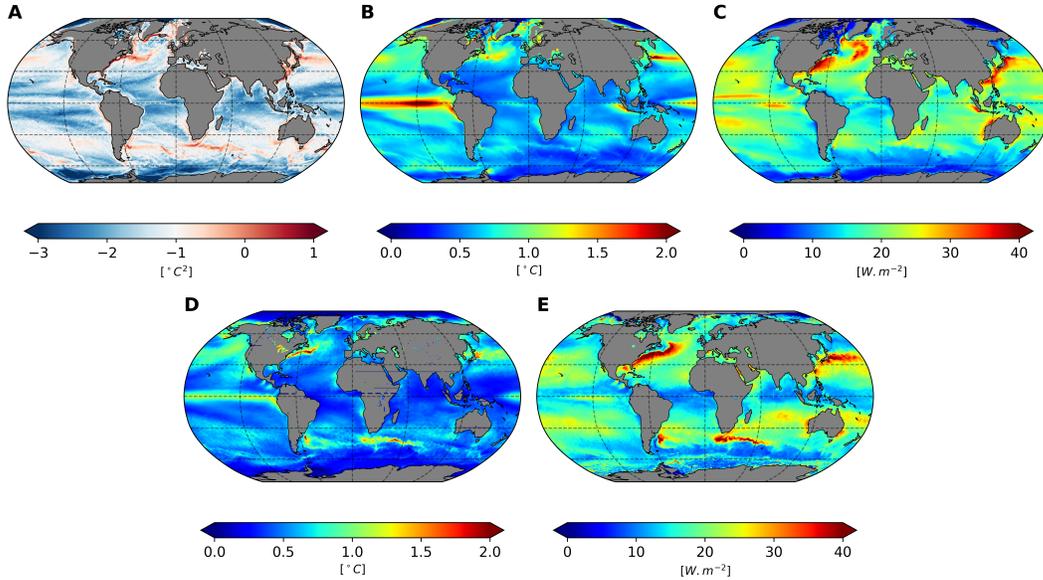
$$\tau(x, y, t) = k\sqrt{\frac{\delta x^2 + \delta y^2}{u^2 + v^2}}. \quad (5)$$

126 Here  $u(x, y, t)$  and  $v(x, y, t)$  are the upper-ocean instantaneous velocities, and  $k = 3.7$   
 127 is a tunable parameter whose value was estimated by Stanley et al. (2020). The decor-  
 128 relation timescale  $\tau$  essentially depends on the resolved fields, and the offline diagnos-  
 129 tics have shown that it varies between a few days to several months for  $2/3^\circ$  resolution  
 130 ocean model. The global map of the parameterized SGS temperature variance for a  $2/3^\circ$   
 131 resolution MOM6 simulations stored as monthly mean is shown in Figure 1a. It is easy  
 132 to note that the variance is significantly higher in mid-latitude western boundary cur-  
 133 rent (WBC) regions compared to the tropics (note the logarithmic scaling). This is due  
 134 to the enormous lateral temperature gradients and strong mesoscale eddy variability present  
 135 in those regions.

## 136 2.2 Model and Observations

137 We tested the above parameterization in the Modular Ocean Model, version 6, (MOM6)  
 138 ocean general circulation model which solves the hydrostatic primitive equations on a  
 139 tripolar grid with C-grid horizontal stencil. It uses an Arbitrary Lagrangian-Eulerian ver-  
 140 tical coordinate method (Adcroft et al., 2019; Griffies et al., 2020) and the energetically  
 141 consistent mesoscale backscatter proposed by Jansen et al. (2019) involving mesoscale eddy  
 142 kinetic energy budget and GM parameterization. MOM6 is coupled to Los-Almos Sea  
 143 Ice Model, version 5, (CICE5; Hunke et al. (2010)) in the Community Earth System Mod-  
 144 eling Version 2.3, (CESM2) framework. The model uses the GEOMETRIC parameter-  
 145 ization (Marshall et al., 2012) to set the GM coefficient  $\kappa$ . Explicit diapycnal mixing in  
 146 the oceans due to convection and static instabilities is not permitted due to the hydro-  
 147 static approximation, but is parameterized using the K-profile parameterization (KPP)  
 148 proposed in Large et al. (1994); restratification of the mixed layer is handled using the  
 149 FFH parameterization (Fox-Kemper et al., 2008). The Wright EOS (Wright, 1997) is  
 150 used to compute density as a function of pressure, temperature, and salinity.

