The internal structure of Mercury's core inferred from magnetic observations

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Key Points:

- We model Mercury's internal magnetic field from MESSENGER data with spherical harmonics
- Our core field model contains non-axisymmetric features from which we make inferences of Mercury's internal structure.
- We estimate Mercury's inner core radius of ∼500-660 km and a corresponding thickness of a top stratified layer of ∼880-500 km.

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Abstract

Previous models of Mercury's core magnetic field based on high altitude data from first MESSENGER flybys revealed an axisymmetric. Here we use low altitude MESSENGER data covering the entire mission period to construct spherical harmonic models based on various spatial norms. Although we find a dominantly axisymmetric field, our models nevertheless include detectable deviations from axisymmetry. These non-axisymmetric features appear at high latitudes, resembling intense geomagnetic flux patches at Earth's core-mantle boundary. Based on this core field morphology, we then attempt to infer Mercury's internal structure. More specifically, assuming that Mercury's high-latitude non-axisymmetric features are concentrated by downwellings at the edge of the planet's inner core tangent cylinder, and accounting for the presence of a stably stratified layer at the top of Mercury's core, we establish a relation between the inner core size and the thickness of the stratified layer. Considering plausible ranges, we propose that Mercury's inner core size is about 500-660 km, which corresponds to a stratified layer thickness of 880-500 km, respectively.

1 Introduction

Based on Mariner and MESSENGER satellite missions, it was found that Mercury's internal magnetic field is very weak, dipole dominated, largely axisymmetric and with a magnetic equator shifted northward with respect to the geographic equator at mid-latitudes of the northern hemisphere (Ness et al., 1974; Ness, 1979; Anderson et al., 2011, 2012; Johnson et al., 2012; Oliveira et al., 2015; Thébault et al., 2018; Wardinski et al., 2019), which is challenging to explain in terms of core structure and dynamics. In addition, several studies of Mercury's interior based on analyses of MESSENGER gravity field measurements and libration data suggested that the top of Mercury's outer core is thermally stratified (Smith et al., 2012; Dumberry & Rivoldini, 2015). Likely, this layer is comprised of FeS, but its phase (liquid or solid) remains uncertain. Thermal stratification implies that the heat flux at the core surface is sub-adiabatic, which has important implications for the inner core solidification and the magnetic field generation.

Numerical dynamo simulations may provide further insight into Mercury's core structure. Possible scenarios include deep-seated dynamos below a thick stable layer (Christensen, 2006; Christensen & Wicht, 2008; Takahashi et al., 2019), thin-shell dynamos (Stanley et al., 2005) and dynamos with a thin stratified layer (Stanley & Mohammadi, 2008).

While numerical dynamos with a stably stratified layer at the top of the shell can explain Mercury's weak magnetic field and its axisymmetry, additional ingredients are needed to explain the northward shift of the magnetic equator. Numerical dynamos with imposed heterogeneous heat flux in the form of equatorial cooling at the outer boundary (Cao et al., 2014; Tian et al., 2015) lead to a convective instability and an offset of the magnetic equator, but their magnetic fields are too energetic and non-axisymmetric. Double diffusive convection phenomena have also been considered to explain Mercury's magnetic field. These phenomena occur when the convection is driven by two sources of buoyancy, i.e. temperature and composition (Manglik et al., 2010). Recently, Takahashi et al. (2019) showed that a double-diffusive convecting shell surrounded by a thick thermally stably stratified layer can generate Mercury-like magnetic fields. Furthermore, numerical dynamo models of Mercury's magnetic field provide estimates of the size of Mercury's inner core. Cao et al. (2014) suggested an inner core radius smaller than 1000 km. Based on geodetic analyses Dumberry and Rivoldini (2015) gave an upper limit on the inner core size of 650 km, with the outer core dynamics partly consisting of snow formation.

These different scenarios of Mercury's dynamo lead to characteristics that should be testable by observations of space-borne magnetometers like MESSENGER and Bepi-Columbo. A careful processing and analysis of magnetic field measurements taken in planetary environments is crucial for the identification of such magnetic field characteristics.

Mainly, two techniques have been applied to study Mercury's magnetic fields: potential field methods such as spherical harmonics (Uno et al., 2009; Wardinski et al., 2019), spherical caps (Thébault et al., 2018) or equivalent source dipoles (Oliveira et al., 2015) that restrict the analysis to those observations obtained in a source free region, and (reduced) parametric models that infer the magnetic dipole moment from the space probe's magnetic equator crossing, i.e. where the radial field B_r is zero, far from the planet (Anderson et al., 2012; Johnson et al., 2012). The latter method provides models with a reduced set of parameters and is popular because of its relative independence of the data distribution. Data used for these reduced parametric models sampled the magnetic field in the magnetospheric region, with a considerable electrical current density that requires additional assumptions about the geometry and distribution of local current systems (Connerney & Ness, 1988). In contrast, Uno et al. (2009) showed by inverting synthetic data from numerical dynamo simulations that a spherical harmonic analysis can recover the

large-scale magnetic field from hemispherical uneven data distribution, as single MESSENGER flybys, when data are taken in a source-free region. The resolution of finer details of the magnetic field needs, off course, numerous orbital tracks.

