

1 **Atmospherically Driven Seasonal and Interannual**
2 **Variability in the Lagrangian Transport Time Scales of**
3 **a Multiple-inlet Coastal System**

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11 **Key Points:**

- 12 • The Lagrangian transport time scales in the Dutch Wadden Sea are typically 1.8
13 times smaller in autumn-winter than in to spring-summer.
14 • The seasonal and interannual variability of the Lagrangian transport time scales
15 is attributed to the local wind.
16 • The winter interannual variations are well explained by North Atlantic large-scale
17 atmospheric patterns.

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Abstract

Intense short-term wind events can flush multiple-inlet systems and even renew the water entirely. Nonetheless, little is known about the effect of wind variations at seasonal and interannual scales on the flushing of such systems. Here, we computed two Lagrangian transport time scales (LTTS), the residence and exposure times, for a multiple-inlet system (the Dutch Wadden Sea) over 36 years using a realistic numerical model simulation. Our results reveal pronounced seasonal and interannual variability in both system-wide LTTS. The seasonality of the LTTS is strongly anti-correlated to the wind energy from the prevailing directions, which are from the southwesterly quadrant and coincidentally aligned with the geographical orientation of the system. This wind energy, which is stronger in autumn-winter than in spring-summer, triggers strong flushing (and hence low values of the LTTS) during autumn-winter. The North Atlantic Oscillation (NAO) and the Scandinavia Pattern (SCAN) are shown to be the main drivers of interannual variability in the local wind and, ultimately, in both LTTS. However, this coupling is much more efficient during autumn-winter when these patterns show larger values and variations. During these seasons, a positive NAO and a negative SCAN induce stronger winds in the prevailing directions, enhancing the flushing efficiency of the system. The opposite happens during positive SCAN and negative NAO, when weaker flushing during autumn-winter is observed. Thus, large-scale atmospheric patterns strongly affect the interannual variability in flushing and are potential drivers of the long-term ecology and functioning of multiple-inlet systems.

Plain language summary

In multiple-inlet coastal systems, strong wind events efficiently renew the water in these systems. In this paper, we investigate if the flushing of such systems has also a marked response to wind variability at longer time scales. To quantify the flushing, we compute the time that particles, each representing a certain volume of water, spend in the system before leaving it (known as the residence time) and the total time they spend within it considering future returns (known as the exposure time). Our 36-year simulation of the hydrodynamics of the DWS shows that the wind induces seasonal and interannual variations in both spatially-averaged quantities. The seasonality is related to the wind energy from the dominant directions, which is much larger during autumn-winter than during spring-summer. This variation leads to a reduction of both time scales by, on average, a factor 1.8 from spring-summer to autumn-winter. Two well-known North Atlantic large-scale atmospheric patterns, primarily active during autumn-winter, induce interannual variations in the wind and consequently in both time scales. Thus, future changes in these patterns could strongly affect water transport and the ecology of the Dutch Wadden Sea. Similar situations are likely to occur in other multiple-inlet systems.

1 Introduction

Transport time scales (TTS), such as the residence, exposure, transit, age, and flushing times (Zimmerman, 1976; Monsen et al., 2002), are measures for the efficiency of transport and exchange of water or freshwater content within a water body system and with its surroundings (Cucco et al., 2009; Duran-Matute et al., 2014; Rayson et al., 2016; Xiong et al., 2021). They also serve to estimate the time that a substance, like dissolved nitrogen, takes to be transported off-shore from high-productivity coastal regions (Hailegeorgis et al., 2021); to understand the variability of the mineralization rates of organic matter in sediments (den Heyer & Kalf, 1998); to explain regional differences of nutrient and eutrophication levels (González et al., 2008; Schwichtenberg et al., 2017); and as a first-order estimation of the exposure of a region (e.g. a protected area) to pollutants (Soomere et al., 2011; Patgaonkar et al., 2012; Pawlowicz et al., 2019).

67 Depending on a coastal system’s particularities, the TTS’s variability can be highly
 68 affected by tides, freshwater discharge, gravitational circulation, winds, and other fac-
 69 tors. The influence of some of these forcing mechanisms on the intra-annual and the sea-
 70 sonal variability of the TTS has been explored in bights (Zhang et al., 2010), bays (Dippner
 71 et al., 2019; Jiang et al., 2019) and lakes (Cimatoribus et al., 2019). However, these stud-
 72 ies were based on just 1 to 2 years of data, and thus, a robust relationship of the sea-
 73 sonality with the local forcing cannot be expected if there is a marked interannual vari-
 74 ability.

75 A realistic simulation covering 32 years was used by Du and Shen (2016) to study
 76 the residence time in the Chesapeake Bay. The seasonal, monthly and interannual vari-
 77 abilities of the system-wide Eulerian residence time were found to be mainly controlled
 78 by the freshwater discharge. To determine the role of the wind, they compared two sim-
 79 ulations for a given year, one with the full forcing and the other without wind. They found
 80 that downstream and upstream winds reduce the residence time in the eastern side of
 81 the Bay, whereas only upstream winds increase the residence time on the opposite side.
 82 This means that in this single-inlet system winds from different directions can trigger
 83 complex patterns in the TTS but not necessarily induce net transport across the system.

84 Single-inlet systems contrast with multiple-inlet systems because, in the latter, winds
 85 from specific directions are very efficient in forcing net residual transport across the sys-
 86 tem (Li, 2013; Herrling & Winter, 2015; Duran-Matute et al., 2016). Due to this effect,
 87 the influence of other forcing mechanisms can become of secondary importance during
 88 strong wind conditions. Thus, winds in multiple-inlet systems can strongly modify the
 89 TTS at local, inter-basin, and system-wide scales. This effect has been observed in dif-
 90 ferent multiple-inlet systems using numerical simulations. Cucco and Umgiesser (2006)
 91 showed that, in the Venice lagoon, strong northeasterly bora winds (of around 12 m/s)
 92 lead to a fully wind-driven dominated system, to a reduction of the system-averaged res-
 93 idence time by a factor of 3, and to a negligible return flow. In the Dutch Wadden Sea
 94 (DWS), strong winds exceeding 10 m/s, and aligned with the geographical orientation
 95 of the system, induce a wind-driven flow that reduces the system-wide flushing time of
 96 freshwater discharge by a factor of 10-15 (Duran-Matute et al., 2014; Donatelli et al.,
 97 2022a). Similar strong winds as in the previous cases, also reduced the monthly-average
 98 residence time by about a factor 2 in the Virginia Coast Reserve (Safak et al., 2015); and
 99 the daily-average Lagrangian residence time (for particles released every 1h during a par-
 100 ticular day) in areas located between the inlets of the Barnegat Bay-Little Egg Harbor
 101 estuary by a factor between 2-4 (Defne & Ganju, 2015).

102 Until now, the previous studies linking TTS to wind in multiple-inlet systems fo-
 103 cused on idealized fixed wind conditions (e.g. Cucco & Umgiesser, 2006), synoptic-scale
 104 events (e.g Duran-Matute et al., 2014; Safak et al., 2015) and annual statistics (e.g Do-
 105 natelli et al., 2022a). In the latter case, Donatelli et al. (2022a) showed that sporadic strong
 106 high-frequency winds (with time scales in the order of days) could impact the annual TTS
 107 averages in the DWS, but also the long-term values (mean or median representative of
 108 their 11-year simulation). However, they did not isolate the effect of high- and low-frequency
 109 winds (with time scales of months or longer) on the TTS to unequivocally attribute the
 110 changes in the annual and long-term TTS to high-frequency wind events. The relevance
 111 of the low-frequency variability is further suggested by the fact that monthly and multi-
 112 decadal sea level variability in the North Sea region is modulated by large-scale atmo-
 113 spheric patterns, which are represented by the North Atlantic Oscillation (NAO), the
 114 East Atlantic Pattern (EAP) and the Scandinavia Pattern (SCAN) (Chafik et al., 2017;
 115 Frederikse & Gerkema, 2018). Therefore, we investigate if and how much these large-
 116 scale atmospheric patterns affect the TTS in the DWS.

117 Our goal is to determine the low-frequency variability (i.e., the seasonality and in-
 118 terannual variations) of the Lagrangian TTS (LTTS), particularly the residence and ex-
 119 posure times, in a multiple-inlet system. Moreover, we aim to correlate their system-wide

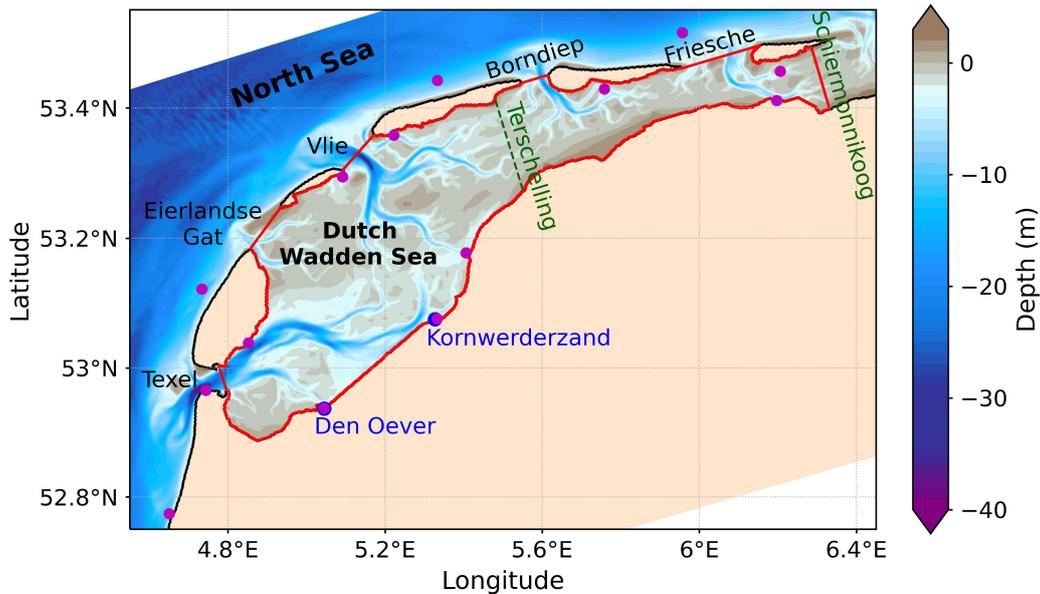


Figure 1. Map of the region of interest. The red contour surrounds most of the DWS and denotes the region where particles were deployed. The names of the five inlets are indicated in black. The Schiermonnikoog and the Terschelling watersheds are marked in green. The location and the names of the two main sluices are depicted in blue. The location of the stations employed for the validation with the sea-surface height (SSH) are shown in magenta. The color bar denotes the depth.