151 We configured CESM-MOM6 as a fully coupled global ocean-atmosphere-sea ice  
 152 model with  $2/3^\circ$  nominal spatial resolution for the ocean and sea-ice model and a coarser  
 153  $0.95^\circ \times 1.25^\circ$  resolution for the atmosphere and the land component. The ocean model  
 154 uses 65 vertical levels in  $z^*$  coordinates (Adcroft & Campin, 2004) with finer vertical res-  
 155 olution around the ocean surface (2.5m) and coarser towards the bottom ( $\approx 250$ m) and  
 156 integrated using a baroclinic time step of 1800 seconds. The atmosphere is represented  
 157 using the finite-volume based Community Atmospheric Model Version 6 (CAM6; Danabasoglu  
 158 et al. (2020)) where the atmospheric primitive equations are discretized on 70 vertical



**Figure 1.** Illustration of the characteristics of the SGS density parameterization, model, and observations: (a) Spatial pattern of the parameterized SGS SST variance using (2); (b)-(c) Standard deviation of monthly anomalies of SST and LHF, respectively, from CESM-MOM6 Stoch simulation; (d)-(e) Same as (b)-(c) but for the J-OFURO3 observations for the period 2000-2015. The monthly anomalies were computed by removing the monthly climatology and the linear trend. In (a), the variance is scaled using  $\log_{10}$ , and the color bar denotes the exponent of 10.

159 levels and integrated using a time step of 300 seconds. The atmosphere, sea-ice, and land  
 160 communicate their fluxes and state information every 30 mins via the CESM coupler bun-  
 161 dled with the Earth System Modeling Framework (ESMF) distribution. The air-sea fluxes  
 162 are computed within the coupler and are passed to the atmospheric model every 30 mins  
 163 and to the ocean model every hour. The model was run for a total of 100 years under  
 164 the pre-industrial greenhouse gas conditions with and without the stochastic SGS den-  
 165 sity parameterization, referred to here as Stoch and Control, respectively. In this study,  
 166 we have analyzed monthly means from the last 35 years of both experiments. We used  
 167 monthly-mean products because mesoscale ocean eddy variability is strongest on monthly  
 168 to annual time scales, and the employed eddy parameterization can be expected to pro-  
 169 duce notable impacts on these frequencies.

170 The benchmarking observational products of SST and surface heat fluxes used in  
 171 this paper are taken from a remote-sensing-based third-generation Japanese ocean flux  
 172 dataset, abbreviated J-OFURO3 (Tomita et al. (2019); hereinafter, also referred to as  
 173 OBS). It provides datasets for surface heat, momentum, freshwater fluxes, and the as-  
 174 sociated physical parameters over the ice-free global oceans from 1986-2017 in daily and  
 175 monthly-mean temporal resolutions with 0.25 degrees spatial resolution; we used the monthly  
 176 mean products. J-OFURO project computes the turbulent surface fluxes using a bulk  
 177 method where all physical parameters are satellite-derived except the 2m air tempera-  
 178 ture, which is obtained from the NCEP-DOE reanalysis product. The latest version, i.e.  
 179 J-OFURO3, is a significant advancement over its predecessors as it uses state-of-the-art  
 180 algorithms to estimate near-surface specific humidity and employs advanced techniques  
 181 to combine multi-satellite sensor outputs. In addition, rigorous and systematic valida-  
 182 tions against the in-situ observations and other datasets ensure more accuracy for J-OFURO3.

183 The OBS version 1.1 monthly-mean products are available from 1988-2017, but we only  
 184 used the years 2000-2015 in this paper to avoid data gaps.