In this study magnetic field data are used to derive field models that may constrain the internal structure of a planet. The downward continuation of a magnetic field model to the core surface reveals patterns of magnetic flux. In particular, the latitude at which intense flux patches are concentrated may indicate the size of the inner core. Intense flux concentrations near the intersection of the inner core tangent cylinder are prominent in the geomagnetic field for at least the last 400 years (e.g. Jackson et al., 2000) and possibly over the past tens of millennia (see Panovska et al., 2019, and references therein). Numerous studies explored the kinematics as well as the dynamical origin of intense high-latitude flux patches in geomagnetic field models and numerical dynamos (Bloxham et al., 1989; Christensen et al., 1998; Amit et al., 2010, 2011; Peña et al., 2016; Olson et al., 2018). The latitude at which these flux concentrations occur has been related to the change of the dynamical regime at the tangent cylinder that is coaxial with the rotation axis and tangential to the inner core boundary (Gubbins & Bloxham, 1987), while the longitude at which these flux patches occur may be controlled by thermal core-mantle interactions (Bloxham & Gubbins, 1987).

Here we will use inferences from the Earth's core to carefully establish the relation between the latitude of intense magnetic flux patches and the tangent cylinder intersection with the core-mantle boundary (CMB), including possible errors associated with time-dependence and variability from one patch to another. We will then account for the existence of stratification to relate the depth of the stable layer with the radius of the inner core for a given latitude of magnetic flux patches. This relation will be implemented for the case of Mercury's magnetic field.

The aim of this study is twofold: First, we explore to what extent intermediate-scale spatial features of Mercury's magnetic field can be retrieved from the MESSENGER data by applying a spherical harmonic analysis; Second, we aim to infer the internal structure of Mercury's core and the convective state of its dynamo. The paper is organized as follows: The description of the data and their selection is given in section 2, section 3 briefly describes the spherical harmonic modeling method, and results are provided in section 4. Implications for the generation of Mercury's core field and the struc-

ture of its core are discussed in section 5. We summarize our main findings in section 6.

2 Data selection

The MESSENGER spacecraft was in orbit around Mercury from 18 March 2011 to 30 April 2015. The orbit of MESSENGER was highly eccentric, with periapsis ranging from 200 to 500 km over the north polar region, and apoapsides of > 12700 km above the southern hemisphere. This highly eccentric orbit led to an uneven data distribution, where only measurements over the northern hemisphere are assumed to be inside the magnetospheric cavity which allow adequate modeling of Mercury's internal magnetic field (Oliveira et al., 2015). All local times are covered within 88 (terrestrial) days.

Here, we selected data from a satellite altitude range of 300 to 1000 km during local night-time. This provides a data set which shows no crustal magnetic signatures and the least contamination from magnetospheric and exospheric magnetic fields (Wardinski et al., 2019), which are strong at the planet's day-side. The altitude selection criterion guarantees that the analyzed magnetic field measurements are within the magnetospheric cavity: 1000 km is smaller than the averaged subsolar distance of the magnetopause location (Winslow et al., 2013), while the lower limit excludes data from the beginning and the end of the MESSENGER mission. Oliveira et al. (2019) showed that the crustal magnetic signal is small-scale, and weak in amplitude at 40 km altitude. Therefore, at 300 km altitude signals due to crustal magnetization are assumed to be negligible at large length scales.

3 Method

We seek to fit MESSENGER observations of Mercury's magnetic field by a potential that is parameterized using spherical harmonics, i.e.

$$V = a \sum_{l=1}^{L_{\text{int}}} \sum_{m=0}^{l} \left\{ (g_l^m \cos(m\phi) + h_l^m \sin(m\phi)) \left(\frac{a}{r}\right)^{l+1} P_l^m(\cos\theta)) \right\} + a \sum_{l=1}^{L_{\text{ext}}} \sum_{m=0}^{l} \left\{ (q_l^m \cos(m\phi) + s_l^m \sin(m\phi)) \left(\frac{r}{a}\right)^{l} P_l^m(\cos\theta) \right\}, \tag{1}$$

where a is Mercury's radius (2440 km). r is the radial distance from Mercury's center, θ the colatitude and ϕ the longitude. $P_l^m(\cos\theta)$ are the Schmidt semi-normalized associated Legendre functions, where l is the degree and m the order. L_{int} and L_{ext} are the

truncation degrees of the spherical harmonic expansions for the internal and external field, respectively. The Gauss coefficients $\{g_l^m, h_l^m\}$ and $\{q_l^m, s_l^m\}$ represent the internal and external magnetic field, respectively. These model parameters are estimated by a least squares fit to data collected during a given time interval. In the following, we outline details of our modeling technique, which is sometimes called smoothed inversion (Holme & Bloxham, 1996; Uno et al., 2009). The selection of night-time data with altitude less than 1000 km allows a robust separation of external and internal magnetic field sources. For the spherical harmonic expansion, we set $L_{\text{int}} = 10$ and $L_{\text{ext}} = 1$. As stated in Wardinski et al. (2019) external magnetic fields with $L_{\text{ext}} > 1$ cannot be estimated with confidence.