120 behavior with the wind and large-scale atmospheric patterns. The region of analysis covers most of the DWS (Figure 1): a UNESCO world heritage site and a complex multiple-
 121 inlets system. Due to the lack and the difficulty of acquiring observed Lagrangian data
 122 in shallow coastal regions, the results are based on a realistic 36-year simulation (1980-
 123 2015) of the DWS, combined with particle tracking. The simulation consists of an of-
 124 fine coupling of the General Estuarine Transport Model (GETM; Burchard & Bolding,
 125 2002) with the Probably A Really Efficient Lagrangian Simulator (Parcels) v2.1.1 (Lange
 126 & van Sebille, 2017; Delandmeter & Van Sebille, 2019).
 127

128 2 Data and methods

129 2.1 Numerical models

130 2.1.1 Eulerian model

131 The currents, sea level, salinity, temperature, and density are obtained through three-
 132 dimensional, baroclinic numerical simulations performed using GETM. The setup is based
 133 on four nested models, with the DWS numerical domain as the end-member. The do-
 134 main is discretized using an equidistant grid of 200 m resolution using the Rijksdriehoek
 135 projection (the standard projection employed by the Dutch Government) in the horizon-
 136 tal and 25 layers in the vertical. The bathymetry was built based on the measurements
 137 closest in time to 2009-2010 (see Duran-Matute et al., 2014, for details), and the result-
 138 ing map was kept fixed throughout the 36-year simulation. This was done intentionally
 139 to remove the effects of bathymetry variations on the hydrodynamics of the system and
 140 to focus on the role of the atmospheric forcing. The meteorological forcing was taken from

141 the dataset “Uncertainties in Ensembles of Regional Reanalyses” (UERRA; Ridal et al.,
 142 2017), which has a spatial resolution of 11 km and a temporal resolution of 1 h. The fresh-
 143 water discharge through the Den Oever and Kornwerderzand sluices and 10 other smaller
 144 ones was reconstructed based on data from Rijkswaterstaat with a temporal resolution
 145 of 12 minutes (see Duran-Matute et al., 2014, for details). Our model configuration is
 146 almost identical to those employed by Donatelli et al. (2022a, 2022b), but the simula-
 147 tion here spans 36 years instead of 11 years.

148 We contrast our numerical results with sea-surface height (SSH) measured at 14
 149 tidal stations located within and around the DWS (Figure 1). Our simulation performed
 150 similar as the one by Duran-Matute et al. (2014), and a full description of the valida-
 151 tion can be found in Text S1 from Supporting Information S1.

152 *2.1.2 Lagrangian model*

153 Passive particle trajectories were obtained offline by feeding vertically-averaged ve-
 154 locities every 20 minutes from the GETM simulation to Parcels. We used a fourth-order
 155 Runge-Kutta method for the temporal integration and a bilinear interpolation in space,
 156 which showed to be accurate enough in idealized and realistic applications (Lange & van
 157 Sebille, 2017; Delandmeter & Van Sebille, 2019). We used a time step of 158 s to bal-
 158 ance accuracy and computational time. It was also chosen to have the timestep as an
 159 integer fraction of the M2 tidal period (44714 s), which is the main tidal constituent in
 160 the DWS. In our setup, particles were released within the region of interest (denoted with
 161 the red contour in Figure 1) in the center of each of the 200 m \times 200 m grid cells but
 162 skipping every other cell. Then they were advected with depth-averaged currents to cap-
 163 ture the effects of the net horizontal currents on water transport. This procedure was
 164 repeated every M2 period from January-1980 to October-2015, with each release con-
 165 sisting of 12967 particles. The total amount of particles trajectories obtained is (12967
 166 particles per deployment) \times (25290 deployments) \approx 328 million particle trajectories (\approx
 167 1.1 TB of data). To avoid deploying particles when most of the tidal flats are dry, the
 168 first deployment was near the time of maximum water volume within the DWS so that
 169 the subsequent ones (every M2 period) were also close to maximum volume conditions.
 170 The particle positions were saved every M2 period to remove the back-and-forth due to
 171 this dominant semidiurnal tidal constituent in the DWS (Zimmerman, 1976). We, thus,
 172 capture the net residual displacement of the particles. We note that individual tidal pe-
 173 riods may deviate somewhat from the M2 period, but since M2 is the dominant constituent,
 174 the long-term mean tidal period equals the M2 period (Gerkema, 2019).

175 To avoid errors in the estimation of LTTs due to particles being stuck because of
 176 being released too close to the coast or to areas that seldom flood, we removed such par-
 177 ticles from our original dataset (containing \approx 328 million particles trajectories) using three
 178 steps. In the first step, we discarded beaching particles (defined as the ones located within
 179 100 m of a land point at any time), which represents around 8.4% of the original data.
 180 In the second step, we removed particles that do not leave our domain of interest (red
 181 contour in Figure 1) through its open boundaries within their integration time (around
 182 1.8%). This latter condition help to remove particles whose trajectories can be poten-
 183 tially affected by the poorly resolved flow near the coast, even though they are not beach-
 184 ing according to our definition. These particles can spend some days barely moving and
 185 meandering close to the coast due to the small currents present in these areas. In gen-
 186 eral, these first two steps remove most of the particle trajectories that suffer from nu-
 187 merical artifacts (e.g. error of the numerical solvers, the spatial resolution of the flow,
 188 and the temporal time step for the integration of trajectories; which are described by Delandmeter
 189 and Van Sebille (2019)). In the third and last step, all the particles released from po-
 190 sitions in which the amount of discarded particles (from the previous two steps) repre-
 191 sents more than 30% of the total deployments per point of release were also discarded.
 192 This step, removes an extra 3.4% of particles. These particles were mostly deployed in

193 the few regions that are above mean sea level, which are only flood during large storm
 194 surges. However, omitting this last step leads to almost the same results because most
 195 of the problematic particles were already removed using the first two steps. Finally, af-
 196 ter applying all the previous steps, we end up with around 283 million particle trajec-
 197 tories for our analysis.

198 To check the sensitivity of our results when using non-uniform total integration times,
 199 trajectories of particles released at the beginning of every month of our 36-year simu-
 200 lation were integrated for 177 M2 periods (about 91 days). Then, we decreased this time
 201 linearly until 117 M2 periods (around 60 days) for the particles released at the end of
 202 every month. Particles were not tracked anymore if they crossed the boundaries of the
 203 numerical domain before their integration time was reached. We found that under a com-
 204 mon integration time of 60 days, instead of the 60-91 days interval employed in our anal-
 205 ysis, the results were almost the same since 98.5 % of the 283 million particles left our
 206 domain of interest (see red contour in Figure 1) trough its open boundaries before 60 days.

207 2.2 Definitions of Lagrangian transport time scales (LTTS)

208 The Lagrangian residence time is a function of space and time and highlights the
 209 spatio-temporal heterogeneity of transport. It is defined as the time required for a par-
 210 ticle to exit a domain for the first time (Zimmerman, 1976; Monsen et al., 2002). Nonethe-
 211 less, this first-crossing definition has a drawback. When particles are close to an open
 212 boundary, they might exit the system during ebb and return during flood, possibly re-
 213 peating this behavior during the following cycles, after which they can remain in the do-
 214 main for several days. In this way, such a definition of the residence time might give a
 215 wrong idea of the actual time particles spend in the system, particularly close to the in-
 216 lets. We largely avoid this problem by saving particle positions only every M2 period (i.e.,
 217 using the net or residual displacement). With those generated tracks, we define the La-
 218 grangian residence time as the number of M2 periods required for the particles to leave
 219 our domain of interest (red contour in Figure 1) trough its open boundaries. Since the
 220 residence time varies with space and time, we define T_r^{ij} as the residence time of a par-
 221 ticle released during the j -th deployment (at time t_j) at position (x_i, y_i) , where i is the
 222 spatial index of the particle released in the center of the 200 m \times 200 m grid, and t_j are
 223 the times of deployments (every M2 cycle during our 36-year simulation). A similar ap-
 224 proach is employed for the Lagrangian exposure time T_e^{ij} , which is defined as the total
 225 amount of time a particle spends in our system (neglecting the time spent outside of it),
 226 and thus $T_e^{ij} \geq T_r^{ij}$ (Monsen et al., 2002; Huguet et al., 2019).