185 For a basic illustration of the OBS and model outputs, standard deviations of the  
 186 monthly anomalies of SST and LHF from the Stoch simulation and OBS are shown in  
 187 Figure 1(b-e). While the spatial patterns of the SST and LHF variability are similar for  
 188 both OBS and Stoch, the magnitude of the variability differs across them. This is es-  
 189 pecially true near the ocean jets and currents, such as Gulf Stream (GS), Kuroshio, Oy-  
 190 ashio, Agulhas, and Brazil-Malvinas confluence, which are the areas of focus in this study.  
 191 These major jets and currents generally show a stronger SST/LHF variability in OBS  
 192 than in the CESM-MOM6 simulation. Kuroshio is an exception to this, as the Stoch sim-  
 193 ulation possesses stronger and more eastward extended sub-monthly SST variability in  
 194 this region (compare Figure 1b and d). This is a known bias related to the convergence  
 195 of the mean kinetic energy and the largest SST gradient regions (Thompson & Kwon,  
 196 2010). Additionally, Stoch possesses significantly high LHF variability around the Labrador  
 197 and Irminger seas region, which is perhaps related to a known long-term bias in this re-  
 198 gion. Nevertheless, the generally reduced variance around the jets in model simulations  
 199 is expected due to their coarse spatial resolution, which does not permit mesoscale ed-  
 200 dies and their large-scale feedback and the difference in the lengths of model simulation  
 201 and OBS products.

### 202 **2.3 Analysis Methods**

203 In this paper, we consider the latent heat flux (LHF) and SST for all our analy-  
 204 ses. We only focus on the LHF component of the net surface heat flux because several  
 205 previous studies have shown that latent heat dominates the net surface heat flux response  
 206 to the SST; the contributions from the sensible and radiative heat fluxes are sub-dominant  
 207 (Frankignoul & Kestenare, 2002; Park et al., 2005; Hausmann et al., 2017). In CESM  
 208 simulations, LHF is computed using a bulk flux formula – proportional to the air den-  
 209 sity, wind speed, and difference in the specific humidity saturated at the ocean surface  
 210 (strongly dependent on SST) and of the air. The invoked parameterization influences  
 211 LHF through the resolved variables for the oceans and the atmosphere used in the bulk  
 212 formula.

213 In this paper, we focus only on local air-sea interactions and study the changes pro-  
 214 duced therein by the stochastic SGS density parameterization. As discussed in Section  
 215 1, at ocean mesoscales, the LHF variability is driven by intrinsic SST variability, led by  
 216 the mesoscale eddies. We call this SST variability intrinsic because it is not forced by  
 217 air-sea heat flux anomalies unlike in the case of slow SST variations over large spatial  
 218 scales. As a result of ocean-driven LHF variability, large outgoing heat flux is noticed  
 219 over warm SST anomalies, and less heat flux is seen departing over the colder SST anoma-  
 220 lies (Small et al., 2008, 2019). This suggests a positive instantaneous correlation between  
 221 SST and LHF, where the sign convention is that the outgoing heat flux from the oceans  
 222 is considered positive and incoming is negative. In contrast, at large scales (e.g., ocean  
 223 basin size), the air is more in equilibrium with the slow-varying SST beneath it and leads  
 224 to situations where significant outgoing heat flux from the oceans, driven by atmospheric  
 225 forcing, is seen to cool the oceans. This refers to lagged SST (or, ocean) response to air-  
 226 sea heat flux variations, i.e., small instantaneous SST-LHF correlation but large  $\partial(\text{SST})/\partial t$ -  
 227 LHF correlation (Wu et al., 2006; Bishop et al., 2017; Small et al., 2019). Throughout  
 228 this paper, we will use the term ‘instantaneous correlation’ to refer to the simultaneous  
 229 SST-LHF correlation and ‘tendency correlation’ to refer to the  $\partial(\text{SST})/\partial t$ -LHF corre-  
 230 lations. We use these two types of correlations to infer the dominant forcing in the ocean-  
 231 atmosphere feedback mechanism, i.e., (1) if the instantaneous correlation is large, it sug-  
 232 gests ocean (precisely, SST) forcing the atmosphere (or, latent heat flux variability), whereas  
 233 (2) if  $\partial(\text{SST})/\partial t$ -LHF is large, it means the atmosphere driving the oceans. While (1)  
 234 is believed to hold true at small scales, (2) is supposed to be the case at large scales. Be-

235 cause the SGS density parameterization corrects the ocean density on ocean mesoscales,  
 236 it is expected to have a more significant impact on instantaneous correlations than ten-  
 237 dency correlations, as synoptic-scale atmospheric processes are already well resolved in  
 238 climate models. It bears noting that the  $2/3^\circ$  ocean model resolution does not resolve  
 239 the mesoscale, so the direct impact of ocean mesoscales on LHF variability must be ab-  
 240 sent from the model. But ocean mesoscales induce ocean-intrinsic variability at larger  
 241 scales that are resolved, a process that is represented in part using the stochastic param-  
 242 eterization.