3.1 Model priors

For a linear least squares problem the model vector m containing the Gauss coefficients is found at the minimum of an objective function

$$\Theta(m) = (\mathsf{y} - \mathbf{A}\mathsf{m})^{\mathsf{T}} {\mathbf{C_e}}^{-1} (\mathsf{y} - \mathbf{A}\mathsf{m}) + \lambda_S (\mathsf{m}^{\mathsf{T}} {\mathbf{C_m}}^{-1} \mathsf{m}) \,, \tag{2}$$

where y is the data vector, $\mathbf{A}$ a design matrix, $\mathbf{C_e}$ the data error covariance matrix and $\mathbf{C_m}$ the prior model covariance matrix (Jackson, 1979; Gubbins, 1983) which is controlled by a Lagrange multiplier. The misfit of the model is computed by

$$\hat{\sigma} = \sqrt{\frac{\sum_{i=1}^{N} (y_i - \hat{y}_i)^2}{N-1}} \,, \tag{3}$$

where $\hat{y}_i$ is the model value for given observation y_i.

Our method to find the Gauss coefficients utilizes prior constraints to reduce the ambiguity of the data inversion. The application of priors to constrain the inversion of MESSENGER data to obtain a model of Mercury's magnetic field is justified by their uneven hemispherical distribution. Primarily, the prior should emphasize the large-scales of Mercury's magnetic field. We test the performance of four different priors of the spatial complexity of the model's field morphology. These priors are usually formulated as

model norms:

$$
\begin{aligned}
&\text{Norm 1}: \oint B^2 dS|_{r=c} = (l+1)\left(\frac{a}{c}\right)^{(2l+4)} \\
&\text{Norm 2}: \oint B_r^2 dS|_{r=c} = \frac{(l+1)^2}{2l+1}\left(\frac{a}{c}\right)^{(2l+4)} \\
&\text{Norm 3}: \oint (\nabla_h B_r)^2 dS|_{r=c} = \frac{l(l+1)^3}{2l+1}\left(\frac{a}{c}\right)^{(2l+6)} \\
&\text{Norm 4}: \oint F dS|_{r=c} = \frac{(l+1)(2l+1)(2l+3)}{l}\left(\frac{a}{c}\right)^{(2l+3)} \leq Q.
\end{aligned}
\tag{4}
$$

In Norm 4 of (4) F is the field intensity and Q is the mean CMB heat flux. In all these expressions (4), Mercury's core radius is $c = 2060$ km (Wardinski et al., 2019). Norm 1 minimizes the power of the magnetic field for higher spherical harmonic degrees, and therefore it steepens the slope of its power spectrum. Norms 2 and 3 smooth the radial magnetic field and its horizontal gradient, respectively (Shure et al., 1982). Norm 4 is different from the other norms as it may include prior knowledge of the heat flux at Mercury's core surface, which is due to the Ohmic dissipation of the radial field B_r at the core surface (Gubbins, 1975). However, there are no observations of the heat flux at Mercury currently available. Therefore, Norm 4 acts merely as a constraint to stabilize the solution of the inversion like the other norms. All norms dim the amplitude of small-scale field features, though at different ways, hence support the large-scale morphology of the magnetic field. Among these norms, this effect is most strongly imposed by Norm 3, where the attenuation scales with l^3.

The strength of the prior constraint is controlled by the Lagrange multiplier λ_S. The resulting model is determined by varying the strength of the prior to be in optimal balance between data misfit and model smoothness. This optimal balance is usually found for the λ_S at the knee of their trade-off or L-curves.

3.2 Iterative modeling scheme

To find the model parameters, we adopt an iterative re-weighting scheme that consists of three steps. At a first step, we determine a model that is based on data covering the MESSENGER's entire mission interval at Mercury. Data are weighted equally, to form the initial error covariance matrix, $\mathbf{C_e}$, in (2). We assign an initial error of 1.6 nT to each datum which corresponds to the upper limit of the instrument's resolution (Anderson et al., 2007). At a second step, individual differences between each data and

corresponding values of the initial model are computed, to provide an update of $\mathbf{C_e}$ and, third, to derive the final model with the updated error covariance matrix. The residual amplitude, and therefore $\mathbf{C_e}$, depends directly on the Lagrange multiplier λ_S; In order to obtain a close trade-off curve for each norm, this iterative re-weighting scheme is applied for each setting of λ_S. In total we derive a large number of models for each norm. We select the model at the knee of each norm trade-off curve.

A closer inspection of the residuals reveals anomalous tracks that show significant larger residual amplitudes than others. The cause for these large residuals remains unclear, but could be related to instrument errors and/or data processing errors. However, these data are automatically down-weighted and rejected from the model derivation when the misfit is larger than 2 σ.

3.3 Robustness of the solutions

There are a few diagnostics to evaluate the robustness and confidence of the inversion results. First, we analyze the resolution matrix of the model m, to obtain a measure of model parameter significance. The resolution matrix is given by

$$\mathbf{R} = (\mathbf{A}^\mathsf{T}{\mathbf{C_e}}^{-1}\mathbf{A} + \lambda_s{\mathbf{C_m}}^{-1})^{-1}\mathbf{A}^\mathsf{T}{\mathbf{C_e}}^{-1}\mathbf{A}\,, \tag{5}$$

where the diagonal elements of $\mathbf{C_m}$ are defined in (4). Ideally, this matrix would be an identity matrix. Due to inadequacy of the data, a regularization scheme must be applied in the solving process to obtain a stable solution. This is reflected in the form of the resolution matrix. A value of the resolution near 1 means that a model parameter is wholly determined by the data, whereas a low resolution, i.e. values ~ 0.1, means that the model is mostly controlled by the prior information. The trace of the resolution matrix $Tr(\mathbf{R})$ can be broadly interpreted as the degree of freedom of the model and as the number of model parameters resolved by the inversion (Tarantola, 1987).