To describe the spatial variability between seasons, we further define the tempo-
 ral average over N_d^i deployments as

$$T_r^i = \frac{\sum_{j=1}^{N_d^i} T_r^{ij} H^{ij}}{\sum_{j=1}^{N_d^i} H^{ij}}, \quad (1)$$

where N_d^i is the total amount of deployments per point of release available during time
 period for averaging, and H^{ij} is the height of the water column in which the particle is
 deployed. Specifically, we consider two temporal averages: one for all autumn-winter (September-
 February) and one for all spring-summer (March-August) seasons of our 36-year simu-
 lation. The weighted average using H^{ij} is employed because particles are advected with
 depth-averaged currents, and thus, a particle released over a large water column repre-
 sents more fluid with that value of T_r^{ij} (Ridderinkhof & Zimmerman, 1990). To study
 the variability of the system-wide LTTS, we define the spatial average over all N_p^j par-

titles released at the same time as

$$T_r^j = \frac{\sum_{i=1}^{N_p^j} T_r^{ij} H^{ij}}{\sum_{i=1}^{N_p^j} H^{ij}}. \quad (2)$$

227 Similarly, we obtain T_e^i and T_e^j using equivalents to equation (1) and equation (2) for
228 the exposure time, respectively.

229 **2.3 Atmospheric forcing characterization**

230 To understand the origin of the variability of the LTTS, we characterize the atmo-
231 spheric forcing using a local and a large-scale approach.

232 **2.3.1 Local approach**

For the local approach, we employ the concept of sectorial wind energy, following Gerkema and Duran-Matute (2017). The wind direction is divided into eight sectors using the indices $s = 1, \dots, 8$, corresponding to southerly (S), southeasterly (SE), easterly (E), northeasterly (NE), northerly (N), northwesterly (NW), westerly (W), and southwesterly (SW) winds (i.e., the direction from which the wind blows). Then, the kinetic energy of an air parcel (wind energy) with mass m crossing a unit area A during an interval Δt and from sector or direction s is given by

$$E_{s,n} = \frac{1}{2} m W_{s,n}^2 = \frac{1}{2} \rho V W_{s,n}^2 = \frac{1}{2} \rho A \Delta t W_{s,n}^3, \quad (3)$$

233 where V is the volume, which is equal to the area A times the length $W_{s,n} \Delta t$; $W_{s,n}$ is
234 the hourly wind speed (used in the GETM simulation) blowing from sector s , with n as
235 a temporal index running over our full 36-year simulation; $\Delta t = 3600$ s is the resolu-
236 tion of our wind data; and $\rho = 1.225$ kg m⁻³ is the density of the air at sea level with
237 temperature of 15°.

238 In all our analysis, the wind energy from the grid point closest to the middle of the
239 Texel inlet is employed. Due to the small spatial variations of the wind inside the DWS,
240 we anticipate that using the wind energy from different locations does not change qual-
241 itatively our results, as was also the case for Duran-Matute et al. (2016) in their anal-
242 ysis of the residual volume transport in the DWS.

243 **2.3.2 Large-scale approach**

244 For the large-scale approach, we use the North Atlantic Oscillation (NAO), the East
245 Atlantic Pattern (EAP), and the Scandinavian Pattern (SCAN). To derive them, we per-
246 form an empirical orthogonal function (EOF) analysis following Chafik et al. (2017) and
247 Frederikse and Gerkema (2018). With this method, the atmospheric patterns have spa-
248 tial structures represented by empirical orthogonal functions (EOFs), whereas their tem-
249 poral variability are captured by principal components (PCs). To obtain the EOFs and
250 PCs, we employ the monthly-mean sea level pressure (SLP) from the NCEP/NCAR Re-
251 analysis 1 (Kalnay et al., 1996) spanning the period 1950-2015 in the North Atlantic/European
252 sector (30°-80°N, 80W-50°E). For every grid cell, the monthly-mean SLP is detrended
253 and deseasonalized, i.e., the linear trend, and the annual and semi-annual components
254 are removed. Then, the data are weighted by the cosine of the latitude at every grid point
255 before computing the EOF analysis. This is done to give less weight to grid cells located
256 towards the poles as they represent less area (which decreases with the cosine of the lat-
257 itude in spherical coordinates). Finally, the EOF analysis is performed only in the North
258 Atlantic domain to avoid the influence of regions outside of it in the three main modes
259 of variability obtained.

3 Results and Discussions

3.1 Seasonality and interannual variability of the LTTS

The mean autumn-winter and spring-summer spatial patterns for the residence time T_r^i (from equation (1)) are shown in Figures 2a and 2b, and in Figures 2c and 2d for the exposure time T_e^i . The lowest values are found near the inlets since they are the primary regions for exchange with the adjacent North Sea. Particles deployed around them leave the system in less than one week, with the corresponding areas being larger during autumn-winter. The highest values are found farther into the basins and mostly in the Western DWS (west of the Terschelling watershed). These values are up to a factor of two larger during spring-summer than during autumn-winter. Most of the particles deployed in the Western DWS during spring-summer tend to return to the DWS (see difference between T_e^i and T_r^i in the inset of Figure 2d). Nonetheless, during autumn-winter (inset of Figure 2c) this effect is observed only in the southern-most part of the domain. Consistent with all of the previously mentioned behavior, the wind roses show a marked difference between autumn-winter (Figure 2e) and spring-summer (Figure 2f), with the former exhibiting more frequent and stronger winds from the W, SW and S directions.

To get a representative seasonal cycle of the LTTS in the full DWS, we computed the spatial mean of the residence and exposures times (i.e., T_r^j and T_e^j from equation (2)). Then, the annual cycle for the residence and exposure times are estimated by fitting T_r^j and T_e^j to a model with a free constant and an annual harmonic. The system-wide annual signal of T_r^j varies from 10-11 days in November-January to 17-18 days in May-July, and for T_e^j from 14-16 days to 24-25 days, respectively (Figure 3). This means that the extra time that particles spend in the DWS system after they leave for the first time is smaller in November-January (around 4 days) than during May-July (around 7 days).

To understand the variability superimposed on the seasonal cycle, high-frequency effects (e.g., tides and energetic synoptic-scale events) from T_r^j (which has an M2 resolution) were removed by computing a 15-day mean, which is shown as \hat{T}_r in Figure 4a. Afterwards, we performed a wavelet analysis (Torrence & Compo, 1998) of this spatially-averaged 15-day-mean residence time (\hat{T}_r), using the rectification of the bias proposed by Liu et al. (2007), to capture the localized time-frequency information in our time series. The wavelet power spectrum exhibits the strongest signal around the annual period (Figure 4b). However, anomalous behavior is still observed, with periods displaying a strong annual power (e.g., around 1983, 1990, 2000, and 2014) or a weak one (e.g., around 1986, 1996, 2006, and 2010). Similar results are obtained for the equivalent exposure time \hat{T}_e (Figure 5). Clearly, studies of the DWS based on time series of a few years, like those for 2009-2011 by Duran-Matute et al. (2014, 2016) and for 2005-2015 by Donatelli et al. (2022a, 2022b), cannot capture well this rich temporal variability of the system-wide transport characteristics.

The wavelet power spectrum of \hat{T}_r (Figure 4b) also contains significant power outside the annual signal, like the time spans with strong four-month periodicity around 1984, 1990 and 1997. There are also higher frequency events with a still significant signal but they are close to the background noise. These events cause large peaks with a relatively low persistence of only a few weeks. Thus, to focus on the system-wide low-frequency (seasonal and interannual) variations of the LTTS and to find links with the wind forcing (which we discuss in section 3.2) and large-scale circulation and atmospheric patterns (which will be addressed in section 3.3), we filtered the time series. We removed variability from \hat{T}_r using a wavelet filter with a cutoff period of half a year. This procedure resulted in the half-year low-pass filtered signal of the spatially-averaged 15-day-mean residence time (\tilde{T}_r) and exposure time (\tilde{T}_e) (see Figures 4a and 5a, respectively). Most of the variability at low frequencies is due to the seasonal cycle. However, there are fluctuations at interannual time scales that modulate it. Clear examples are the anomalous winters (DJF) with the lowest \tilde{T}_r (5-7 days) of 1983, 1990, 1995, 2000, 2007, 2008, and