243 Because we intend to study the scale dependence of local correlations, we use a spa-  
 244 tial filter on the original fields to separate the eddying part from their large-scale coun-  
 245 terpart. We use a fast, efficient python package named GCM-Filters (Loose et al., 2022),  
 246 which achieves filtering using an iterative application of a discrete Laplacian, resembling  
 247 diffusion (Grooms et al., 2021). We use the Taper filter shape described by Grooms et  
 248 al. (2021), which makes a sharper separation between large and small scales than Gaus-  
 249 sian or boxcar filters. We used filtering length scales from 200 km up to 800 km with a  
 250 spacing of 100 km. Although the term ‘eddy’ is frequently used to describe the small-  
 251 scale part of a field produced by a high-pass spatial filter, we use the term sub-filter scale  
 252 (SFS) to avoid confusion, since our model does not resolve mesoscale eddies. A monthly  
 253 climatology (for both SST and LHF) is then computed and subtracted from the monthly-  
 254 mean values to provide the monthly anomalies, followed by the removal of linear trend.

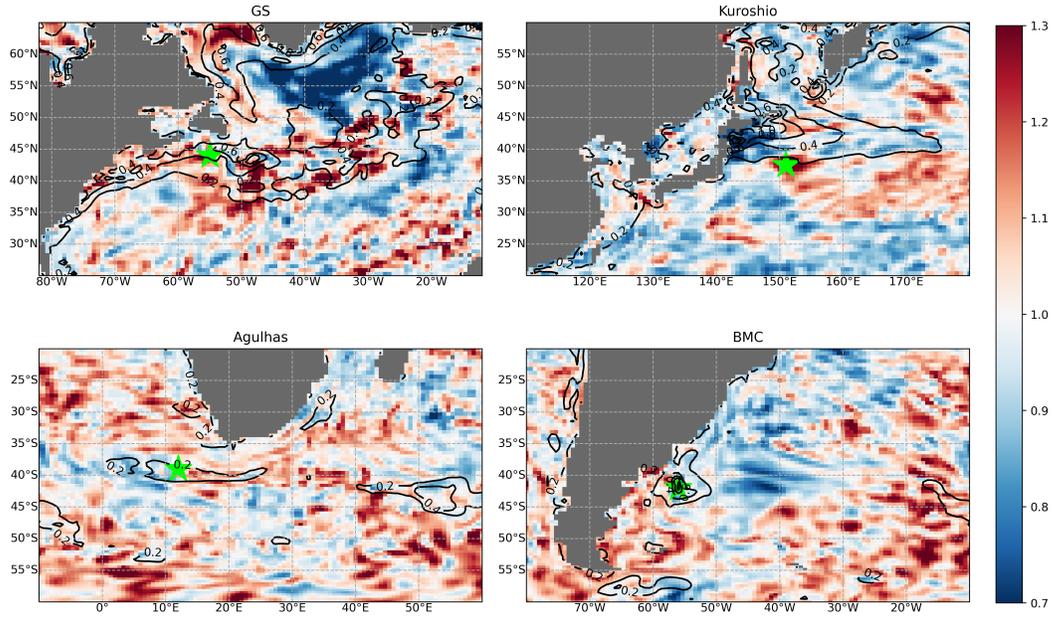
### 255 3 Results

256 In this section, we diagnose the impact of the SGS stochastic density corrections  
 257 on the variability and co-variability of SST and LHF and pinpoint the gains/losses by  
 258 comparing against the J-OFURO3 observational outputs. We also make efforts to ex-  
 259 plain the identified parameterization impacts from a physical perspective. Furthermore,  
 260 because the parameterization is mostly active near the regions of strong temperature fronts  
 261 (see Figure 1a), from here onward we only focus on four regions: the GS and Kuroshio  
 262 in the northern hemisphere, and the Agulhas and Brazil-Malvinas Confluence (BMC)  
 263 in the southern hemisphere.