Characteristics and diagnostics of the field models are listed in Table 1. All models widely agree in their statistical properties, and mostly differ in their numbers of resolved parameters. The lowest number of resolved parameters is found for Norm 3, as it more strongly damps contributions of higher spherical harmonic degrees than other norms and therefore reduces the degree of freedom most strongly.

Table 1. Inversion parameters, diagnostics and global characteristics of the field models.

	Norm1	Norm 2	Norm 3	Norm 4
λ_s	8.0×10^2	8.0×10^2	4.0×10^2	8.0×10^6
rms misfit (nT)	26.11	26.09	26.5	26.39
Trace of R-Matrix	65	70	36	57
rms field intensity (nT)	331.19	332.75	327.05	335.24
g_1^0 (nT)	-217.5	-218.8	-213.8	-221.5
g_2^0/g_1^0	0.29	0.29	0.31	0.28
dipole tilt angle (°)	0.6	0.4	0.7	0.8

4 Results

In this section, we present models of Mercury's time-averaged magnetic field as they are based on MESSENGER measurements covering the period 2011-2015. We discuss to what extent our results are conclusive and estimate their robustness. The models provide reasonably good fits to the data.

4.1 Resolution analysis and spectral content

For each of the four resulting models we computed the resolution matrix **R**, and charted their diagonal elements, where labels of the models refer to the norm used to constrain the solution, e.g. Norm 1 → Model 1. These plots (resolution curves) are shown in Figure 1.

The resolution curves of all models generally agree for the first four spherical harmonic degrees. Most notable are the high resolution of sectorial Gauss coefficients, i.e. g_m^m, h_m^m, of at least the first five spherical harmonic degrees. Resolution curves of models 1, 2 and 4 show this particular pattern also for higher spherical harmonic degrees, which may indicate a higher ability of these norms to capture small-scale magnetic field signatures. The higher resolution of the sectorial terms can be explained by MESSENGER's flight path along latitude. We find that Model 3 resolves magnetic field structures only until spherical harmonic degree 4. The other models show resolution up to spher-

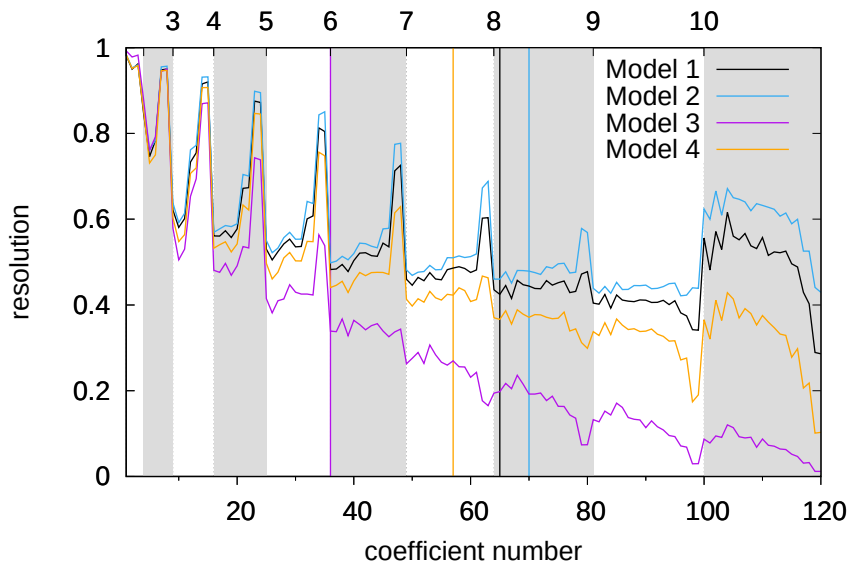

Figure 1. Diagonal elements of the resolution matrix of the preferred models for different priors vs. coefficient number (see also degree at the top axis). Gray shaded areas indicate even spherical harmonic degrees. The colored vertical lines represent the degree of freedom of the respective model.

ical harmonic degrees 6 (Model 4) and 7 (Models 1 and 2). For degrees 8 and 9 none of the models show resolution larger than 0.5. Below this level the model is dominated by the prior. At degree 10, i.e. coefficient numbers between 100 and 120, Models 1, 2 and 4 show enhanced resolution, where they may become sensitive to spectral leakage, signals of other sources and possible data errors. We assume the high resolution at these small scales to be an artifact and possibly caused by the orbital geometry of MESSENGER. Holme and Bloxham (1996) discussed a similar effect observed in the Voyager II data at Neptune, which was likely caused by the spacecraft trajectory. The truncation of the spherical harmonic expansion leads also to an aliasing of the higher degree field ($l > l_{\mathrm{int}}$) into coefficients of the truncated spherical harmonic expansion (spectral leakage). This effect is significantly reduced in Model 4, and therefore, we favor Model 4 as an optimal representation of Mercury's core field up to spherical harmonic degree $l < 9$.