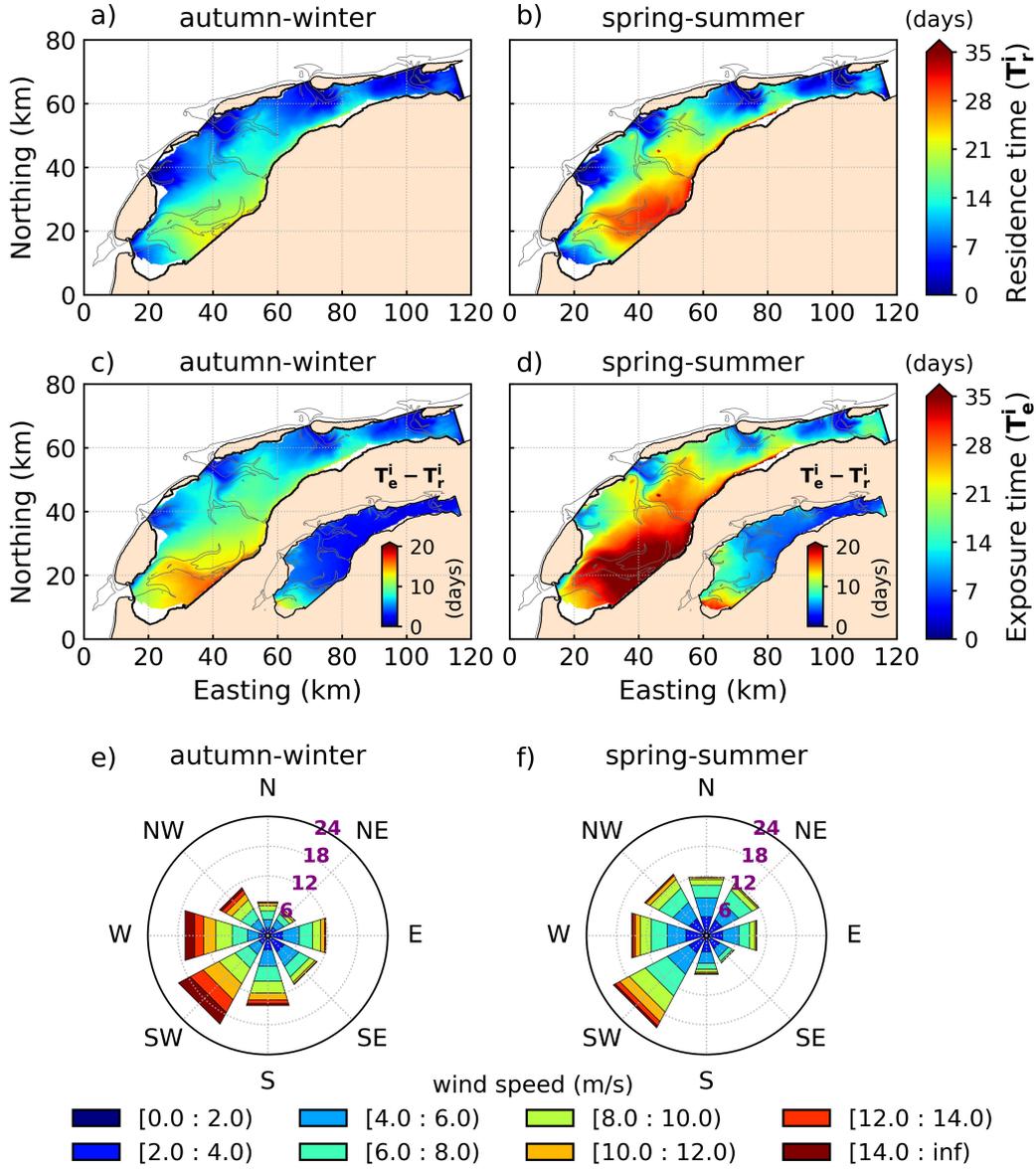


Figure 2. The time-averaged residence time T_r^i for a) autumn-winter (September-February) and b) spring-summer (March-August) based on the 36-year simulation; and the mean exposure time T_e^i for c) autumn-winter (September-February) and d) spring-summer (March-August). The insets in c) and d) show the difference between T_e^i and T_r^i . Regions in white within the DWS were removed from the analysis (see section 2.1.2). The grey line indicates the -5 m isobath. e) Autumn-winter and f) spring-summer wind rose, in which the purple numbers indicate the percentage of time that the wind blows from a particular direction.

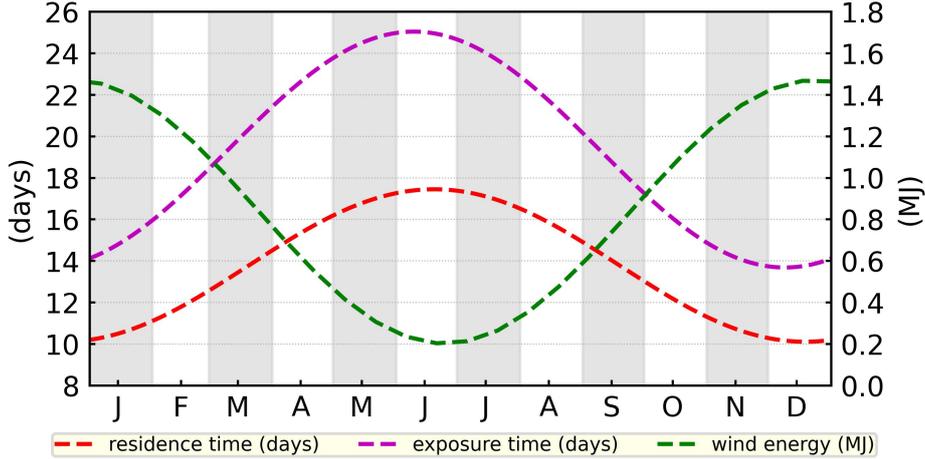


Figure 3. Annual cycle of the residence time (red), the exposure time (magenta), and the wind energy (green).

2014 (using the year after December as the name of the winter); or the anomalous winters with the largest \tilde{T}_r (12-17 days) of 1996, 2003, 2006, 2009, and 2010. In summer (JJA), the variability of the peaks is less pronounced, with values that vary between 15 and 20 days. For \tilde{T}_e (Figure 5a), a similar behavior is observed during those winters, with the lowest values around 7-8 days and the largest between 16-28 days. During summer, \tilde{T}_e mainly varies between 21 and 30 days.

3.2 Impact of the wind on the system-wide LTTTS

To show the dominance of the wind on the variability of the LTTTS, we propose a reconstruction of \tilde{T}_r (and an identical one for \tilde{T}_e) using the energy of the most dominant wind sectors (W, SW, and S). Winds from these directions are the most efficient for driving a strong residual flow from the Texel inlet to the Vlie inlet and the Terschelling watershed (Duran-Matute et al., 2014). We refer to this reconstruction as the *wind-based model* and is given by

$$\bar{T}_r = A e^{-\tilde{E}/B}, \quad (4)$$

where \tilde{E} is the sum of the half-year low-pass filter signal of the 15-day-mean wind energy of the dominant sectors (see Appendix A for the definition of the 15-day-mean wind energy per sector, and for the computation of \tilde{E}). Because \tilde{T}_r and \tilde{T}_e are quantities that depend on the future, the *wind-based model* employs \tilde{E} of the next 15-day interval in comparison to the LTTTS time series. The constants A and B are fitting coefficients. The negative sign in the argument of the exponential reflects the anti-correlation between \tilde{T}_r and \tilde{E} (Figure 6a), which means that strong \tilde{E} conditions result in low \tilde{T}_r and \bar{T}_r ; while the opposite holds during weak \tilde{E} conditions. The constant $A = 19.29 \pm 0.16$ days (with 95% CI) for \bar{T}_r represents the maximum value that can be predicted with \bar{T}_r , which is reached during $\tilde{E} = 0$ conditions. This constant contains the mean effects of the residual tides, freshwater discharge, and other wind directions not included in the reconstruction. The constant $B = 2.31 \pm 0.06$ MJ is an e-folding wind energy scale for \bar{T}_r , which indicates that an increase in \tilde{E} equal to B would lead to a reduction of \bar{T}_r by 63%. For the exposure time, there is also a strong anti-correlation between \tilde{T}_e and \tilde{E} (Figure 6b). The maximum value predicted by \bar{T}_e is given by $A = 27.96 \pm 0.13$ days, and its e-folding wind energy scale is $B = 2.07 \pm 0.03$ MJ.

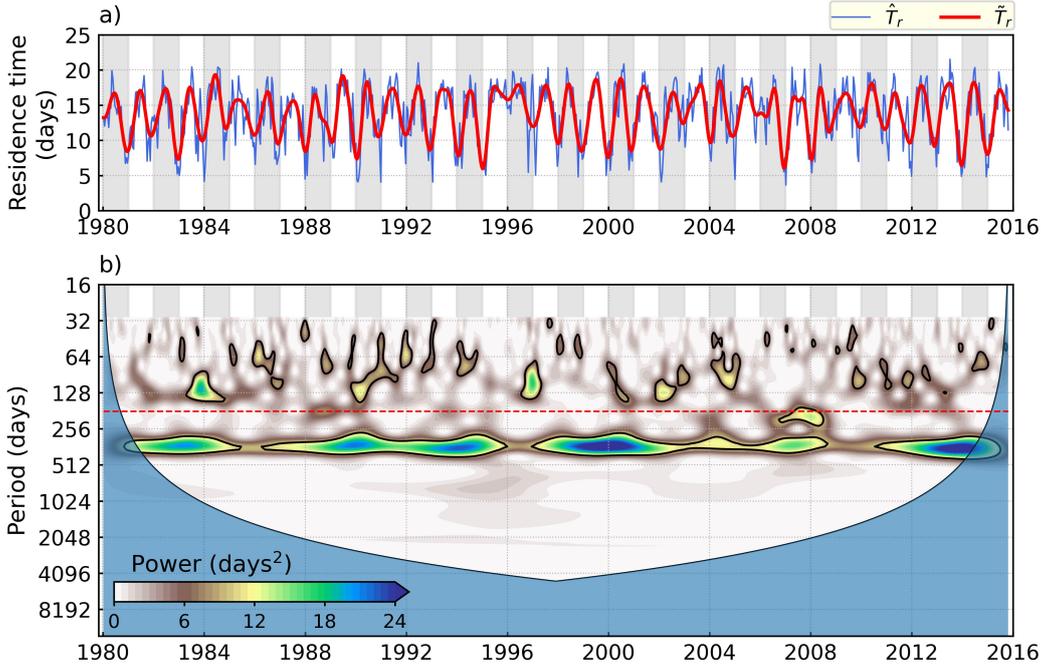


Figure 4. (a) Time series of the spatially-averaged 15-day-mean residence time (\hat{T}_r), and its half-year low-pass filtered component (\tilde{T}_r). (b) Wavelet power spectrum of \tilde{T}_r , where the black contour encloses regions with power greater than a lag-1 red-noise process with 95% confidence level; and the grey shadow region is the “cone of influence”, where errors due to the finite length of the time series are present. The horizontal red dashed line highlights the half-year period employed as a cutoff for computing \tilde{T}_r .