#### 264 3.1 Sub Filter Scale Variability

265 To elucidate the modifications produced by the SGS density parameterization across  
 266 scales, maps of the ratio of the standard deviations of the SFS SST from Stoch and Con-  
 267 trol runs are shown in Figure 2. Here, the SFS fields are obtained using a filter size of  
 268 500 km. It is evident that the density corrections produced by the parameterization sig-  
 269 nificantly affect the SFS SST variability – as much as 30% shift in their standard devi-  
 270 ation – in all four regions. While Agulhas is predominantly characterized by a net in-  
 271 crease in their SFS variability, GS, Kuroshio, and BMC display a mixed response, i.e.,  
 272 both increase (red) and decrease (blue). An increase/decrease in variability in the form  
 273 of a red/blue dipole suggests that the parameterization is making dynamical adjustments  
 274 by changing the positions of the mean currents (cf. Kenigson et al., 2022).

275 In case of the GS, an increase in SFS variability is clear in the eastward extension  
 276 portion of the jet between  $35^\circ$ – $45^\circ$  N and  $30^\circ$ – $60^\circ$  W. This is a prominent feature of  
 277 the parameterization, as several previous idealized studies have shown that mesoscale  
 278 eddying features are paramount to producing eastward extension of jets (Shevchenko &  
 279 Berloff, 2015; Agarwal et al., 2021). However, either minimal increase or a decrease in  
 280 the variability is seen around the far-east extension of the jet. It is also intriguing to spot  
 281 a region of significantly reduced SFS SST variability in the Irminger Sea and partly in  
 282 the Labrador Sea between  $50^\circ$ – $60^\circ$  N and  $30^\circ$ – $50^\circ$  W. This is related to an increase in  
 283 mixed-layer depth in this region (not shown), which increases the heat capacity of the  
 284 mixed-layer column and, therefore, a decrease in the variation of the surface tempera-



**Figure 2.** Manifestation of the influence of the stochastic parameterization on variability across different scales. Ratio of the standard deviation of SFS SST from Stoch and Control simulations in four most eminent frontal regions: GS, Kuroshio, Agulhas, and BMC. The filter size used here is 500 km. The ratio is taken as Stoch over Control, so the red/blue indicates an increase/decrease in the SFS SST variability due to the induced parameterization. The contour lines belong to the standard deviations of the SFS SST from the Control experiment. The stars denote the locations picked for the analysis in section 3.2 (in BMC, the star is at 42°S, 56°W). The color scale is in dimensionless units.