Maps derived from truncated models ($l < 9$) of the radial magnetic field at the core surface are shown in Figure 2. As expected field structures in the northern hemisphere show more details than in the southern hemisphere, because of the data distri-

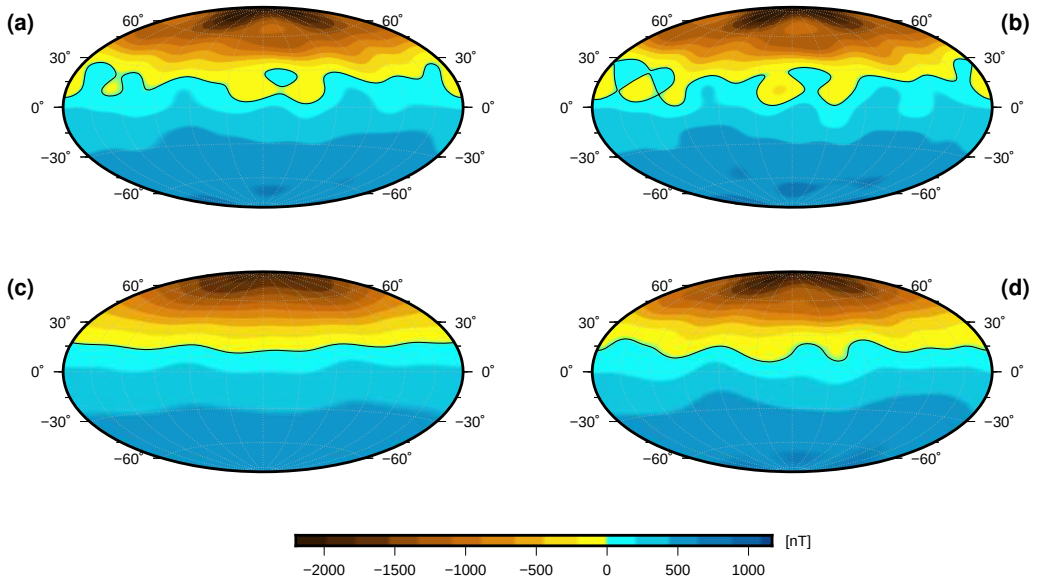

Figure 2. Radial component of the magnetic field at Mercury's core surface of the selected model solutions: (a) Model 1, (b) Model 2, (c) Model 3 and (d) Model 4.

bution. Generally, the field is dominated by the axial dipole, but the magnetic equator is significantly shifted towards the North pole in agreement with previous studies (Anderson et al., 2011, 2012; Thébault et al., 2018). The different models show differing spatial complexities, in particular of the magnetic equator. The map derived with Norm 3 shows the most axisymmetric field morphology, whereas models derived with Norms 1 and 2 show more longitude-dependent structures including even some reversed flux patches. Overall, all models tend to agree in their large-scale structure (Table 1) and differ in their quantification of small scale features.

All models (1 - 4) show axial quadrupole-dipole ratios of 0.28-0.31 (Table 1) which are significantly smaller than those obtained by dipole offset models (Anderson et al., 2012; Johnson et al., 2012) but are in agreement with a model constructed using spherical caps (Thébault et al., 2018). We note that we could force the models to have a larger quadrupole-dipole ratio close to $g_2^0/g_1^0 = 0.4$; however, this leads to 10 - 20% larger rms misfits, which we consider to be significant and eventually deleterious for a large quadrupole-dipole ratio.

Maps in Figure 2 have also structures where no data are available, i.e. in the southern hemisphere. The magnetic field morphology in this hemisphere is mostly determined

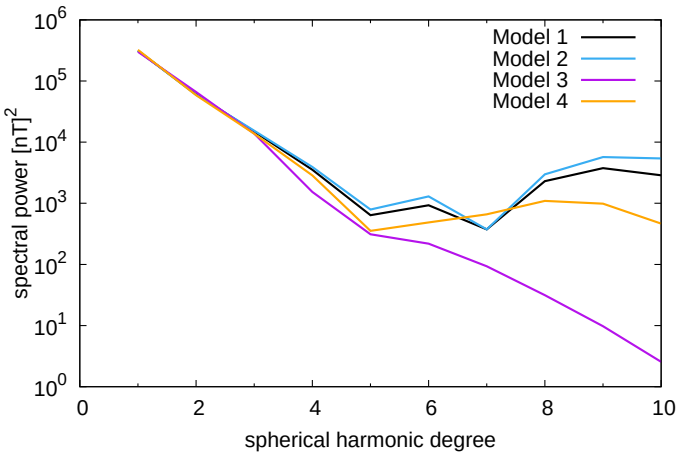

Figure 3. Power spectra of the four magnetic field models.

by the global characteristic of the spherical harmonic analysis and the prior used in the inversion. We, therefore do not attempt to interpret magnetic field features in the southern hemisphere.