335 The values of \bar{T}_r (Figure 6a) match the numerical data quite well, with a Pearson
 336 correlation coefficient $R = 0.94$ and a root mean square error $RMSE = 1.05$ days (see
 337 Wilks (2011) for the definition of R and $RMSE$), with the latter representing 7% of the
 338 difference between the largest and lowest \hat{T}_r (15 days). Similar results are obtained
 339 for the exposure time (Figure 6b), with $R = 0.95$ and $RMSE = 1.58$ days, which repre-
 340 sents 6% of the difference between the largest and lowest \hat{T}_e (25 days). These results re-
 341 flects the capacity of the *wind-based model* to capture the seasonality, the energy trans-
 342 fer of most of the anomalous autumn-winter seasons to \hat{T}_r and \hat{T}_e , and some of the small
 343 spring-summer \tilde{E} fluctuations that modify both time scales during these seasons.

344 An exponential relationship between the residence time and the local forcing was
 345 also found in the Pearl River estuary (Sun et al., 2014), but with the freshwater discharge
 346 as predictor in this riverine dominated estuary. The exponential model used in their study
 347 and in ours captures the asymptotic behaviour of the TTS keeping physical values larger
 348 than zero during strong forcing conditions. For our case, the *wind-based model* can pro-
 349 vide robust predictions if, for example, the model would be exposed to larger \tilde{E} values
 350 not seen during the fitting step. These attributes are hard to achieve with linear or poly-
 351 nomial models, which make the exponential one a good and a simple tool to predict TTS.

352 An example of the ability of the *wind-based model* to capture anomalous \hat{T}_r val-
 353 ues is the winter of 1990. During this period, the lowest \hat{T}_r is well reproduced, which is
 354 related to the largest \tilde{E} (3 MJ) of our 36-year record (Figure 6a). On the opposite side,
 355 we have the winter of 1996, which is a famous period in the North Sea region due to its

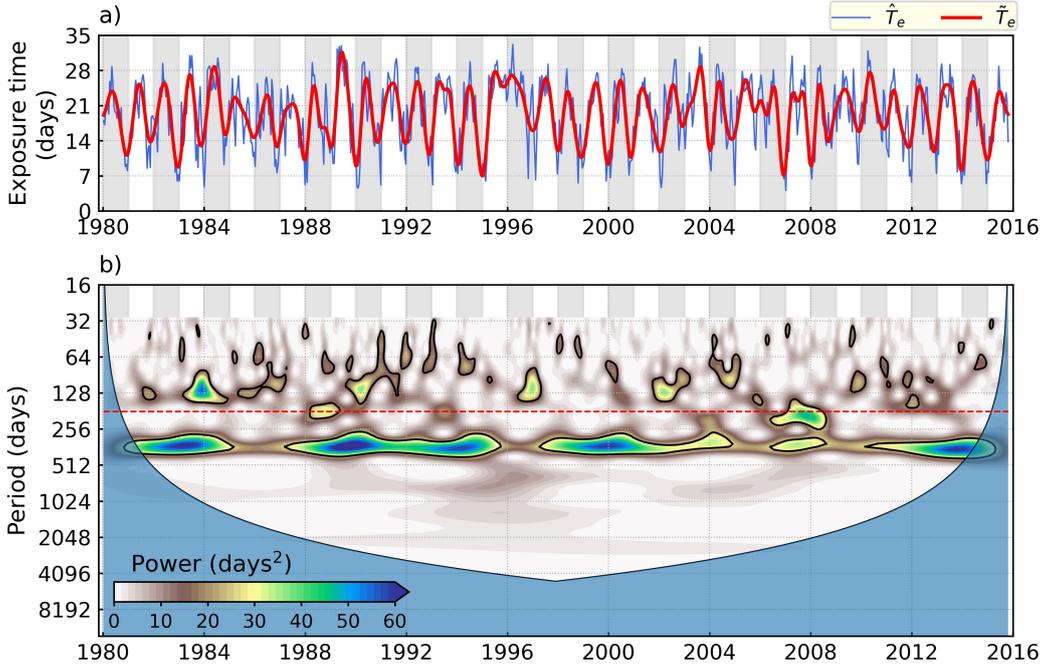


Figure 5. As in Figure 4, but for the exposure time.

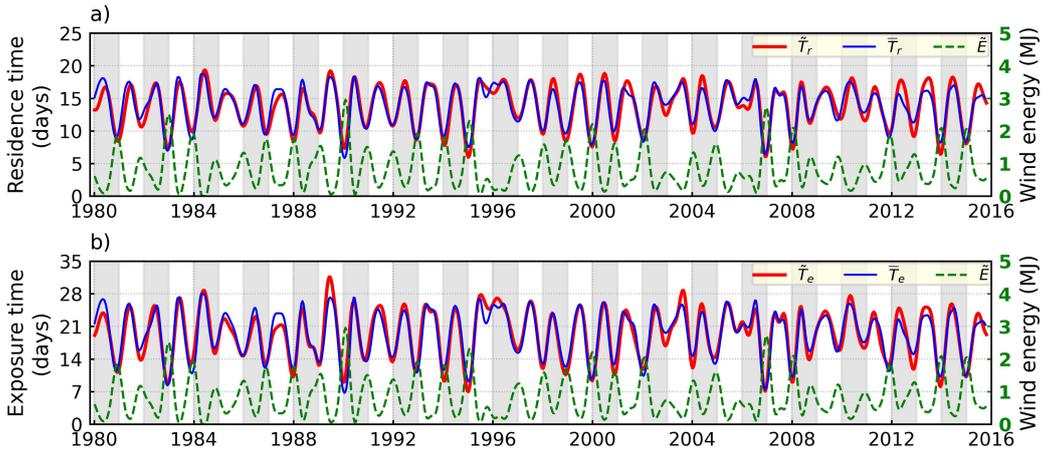


Figure 6. (a) Time series of the half-year low-pass filter of the spatially-averaged 15-day-mean residence time (\tilde{T}_r), which is the same as the red line in Figure 5a; the reconstruction of \tilde{T}_r using the *wind-based model* (\bar{T}_r , equation (4)); and the sum of the half-year low-pass filter of the 15-day-mean wind energy of the dominant wind sectors W+SW+S (\tilde{E}). (b) Time series of the half-year low-pass filter of the spatially-averaged 15-day-mean exposure time (\tilde{T}_e); the reconstruction of \tilde{T}_e using the *wind-based model* (\bar{T}_e , instead of \bar{T}_r in equation (4)); and \tilde{E} .

356 low temperatures (Loewe, 1996). In this season, winds from the most dominant direc-
 357 tions were unusually weak, but strong E winds were predominant, with most of their vari-
 358 ability contained in periods of less than half a year. During this winter, \tilde{T}_r shows larger
 359 values than expected from the climatological winter months and exhibited closer values
 360 to the climatological summer months. The *wind-based model* (Figures 6a and 6b for \bar{T}_r

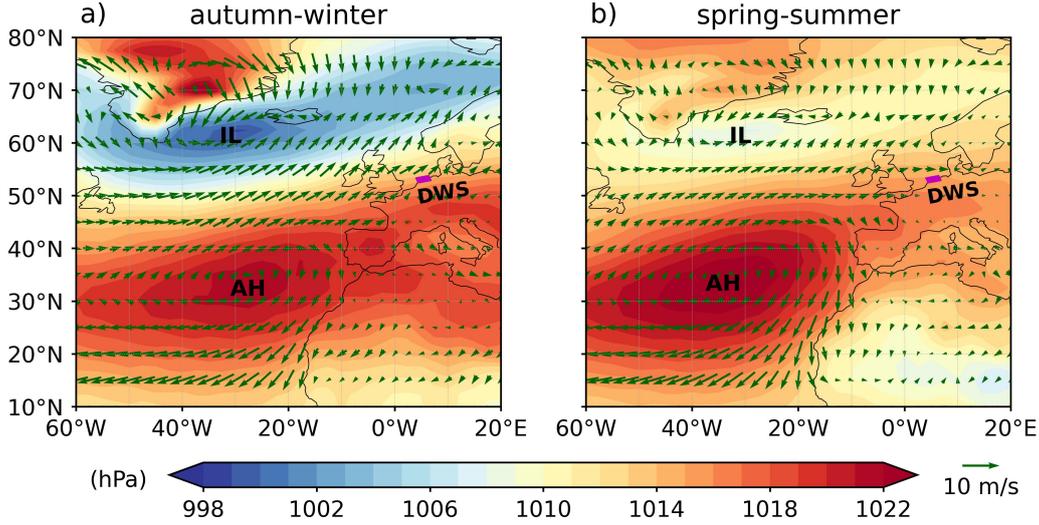


Figure 7. Mean sea level pressure and wind at 10 m above ground for a) autumn-winter (September-February) and b) spring-summer (March-August). These averages were obtained using the monthly NCEP/NCAR Reanalysis 1 data for the 1980-2015 period. The mean wind vector is obtained by separately computing the average wind direction and speed following Farrugia and Micallef (2017). The small purple rectangle in panels (a)-(b) represents the DWS numerical domain. The location of the Azores High (AH) and Icelandic Low (IL) pressure systems are also highlighted.