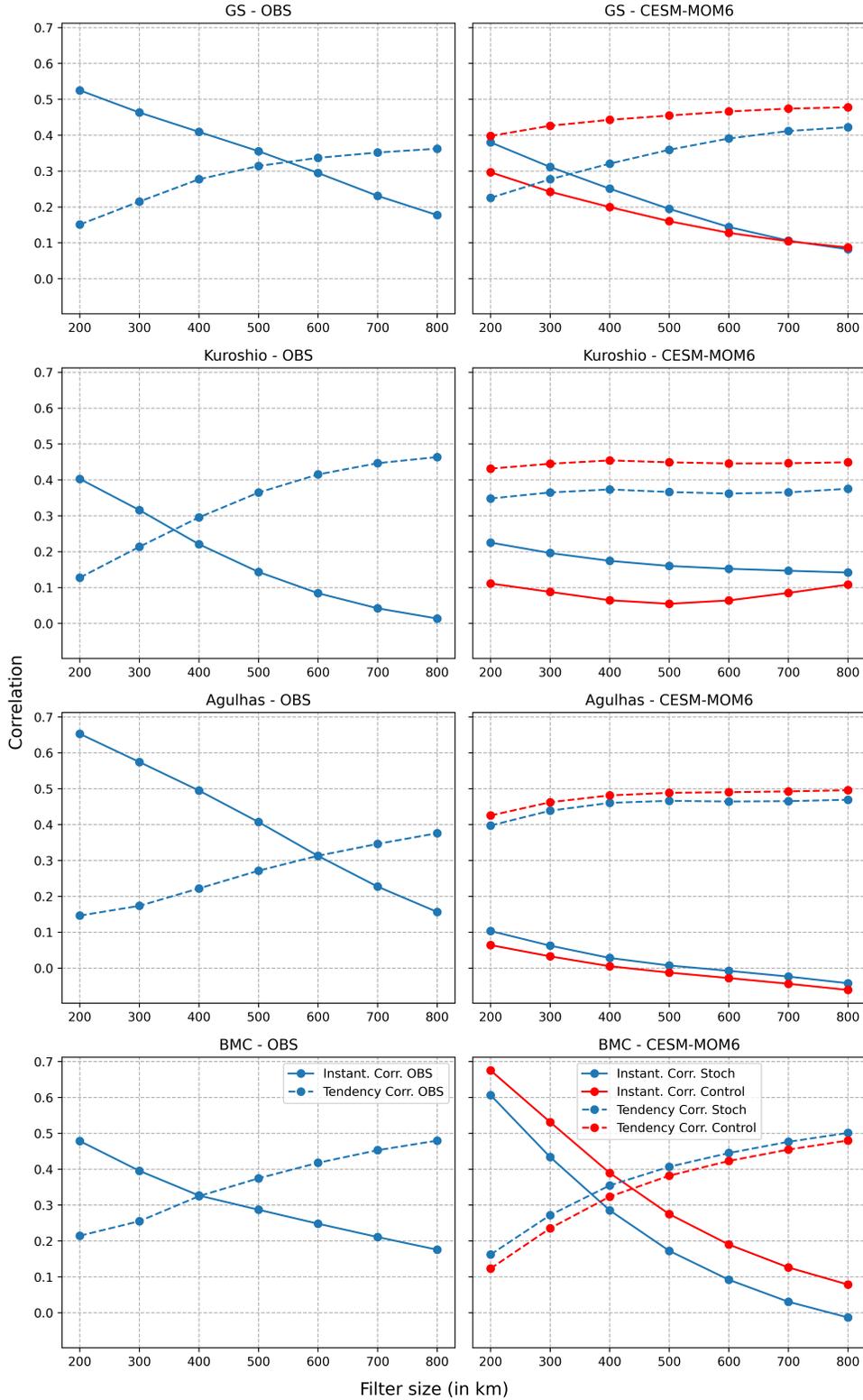
285 ture (more heat is now required to change the surface temperature by  $1^{\circ}\text{C}$ ). The Kuroshio  
 286 extension mostly witnesses a decrease in the SFS SST variability, especially around the  
 287 continental boundaries. A clear dipole is visible around the separation location, which  
 288 hints at shift in the course of the jet. The physical correctness of this shift is discussed  
 289 in section 3.2 using a more local analysis. The Agulhas return current is an eddy-rich  
 290 region, and we see an increase in the SFS SST variability in a large swath of this region.  
 291 The same is also true for the South Atlantic current, where a large number of locations  
 292 possess 10 – 30% increase in the SST variability. However, a region of decreased SST  
 293 variability is seen around the Brazil-Malvinas confluence between  $30^{\circ}$ – $60^{\circ}\text{W}$  and  $35^{\circ}$ –  
 294  $45^{\circ}\text{S}$ . The exact reason for this dip is not known, but may be related to the seasonal south-  
 295 ward shift of the South Atlantic Current that Kenigson et al. (2022) found when analy-  
 296 zing the effects of this parameterization in a forced-ocean simulation. We also analyzed  
 297 the ratio of the standard deviations of SFS LHF but found them qualitatively similar  
 298 and they are therefore not discussed here.

### 299 3.2 Correlations

300 Here we discuss the instantaneous and tendency correlations (as described in sec-  
 301 tion 2.3) for the low-pass fields obtained using spatial filtering with filter sizes between  
 302 200–800 km. We compute the correlations for both Control and Stoch simulations and  
 303 compare them against OBS. We aim to establish physical significance of the parameter-  
 304 ized density perturbations by studying their influence on large-scale patterns’ correla-  
 305 tions and the associated transition length scale at which the THF variability changes from  
 306 ocean-driven to atmospheric-driven. The transition length scale is computed as the fil-  
 307 ter width cutoff at which the instantaneous and tendency correlation magnitudes inter-  
 308 sect (Bishop et al., 2017). The correlation relationships discussed here are local in na-  
 309 ture and belong to the locations marked by a star in Figure 2 in each of the four frontal  
 310 regions. These locations have two important properties: (i) they possess high SFS SST  
 311 variability (cf. the SFS SST standard deviation contours in Figure 2), and (ii) the pa-  
 312 rameterization made a significant change in SFS variability at these locations, e.g., here  
 313 all locations exhibit more than 15% change in their SFS SST standard deviation.