Power spectra (Lowes, 1966; Mauersberger, 1956) of the models at the core surface are shown in Figure 3. The spectra mostly match for spherical harmonic degrees 1 to 3. We find three different types of spectral slopes for spherical harmonic degrees $l >$ 5: decreasing, increasing and flat. The spectral power of Model 3 drops linearly, whereas Models 1 and 2 show powers that increase by one order of magnitude. Model 4 shows a flatter spectrum. This may lead to similar conclusions as taken from the resolution analysis, where for Models 1, 2 and 4 spherical harmonic degrees above $l > 8$ may be influenced by spectral leakage of magnetic small-scale sources close to the surface of Mercury.

The discussion of the spatial characteristic of Mercury's steady magnetic field will therefore be based on Model 4 which is neither too damped (as Model 3) nor contaminated by spectral leakage (as possibly Models 1 and 2).

4.2 Mercury's time-averaged magnetic field

Maps in Figure 4 are derived from our preferred Model 4 until spherical harmonic degree 8. Figures 4a and b show the non-dipole field and the non-axisymmetric, i.e. non-zonal, field at Mercury's core surface, respectively. The mapping of the non-dipole field

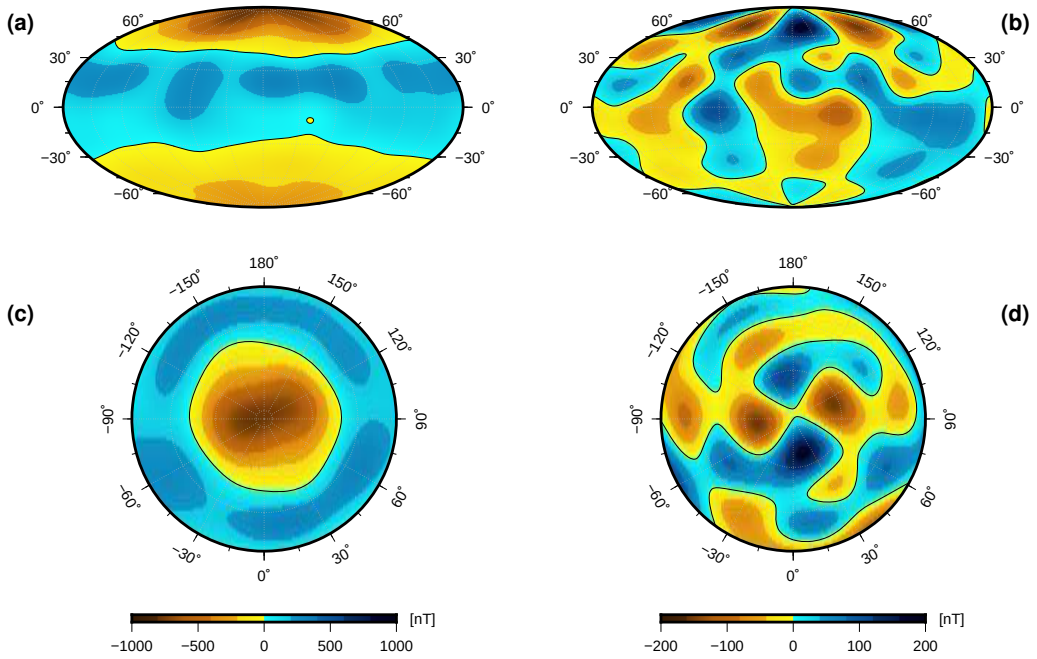

Figure 4. Radial component of: (a) the non-dipole and (b) the non-axisymmetric (non-zonal) magnetic field at Mercury's core surface, respectively. (c) and (d) show north polar views of these magnetic field parts. Maps are derived using Model 4 up to spherical harmonic degree $l = 8$. The black lines mark the zero contour. Note different scales for maps (a), (c) and (b), (d).

excludes the dipole coefficients g_1^0, g_1^1 and h_1^1, whereas the non-axisymmetric field excludes all zonal terms, i.e. g_l^0. The non-dipole field (Figure 4a) is dominated by the equatorial-symmetric g_2^0 term. Though the estimate of g_2^0 is strongly influenced by the uneven distribution of MESSENGER data, it is the second strongest coefficient of the field. In addition, the field features at the northern hemisphere are stronger due to significant equatorial-antisymmetric terms, i.e. g_3^0. Finally, the signature of two flux patches at northern high latitudes is evident in Figure 4b.

The polar view map of the non-dipole radial field at the surface of Mercury's core (Figure 4c) shows an elongated patch of intense magnetic flux over the North pole. This pattern is surrounded by a region of positive (i.e. opposite polarity) magnetic flux with some intensified patterns, where the boundary between these regions of opposite polarity, i.e. the magnetic equator (black line) shows considerable undulations. These undulations further indicate non-axisymmetric field contributions.