361 and \bar{T}_e , respectively) suggests that the large values of the LTTS in winter of 1996 are
 362 explained by the weak wind energy from the usually dominant directions and not by the
 363 strong easterly winds observed (which are not explicitly included in the *wind-based model*).

364 **3.3 The role of the large-scale atmospheric circulation and patterns on**
 365 **the system-wide LTTS**

366 The annual cycle of the large-scale wind in the subtropical North Atlantic is related
 367 to the seasonality (a meridional shift and change in intensity) of the the Azores High and
 368 the semi-permanent Icelandic Low North Atlantic pressure systems (Trenberth et al., 1990)
 369 (Figure 7). This variability is transferred to the regional wind, which induces a local wind
 370 response, and ultimately to the LTTS. As a result, a prevailing climatological wind en-
 371 ergy (from the SW quadrant) is induced in the DWS, which was computed fitting the
 372 sum of the 15-day-mean wind energy of the dominant sectors (W+SW+S, see equation
 373 (A2) in appendix A for the formal definition) to a model with a free constant and an an-
 374 nual harmonic. This signal is aligned with the geographical orientation of the system,
 375 and characterized by larger values in autumn-winter than in spring-summer (seven times
 376 more when contrasting the peaks in November-January with the lowest values in June-
 377 July, see Figure 3). Thus, it explains why the DWS is at its most efficient climatolog-
 378 ical state for flushing in autumn-winter, which are the seasons when the LTTS are the
 379 lowest (Figures 2a, 2b, and 3).

380 Other low-frequency variations of the wind and sea level pressure, which are not
 381 explained by the seasonality, are mainly related to large-scale atmospheric patterns, such
 382 as the NAO, EAP and SCAN (Frederikse & Gerkema, 2018). Therefore, our final ob-
 383 jective is to determine if interannual variations of the LTTS in the DWS are driven by

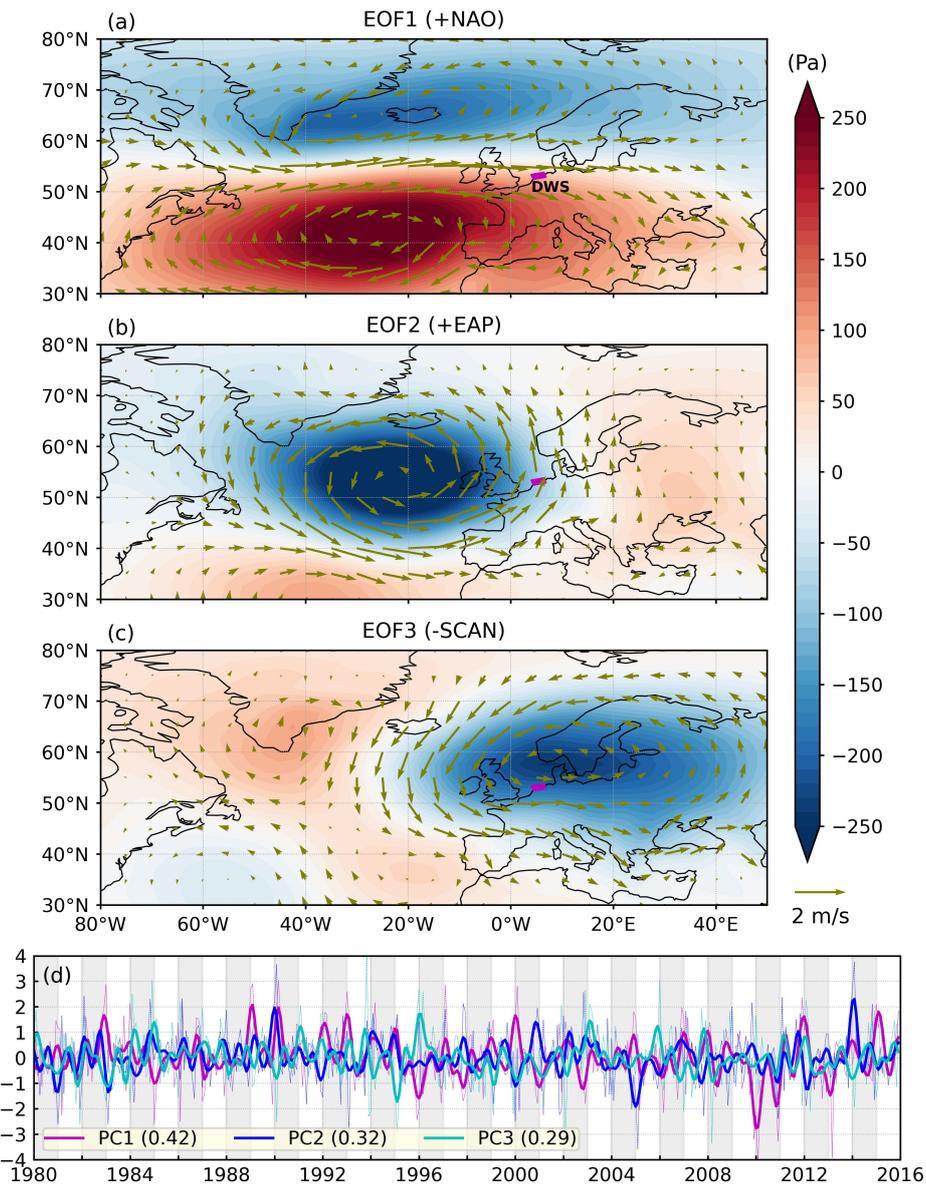


Figure 8. The three leading modes of the empirical orthogonal function (EOF) analysis based on the deseasonalized monthly-mean sea level pressure over the North Atlantic sector. (a)-(c) EOFs with units of Pressure (Pa), and (d) the monthly PCs (dotted lines) and their half-year low-pass filtered component (thick lines). The EOF and PC modes are defined following the common positive convention for NAO, EAP and SCAN (see the website of the Climate Prediction Center, <https://www.cpc.ncep.noaa.gov/data/teledoc/telecontents.shtml>). The first two EOFs (NAO and EAP) are displayed during their positive phases, whereas the third one (SCAN) is depicted during its negative phase. The geostrophic winds computed from the EOFs are depicted with arrows. The variance of the three monthly PCs (PC1 for NAO, PC2 for EAP, and PC3 for SCAN) is scaled to 1, and the numbers in the legend of (d) highlight the fraction of variance explained by the low-pass filtered PCs with respect to their monthly values. The small purple rectangle in panels (a)-(c) represents the DWS numerical domain.

384 these large-scale patterns. First, we obtain the three leading modes of variability from
 385 the EOF analysis of the deseasonalized monthly-mean SLP in the North Atlantic region
 386 (see section 2.3.2). Their spatial structure (EOFs) and their temporal variations (PCs)
 387 are shown in Figure 8, and they are very similar to those showed by Chafik et al. (2017)
 388 and Frederikse and Gerkema (2018). These first three modes at a monthly scale explain
 389 32%, 17% and 15% of the SLP variability in the North Atlantic domain. They exhibit
 390 large-scale atmospheric structures that are akin to the NAO, EAP and SCAN telecon-
 391 nection patterns. In comparison to the method used by the Climate Prediction Center
 392 (CPC, <https://www.cpc.ncep.noaa.gov/data/teledoc/telecontents.shtml>), our
 393 EOFs and the CPC teleconnection patterns are quite similar, but our PCs and the CPC
 394 indices are not necessarily fully interchangeable (Frederikse & Gerkema, 2018). Our first
 395 mode (NAO) is characterized by a north-south dipole between the Icelandic low and the
 396 Azores high, and it enhances the intensity of the westerlies in the North Sea basin dur-
 397 ing its positive phase (Figure 8a), whereas the opposite holds during its negative one.
 398 Our second mode (EAP) highlights a strong monopole pressure core south of Iceland with
 399 meridionally oriented geostrophic winds in the North Sea (Figure 8b). Two weak cores
 400 of the opposite sign are also present in the southern part of the subtropical North At-
 401 lantic region and over Eastern Europe respectively. The NAO and EAP teleconnection
 402 patterns modulate the variations in the speed of the jet stream, whereas the NAO mostly
 403 describes the latitudinal shifts of the jet, and hence, the main Atlantic storm track (Woollings
 404 & Blackburn, 2012). Our third mode (SCAN) displays a zonal pressure dipole between
 405 Greenland and Scandinavia, with the strongest center of action over Scandinavia and with
 406 a southeastward extension from Greenland towards the Iberian Peninsula (Figure 8c).
 407 Its associated geostrophic winds exhibit a strong meridional shear in the North Sea with
 408 zonal orientation over much of Western Europe. A positive SCAN is closely related to
 409 the well-known Scandinavian blocking weather regime, which in combination with per-
 410 sistent negative NAO phases, can induce extreme cold outbreaks in Europe during win-
 411 ter (Cattiaux et al., 2010; Kautz et al., 2020).