314 The GS, Kuroshio, and Agulhas locations show higher instantaneous correlations  
 315 for Stoch than Control for all filter lengths (Fig. 3, right column); the opposite is true  
 316 for the tendency correlations. Physically this means that the parameterization is boost-  
 317 ing the ocean-intrinsic THF variability and diminishing the fraction of THF that is atmospheric-  
 318 forced across all scales at these locations. The augmentation of ocean-forced THF vari-  
 319 ability by the parameterization is consistent with OBS (Fig. 3, left column), as the Con-  
 320 trol instantaneous correlations are much smaller than OBS for nearly all filter sizes at  
 321 these mesoscale-eddy-rich locations. Only in Kuroshio, Stoch THF variability goes too  
 322 strongly ocean-forced compared to OBS beyond 500 km filter width. Modifications in  
 323 the correlations by the stochastic parameterization are most pronounced near the small-  
 324 est filter size (200 km), where the Control instantaneous correlations are too low and the  
 325 tendency correlations are too high compared to OBS – especially for the GS and Kuroshio  
 326 locations. However, despite the reinforcement, the Stoch instantaneous correlations are  
 327 generally lower than the corresponding OBS values. A perfect match between Stoch and  
 328 OBS is nevertheless not expected because the stochastic parameterization used here only  
 329 accounts for one process (density variations), whereby ocean mesoscales induce variabil-  
 330 ity at larger scales.

331 The results for the BMC location are different from the other three locations, as  
 332 it experiences a decrease in the instantaneous correlation and an increase in the tendency  
 333 correlations across all filter sizes when subjected to the parameterization. The reason  
 334 behind this is the seasonal southward shift in the Brazil current, and, therefore, the BMC  
 335 location, as a response to the intense parameterized density correction in this region (Kenigson  
 336 et al., 2022). Owing to this shift, the THF variability at the BMC location is more atmospheric-



**Figure 3.** Comparison of local correlations around major WBCs and their scale dependence. Solid lines denote the instantaneous correlations and tendency correlations are depicted in dotted lines. The left column belongs to OBS and the right one corresponds to CESM-MOM6 results. In the right panels, blue/red curves belong to Stoch/Control runs. The rows correspond to the chosen locations marked by stars in Figure 2. The filter length around which the instantaneous and tendency correlation curves intersect is the transition length scale.

337 driven in the Stoch outputs. This is consistent with OBS for 200–300 km filter sizes;  
 338 outside this filter limit, Stoch’s instantaneous correlations are much smaller than OBS’s.  
 339 Little difference exists between Stoch and Control tendency correlations in this region,  
 340 and both are close to the OBS magnitudes for all filter sizes.

341 Finally, we analyze the transition length scale, i.e., the length scale at which LHF  
 342 variability switches from ocean-driven to atmospheric-driven. The induced stochastic pa-  
 343 rameterization revises the transition lengths at all chosen locations and pushes them closer  
 344 to the reference truth – the OBS values. This is clearer in the GS case, where the ad-  
 345 dition of the stochastic parameterization increases the transition scale from  $\approx 70$  km  
 346 (not shown) to  $\approx 350$  km, which is closer to but still below the OBS value of  $\approx 550$  km.  
 347 At the BMC location, Stoch offers a smaller transition scale ( $\approx 380$  km) than Control  
 348 ( $\approx 440$  km), yet slightly closer to the OBS value ( $\approx 400$  km). At the Kuroshio and Ag-  
 349 ulhas locations, the Control and Stoch THF outputs are atmospherically driven at the  
 350 grid scale, and, therefore, the transition length scale is not defined. However, Stoch is  
 351 less atmospheric-dominated and more ocean-dominated than Control, implying a big-  
 352 ger transition length scale than Control.