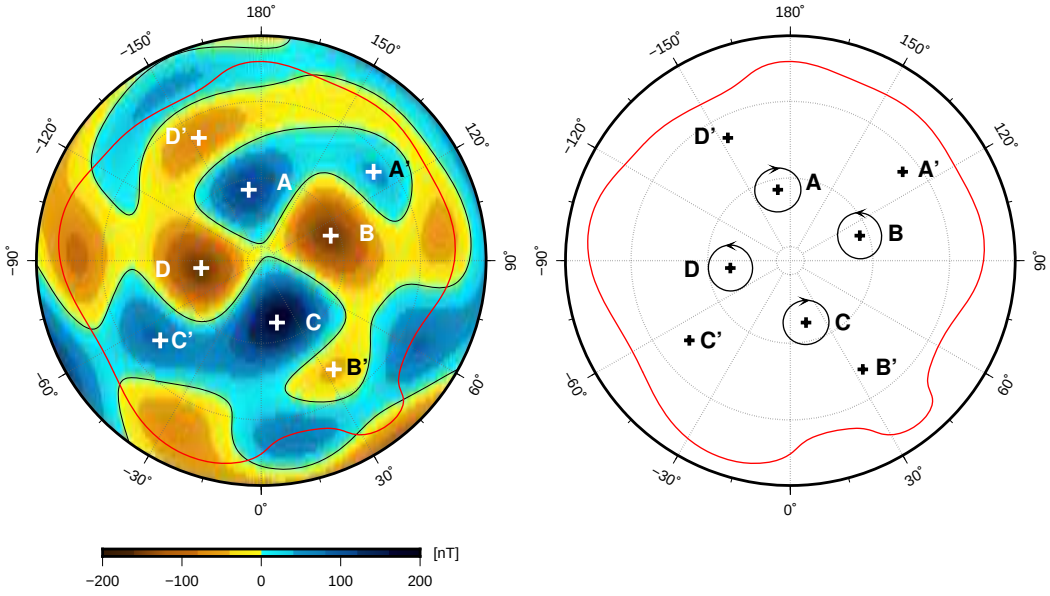

Figure 5. Polar view of the non-axisymmetric radial magnetic field at Mercury's core surface. The red line shows the position of the magnetic equator, capital letters mark apparent non-zonal field features and pluses their centers. Right: a schematic illustration of the individual convective rolls associated with the high-latitude non-zonal field features (clockwise A, C; counterclockwise B, D).

The non-zonal field, shown in Figures 4b and d, is fainter. Its amplitude ranges between ± 200 nT, corresponding to ∼ 10% of the total field. This part of the field allows unraveling longitude-dependent structures that are otherwise masked by the strong axisymmetric field. Particularly, the non-zonal field shows four features with alternating signs at high latitudes (A, B, C & D in Figure 5), indicative of two intense normal flux patches. The centers of these flux patches appear approximately at 65° northern latitude.

Finally, Mercury's core field also shows non-zonal structures at lower latitudes. These primed features (A', B', C' & D' in Figure 5) are weaker than their higher latitude counterparts. Moreover, the primed features do not correspond to any radial field structure of a certain polarity. The primed features seem to be shifted relatively to the higher latitude structures by a longitudinal angle of 30° to 60° to the west.

4.3 Inferring Mercury's internal structure

The concentric arrangement of non-zonal features (A, B, C & D) in the northern hemisphere as seen in Figure 5 could be indicative of processes that are involved in the magnetic field generation. We assume that the nature of these features are linked to columnar rolls tangent to the inner core and parallel to the planet's spin axis. Busse (1975) showed that such columnar flow exists when the Coriolis force dominates viscous and Lorentz forces in the convective region. Oppositely rotating convective rolls (clockwise and anticlockwise, see Figure 1 of Busse, 1975) may explain the different signs of the non-zonal magnetic field structures. Cyclones/anti-cyclones in the northern hemisphere correlate with convergence/divergence and concentrated/dispersed field, respectively (e.g. Olson et al., 1999)). Accordingly, in Figure 5 the flux patches B & D may be concentrated by fluid downwellings associated with cyclones, while the positive non-zonal field (i.e. relatively weak field) in A & C may be dispersed by fluid upwellings associated with anti-cyclones.

We interpret the latitude of these flux patches by comparing to Earth's magnetic core field. Amit et al. (2011) quantitatively identified centers of geomagnetic intense flux patches. Their Figure 9 and our Figure A.1 suggest that patch centers appear persistently at latitudes somewhat lower than that of the tangent cylinder. Analysis of the *gufm1* historical geomagnetic field model (Jackson et al., 2000) reveals that patch latitudes are time-dependent, appearing from about 30° latitude lower than the tangent cylinder until very close to it. However, in recent epochs when the field models are more reliable the patches reside less than ∼10° lower than the tangent cylinder (Amit et al., 2011). This agrees with our analysis of a recent IGRF model (Thébault et al., 2015). The latitude of the geomagnetic flux patches based on Figure A.1 is approximately 8° lower than that of the tangent cylinder. We conclude that based on the behavior of the geomagnetic field the offset between the patches and the actual latitude where the tangent cylinder intersects the CMB is roughly $\delta\theta \sim 10^\circ \pm 10^\circ$.