412 To link the interannual variations of \tilde{T}_r (and \tilde{T}_e) to the large-scale patterns, we re-
 413 move the seasonal component from \tilde{T}_r , and then this deseasonalized or anomalous \tilde{T}_r was
 414 reconstructed using a multi-linear regression model. The predictors are based on the monthly
 415 PCs, which were interpolated to match the 15-day resolution of both LTTS, and then
 416 low-pass filtered using a cutoff period of half-year to remove high-frequency variations.
 417 We call this reconstruction the *PCs model*. Similar to the *wind-based model*, the PCs of
 418 the next 15-day interval are used as predictors. The reconstruction of \tilde{T}_r is obtained by
 419 joining the seasonal component with the *PCs model*. This combination is referred to as
 420 the *large-scale model* and is shown in Figure 9a; whereas the reconstruction of the dese-
 421 seasonized \tilde{T}_r given by the *PCs model* is shown in Figure 9b. The *large-scale model* matched
 422 \tilde{T}_r quite well, with $R = 0.94$ and $RMSE = 1.03$ days. It also explains 96% of the vari-
 423 ance of \tilde{T}_r (VAR_{exp} in Figure 9c), from which 72% is attributed to the seasonality, 21%
 424 to SCAN and NAO, and the remaining 3% to EAP. In general, the model captures most
 425 of the autumn-winter variability, but it has difficulties in reproducing the variations of
 426 the spring-summer peaks (Figure 9a), as was also the case for the *wind-based model* (Fig-
 427 ure 6a). Similar results ($R = 0.92$ and $RMSE = 1.97$ days) and weak spring-summer
 428 predictability for the *large-scale model* are obtained for \tilde{T}_e (Figure 10).

429 The maximum predictability of the *PCs model* in terms of VAR_{exp} and R is found
 430 between November and February (Figure 9d), and it is mainly attributed to SCAN and
 431 NAO. This behavior is expected since the effects of the large-scale patterns are notice-
 432 able when the PCs show strong changes and largest values, which is more common dur-
 433 ing autumn-winter (Figure 8d). The lowest \tilde{T}_r observed during autumn-winter (Figure
 434 9a) are predominantly associated with the interplay between negative SCAN, positive
 435 NAO, and positive EAP (Figure 8d), with the latter having the lowest contribution. The
 436 combination of their spatial patterns tend to induce along-coast anomalous winds (mostly
 437 from W and SW directions) that favor the flushing efficiency of the DWS system. This

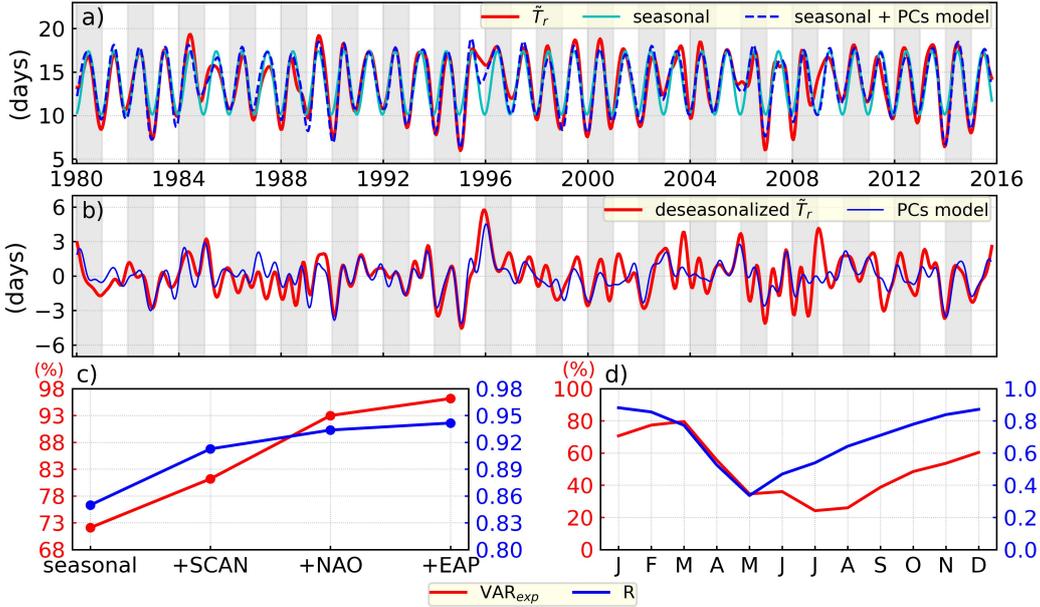


Figure 9. (a) Time series of the half-year low-pass filter of the spatially-averaged 15-day-mean residence time (\tilde{T}_r), its seasonal component, and its reconstruction with the *large-scale model* (seasonal + *PCs model*). (b) The deseasonalized \tilde{T}_r and its reconstruction with the *PCs model*. (c) Explained variance VAR_{exp} and correlation R for the reconstruction of \tilde{T}_r using cumulative components of the *large-scale model*: only the seasonal component; seasonal + SCAN (+SCAN); seasonal + SCAN + NAO (+NAO); and the *large-scale model*, i.e., seasonal + SCAN + NAO + EAP (+EAP). The VAR_{exp} is defined as the ratio between the variance of the cumulative components of the *large-scale model* and the variance of \tilde{T}_r . (d) Monthly statistics (VAR_{exp} and R) of the reconstruction of the deseasonalized \tilde{T}_r with the *PCs model*. In this case, the VAR_{exp} is defined as the ratio between the variance of the *PCs model* and the variance of the deseasonalized \tilde{T}_r per month.

438 behavior is consistent with the study of Chafik et al. (2017), in which negative SCAN
 439 and positive NAO patterns explain most anomalous high monthly sea level values ob-
 440 served at several North Sea tidal gauge stations during autumn-winter. According to our
 441 results, they are concurrent with strong flushing conditions and with a low likelihood for
 442 the particles to return to the DWS (represented by low \tilde{T}_r and \tilde{T}_e , respectively).

443 Winters with the strongest flushing were well captured by the *PCs model* (Figures
 444 9a and 9b). For example, in the winters of 1990, 1995, 2007, and 2014, a decrease of \tilde{T}_r
 445 of around 3-5 days with respect to the December-January climatological value of 10 days
 446 was observed, which was related to high \tilde{E} (Figure 6a). Therefore, the lowest \tilde{T}_r values
 447 were induced by large-scale atmospheric patterns and not by storms, which induce high-
 448 frequency variations and are commonly associated with the presence of well-known weather
 449 regimes (Hochman et al., 2021). For example, during the well-known winter of 1990, two
 450 exceptionally strong storms (“Daria” and “Vivian”) passed over central Europe and crossed
 451 the North Sea in just few days (Pinto et al., 2009). As a result, they trigger the strongest
 452 hourly wind speeds from SW and W directions in our 36-year record (around 30 m/s or
 453 60 MJ), but induced 15-day-mean peaks in the wind energy similar to other less stormy
 454 periods. On the other hand, the most anomalous winters with the largest \tilde{T}_r values (1996
 455 and 2006) were also well explained by the *PCs model*. During these winters, an increase

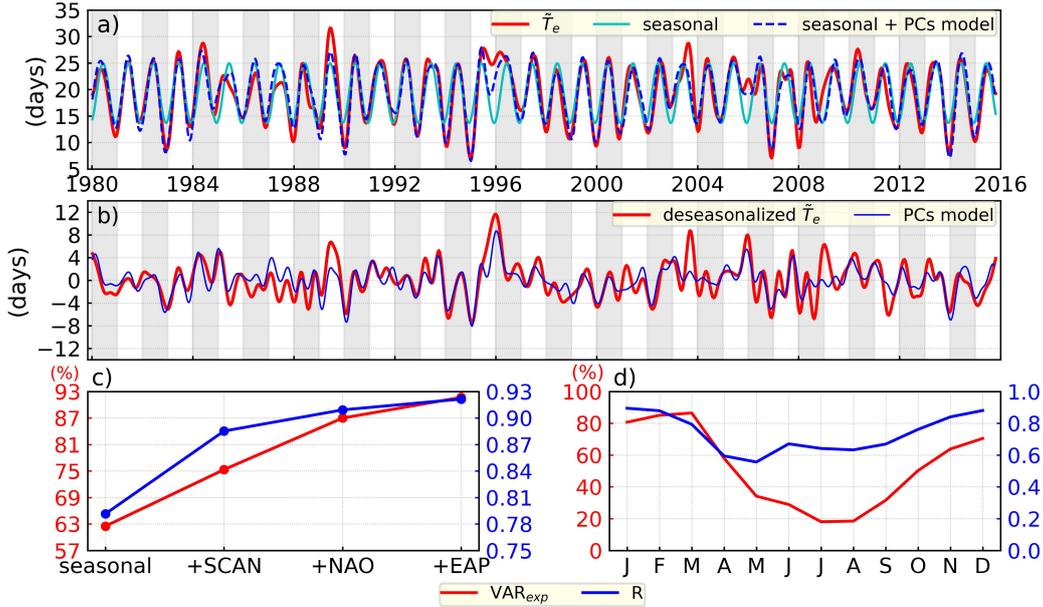


Figure 10. As in Figure 9, but for the exposure time.

of \tilde{T}_r of about 7 and 4 days with respect to the December-January climatology were observed. However, the *PCs model* underestimates these values by around 2-3 days and 1 day, respectively. The most extreme change between two consecutive winters (10 days for \tilde{T}_r and about 20 days for \tilde{T}_e) occurred between the winters of 1995-1996. In 1995, a combination of negative SCAN with positive NAO and EAP triggered a \tilde{E} stronger than its December-January climatology and induced one of the lowest \tilde{T}_r (around 6 days). The following year, the largest \tilde{T}_r during winter was observed (about 17 days). During this famous winter, positive SCAN and negative NAO induced strong E winds. However, as was stated in the previous section, the lack of \tilde{E} (and hence, the background forcing by the tides and freshwater discharge) is enough to explain why \tilde{T}_r during the 1996 winter was similar to its May-July climatology. In agreement with this, during the winter of 2006 (and to a lesser extent for 2003, 2009, and 2010), \tilde{T}_r was also larger than its climatological value, which was related to quite low \tilde{E} , but also to low-frequency energy from the other directions.