## 353 4 Conclusions and Discussion

354 We implemented a physics-based stochastic subgrid-scale (SGS) parameterization  
 355 for ocean density in a CESM-MOM6 coupled climate model and studied its impact on  
 356 air-sea turbulent heat flux (THF) variability, primarily latent heat flux (LHF). Past stud-  
 357 ies have shown that the air-sea flux variability is driven by oceanic-intrinsic variability  
 358 at ocean mesoscales and by synoptic-scale atmospheric processes at larger scales, e.g.,  
 359  $\mathcal{O}(1000)$  km. But, due to the spatial resolution of non-eddy ocean climate models,  
 360 the air-sea flux variability due to intrinsic oceanic turbulence is not well represented. Here,  
 361 we show that a SGS density parameterization successfully restores a significant portion  
 362 of the missing ocean-intrinsic air-sea THF variability across turbulent, eddy-rich regions,  
 363 such as western boundary currents and the adjacent re-circulation zones. This study is  
 364 the first in its kind which shows the revival of intrinsic ocean-driven THF variability in  
 365 a comprehensive coupled climate model using a systematic physics-based SGS param-  
 366 eterization.

367 The results presented in this paper are based on a localized study around four WBC  
 368 regions – Gulf Stream (GS), Kuroshio, Agulhas, and Brazil-Malvinas Confluence (BMC)  
 369 – and involves subfilter-scale (SFS) fields obtained using a highly scale-selective spatial  
 370 filter. The parameterization significantly influences SFS SST and LHF variability around  
 371 the western boundary current regions, as several locations display more than 30% increase  
 372 in their standard deviation (figure 2). Instantaneous SST-LHF correlations and  $\partial\text{SST}/\partial t$   
 373 - LHF tendency correlations as a function of the filter scale revealed the impact of the  
 374 parameterization on large-scale SST-LHF covariability and the associated transition scales.  
 375 We established that the changes in the SFS SST and LHF variances produced by the pa-  
 376 rameterization are physically significant as they cascade to larger scales and yield sub-  
 377 stantial modifications in the mean fields’ correlations, which were found consistent with  
 378 the high-resolution J-OFURO3 observations. Although the high-/low-pass fields used  
 379 in this paper are obtained using the Taper filtering kernel following Grooms et al. (2021),  
 380 a Gaussian filtering kernel was also tested. The latter resulted in qualitatively similar  
 381 results with a slight drop in the instantaneous SST-LHF correlations and an increase in  
 382 the  $\partial\text{SST}/\partial t$  - LHF tendency correlations; therefore, our results are robust to filtering  
 383 kernels. The comparison of a pre-industrial climate simulation to modern observations  
 384 is a limitation of this study. Nevertheless, the conclusion that the stochastic parameter-  
 385 ization leads to increases in ocean-intrinsic air-sea heat flux variability is not likely to  
 386 be sensitive to climate changes.

387 This work has significant potential for further advancements. One possible line of  
 388 extension is a systematic study of seasonal dependence of the correlations and the tran-  
 389 sition length scales while focusing on their physical mechanisms. Another possible re-  
 390 finement is to make the whole study more consistent by considering a CESM-MOM6 sim-  
 391 ulation with a spatial resolution similar to the observations ( $1/4^\circ$  here). Presently the  
 392 observations have more spatial scales resolved and higher variance across scales than the  
 393 model output. It may also be valuable to develop a physics-based stochastic parameter-  
 394 ization for small-scale air-sea flux variability by directly manipulating bulk flux formu-  
 395 las, which possess significant covariability among its constituent variables – all interact-  
 396 ing in a nonlinear fashion.

## 397 Data Availability Statement

398 The CESM-MOM6 outputs and the Python analysis scripts used in this work are  
 399 available in the Zenodo repository: <https://doi.org/10.5281/zenodo.7359120>. The cou-  
 400 pled CESM-MOM6 datasets for other earth system components, e.g., atmosphere, land  
 401 (not used in this work), are available upon request. The J-OFURO3 observations are avail-  
 402 able for download from the official J-OFURO project website ([https://www.j-ofuro.com/en/dataset/entry-  
 403 323.html](https://www.j-ofuro.com/en/dataset/entry-323.html)).

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