3.4 Other sources of variability on the LTTS

Variations of the bathymetry were neglected in our simulation, which was done intentionally to isolate the role of the atmospheric forcing in our results. Relative stability in the location and orientation of the major channels connected to the Texel inlet has been observed since approximately 1972 or 40 years after the construction of the Afsluitdijk in 1932 (Elias et al., 2003, 2006), which is a closure dyke of around 30 km where the two main sluices feeding freshwater into the are located (Figure 1). Changes in the sedimentation-erosion patterns of the channels were observed in these studies, but with only minor modifications of the bathymetry profiles. Thus, during our period of analysis, we expect small effects of these bathymetry variations compared to the large effects of wind, particularly when focusing on the variability of system-wide LTTS, as is the case in most of our results.

The time series of the freshwater discharge from the sluice located at Den Oever is correlated with \tilde{E} ($R = 0.56$) and anti-correlated with \tilde{T}_r ($R = -0.68$) and \tilde{T}_e ($R =$

484 -0.61); whereas for the sluice located at Kornwerderzand non-significant correlations are
 485 obtained. Because of this, it is not trivial to isolate the effect of both sluices on the vari-
 486 ability of \tilde{T}_r and \tilde{T}_e under our current approach. However, it is known that the resid-
 487 ual volume flow rate through the DWS during strong wind conditions from the domi-
 488 nant directions is one order of magnitude larger than the one associated with the tides
 489 and the freshwater discharge (Duran-Matute et al., 2014), and that the total freshwa-
 490 ter discharge of both sluices can only explain less than 5% of the variability of the resid-
 491 ual transport in this system (Donatelli et al., 2022a). Therefore, we expect that the fresh-
 492 water discharge and the residual tidal currents are the main factors controlling the back-
 493 ground \tilde{T}_r ($A = 19.29$ days) and \tilde{T}_e ($A = 27.96$ days), which are obtained when the
 494 wind energy of the most energetic sectors (\tilde{E}) is null in the *wind-based model*. In addi-
 495 tion, these forcing mechanisms also seem to explain part of the variability of \tilde{T}_r and \tilde{T}_e
 496 not explained by the *wind-based model* and the *large-scale model* during calm conditions
 497 (mainly spring-summer months), which are the periods in which both these models show
 498 strong lack of predictability.

499 Because our main results are based on the characterization of the system-wide LTTS,
 500 the vertical structure of the LTTS was ignored using depth-averaged currents. Locally,
 501 there might be a marked heterogeneity in this vertical structure (Wolk, 2003; Du & Shen,
 502 2016), which might be associated to, for example, a strong gravitational circulation. How-
 503 ever, it is not currently feasible to perform a 3D Lagrangian analysis for 36-year of the
 504 DWS due to the amount of data required to compute the necessary 3D particle trajec-
 505 tories. Nonetheless, our results can be useful to select, simulate, and understand the 3D-
 506 behaviour of the LTTS during particular and striking conditions, like the transition be-
 507 tween the winters with strong and weak winds from the most energetic directions in 1995-
 508 1996.

509 4 Conclusions

510 While it has been acknowledged that high-frequency events, like storms crossing
 511 the Dutch Wadden Sea (DWS) in few days or bora winds in the Venice lagoon, can com-
 512 pletely renew the water in multiple-inlet systems, we show here that low-frequency wind
 513 variability can also play a large role in modulating the transport time scales in a multiple-
 514 inlet system. The broad and immediate implication of our results is that interannual changes
 515 in the atmospheric patterns can have a much larger effect on the variations of the wa-
 516 ter transport than may have been expected, and hence, on the long-term ecology and
 517 functioning of multiple-inlet systems.

518 For the case of the DWS, the lowest system-wide Lagrangian transport time scales
 519 (LTTS) are observed in several years during autumn-winter months and are well explained
 520 by the concurrent negative phase of the Scandinavia Pattern (SCAN) and the positive
 521 phase of the North Atlantic Oscillation (NAO), which induce stronger SW and W winds
 522 in this system. These winds trigger an anomalous eastward flow that enhances the flush-
 523 ing efficiency, which is typically already strong in autumn-winter. The opposite happens
 524 during positive SCAN and negative NAO, and weaker flushing during autumn-winter
 525 is observed. In contrast to single-inlet systems (like in the study of Du and Shen (2016)),
 526 our results show that system-wide LTTS in multiple-inlet systems, like the DWS, are rep-
 527 resentative of the overall system when studying the influence of winds on the seasonal
 528 and interannual variations of the LTTS. This response is in agreement with the fact that
 529 winds from specific intensities and directions are very efficient in forcing net residual trans-
 530 port across watersheds (i.e. tidal divides) and through the inlets of multiple-inlet systems
 531 (Li, 2013; Duran-Matute et al., 2016). A similar response can be expected in other wind-
 532 dominated multiple-inlet systems (e.g., along the North Sea coast), leading to seasonal
 533 and interannual variations of the LTTS driven by the large-scale circulation and atmo-
 534 spheric patterns, respectively.

Our findings also reveal that care should be taken when observing variations of the long-term values of the residual volume flow rate across inlets and watersheds, when events with strong wind conditions from the analysis are removed. Using this approach, Donatelli et al. (2022a) found changes of the long-term residual volume transport using a 11-year simulation of the DWS. According to our results, this does not necessarily indicate that extreme events can alter these long-term values. Instead, we expect that long-term variations of the residual flow rate in other wind-dominated multiple-inlet systems would be also driven by large-scale atmospheric patterns, as was the case for the interannual variations of the LTTS in the DWS (from our current study), and for the multi-decadal sea level variability along the North Sea coastal areas (Frederikse & Gerkema, 2018).

Finally, our study highlights the importance of understanding the water transport variability due to local and remote forcing to, for example, explain better why large-scale atmospheric patterns affect biological processes (see e.g., Straile & Adrian, 2000; Golubkov & Golubkov, 2021), and to improve analytical models that use TTS to model ecological processes (see e.g., Lucas & Deleersnijder, 2020). From a practical point of view, analytical models like those proposed here to predict the LTTS using the wind and the large-scale atmospheric patterns could be employed to estimate the LTTS during periods not covered by such detailed simulations, particularly, for seasonal forecasts and future climate-change scenarios.

Conflict of Interest

The authors declare no conflicts of interest relevant to this study.

Data Availability Statement

Data and scripts (based on Python v3.8) used to reproduce the figures of this study are available at the GitHub repository https://github.com/Jeancar1oFU/paper_Atmospherically_Driven_Seasonal_Interannual_LTTS_MultipleInlet. The wavelet analysis is based on the Python package Pycwt v0.3.0a22 (<https://anaconda.org/conda-forge/pycwt>), but we added a script to perform the bias correction (Liu et al., 2007) and a wavelet filter (Torrence & Compo, 1998). Monthly-mean sea level pressure and wind at 10 m above ground were obtained from The NCEP-NCAR Reanalysis 1 data, which is provided by the NOAA PSL, Boulder, Colorado, USA, from their website at <https://psl.noaa.gov/data/gridded/data.ncep.reanalysis.html>. Eulerian data was produced with the GETM/GOTM model, and its set-up is described in Duran-Matute et al. (2014) and Gräwe et al. (2016). The Lagrangian model (Parcels v2.1.1) can be downloaded from <https://anaconda.org/conda-forge/parcels> or <https://oceanparcels.org>.

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Appendix A Wind energy averaging

To establish connections with the LTTS and to smooth the noisy, hourly, high-resolution wind energy data from equation (3), and to remove most of the high-frequency effects (e.g., storms), we compute the mean wind energy during 15-day intervals. For a given

sectorial direction s , the 15-day-mean wind energy is defined as

$$E_s = N^{-1} \sum_n E_{s,n} = \frac{1}{2} \rho A \Delta t N^{-1} \sum_n W_{s,n}^3 = C \Delta t N^{-1} \sum_n W_{s,n}^3, \quad (\text{A1})$$

575 where $N = 360$ is the total amount of hourly data points, $C = \frac{1}{2} \rho A = 0.6125 \text{ kg m}^{-1}$,
 576 and the total wind energy is obtained from $E_T = \sum_s E_s = C \Delta t N^{-1} \sum_n W_n^3$, where
 577 $W_n^3 = \sum_s W_{s,n}^3$ is the cube of the hourly wind speed. A similar expression to equa-
 578 tion (A1), but for yearly averages, was used by Gerkema and Duran-Matute (2017) and
 579 Donatelli et al. (2022a).

The sum of the wind energy of the most energetic sectors (W+SW+S) is obtained from equation (A1) yielding

$$E = E_W + E_{SW} + E_S. \quad (\text{A2})$$

580 This time series, with 15-day resolution, was employed to compute the annual cycle showed
 581 in Figure 3.

582 Then, we apply a half-year low-pass filter to each E_s (equation (A1)), as was done
 583 for the LTTS, which we call \tilde{E}_s . Due to the undulatory nature of the wavelet filter (and
 584 other similar ones like the Lanczos filter) and to the fact that E_s could be near zero, slightly
 585 negative values appear. To be physically correct, we set all negative values of \tilde{E}_s to zero.
 586 Finally, we add \tilde{E}_s from the most energetic sectors (W+SW+S), and get \tilde{E} , which we
 587 call the sum of the half-year low-pass filter of the 15-day-mean wind energy of the dom-
 588 inant sectors. Almost identical results are obtained if we apply the low-pass filter directly
 589 to E defined in equation (A2).

590 References

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