Figure 6 (top) illustrates the classical tangent cylinder geometry with the addition of the effect of $\delta\theta$. This geometry is written as

$$\sin(\theta_{cmb} - \delta\theta) = \frac{r_i}{r_o}\,, \tag{6}$$

where r_i and r_o are the radii of the inner core and the CMB respectively. We assume that θ_{cmb} can be obtained from Mercury's non-zonal field and that $\delta\theta$ is similar to Earth's

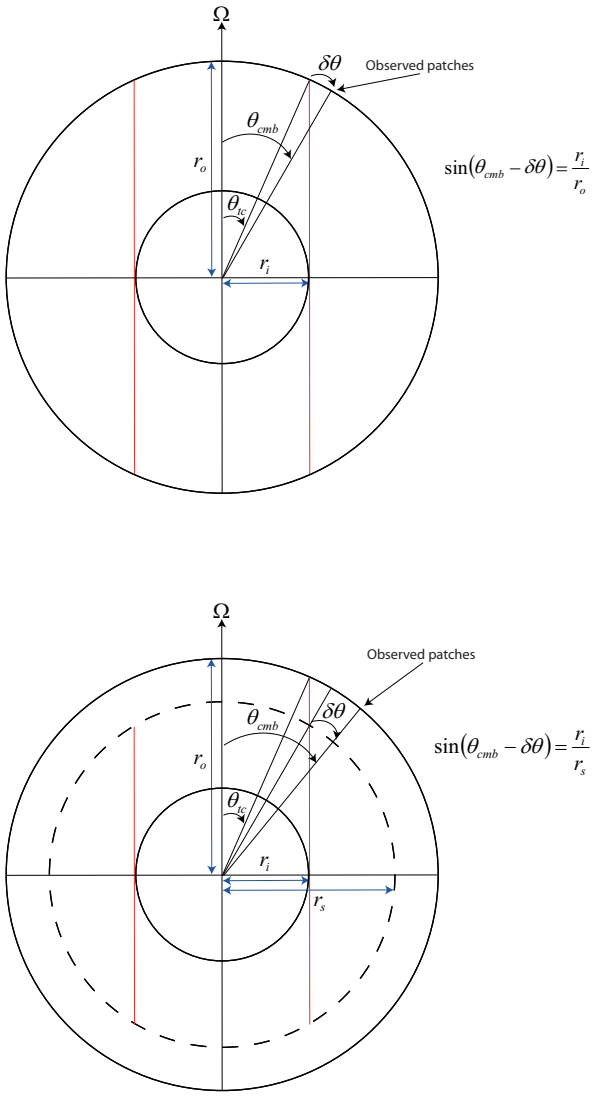

Figure 6. Schematic illustrations of the geometry of the tangent cylinder effect without (top) and with (bottom) a stably stratified layer. See text for the definitions of different angles.

value. This allows to derive r_i, Mercury's inner core size. However, the presence of a stratified layer at the top of the core complicates this inference. When such a layer exists, the convective rolls concentrate flux at the base of the stratified layer, from which the skin effect carries the signal to the CMB by diffusion. Assuming that the signal propagation across the stratified layer is roughly radial, then Figure 6 (bottom) illustrates the relation between the co-latitude of the patches θ_{cmb}, the radius of the inner core r_i and the radius of the base of the stratified layer r_s. Mathematically this relation is

$$\sin(\theta_{cmb} - \delta\theta) = \frac{r_i}{r_s}\,, \tag{7}$$

which contains two unknowns, r_i and r_s, and therefore cannot be uniquely determined. However, it provides a useful constraint and may be used to highlight various plausible scenarios for Mercury's internal structure.

To estimate Mercury's inner core size, we first estimate θ_{cmb} from Mercury's magnetic field model. The centers of intense flux patches B & D (Figure 5) reside at about latitude ∼65° North, or co-latitude $\theta_{cmb} = 25°$. From the analysis of the geomagnetic field we further assume $\delta\theta = 10° \pm 10°$. Substituting these values into (7) gives scenarios for Mercury's internal structure. Figure 7a presents the results for Mercury's inner core size r_i and the thickness of the convective region is given in Figure 7b. Both are functions of the radius of the base of the stratified layer r_s, for three values of $\delta\theta$ which cover the considered range. Small values of r_s, which correspond to a very deep base of the layer (thick layer), give a very small inner core which would render the identification of a tangent cylinder effect to be impossible. Moreover, if most of the core is stratified, a dynamo action is unlikely. Larger values of r_s, which correspond to a thinner stratified layer, give a thicker inner core with stronger dependence on $\delta\theta$. For a thin stratified layer of ∼50 km, with $\delta\theta = 0°$ we find an upper bound r_i ∼850 km and a convective region of 1160 km, with $\delta\theta = 10°$ we find r_i ∼500 km and a convective region of 1490 km, whereas with $\delta\theta = 20°$ r_i is ∼180 km (unlikely to be magnetically detectable) and a convective region of ∼1830 km. On the other hand, with a thick stratified layer of ∼1600 km for all $\delta\theta$ the inner core size is smaller than 200 km and the respective sizes of the active dynamo region are less than 400 km.

In the discussion section we elaborate on the consequences of the latitude of the magnetic flux patches on inferring the internal structure of Mercury.

5 Discussion

Figure 1 can directly be compared to results of a resolution analysis by Uno et al. (2009). The resolution of our preferred model is certainly higher than the resolution of their inversion results. This is mainly because of the wider spatial coverage during the MESSENGER main mission (2011 - 2015) than during the three flybys of Mariner-10 and the one MESSENGER flyby in 2008. However, Uno et al. (2009) concluded that a realistic resolution up to spherical harmonic degree 10 can be obtained from the flyby data. We consider this as an optimistic view, as it (implicitly) assumes that model pa-

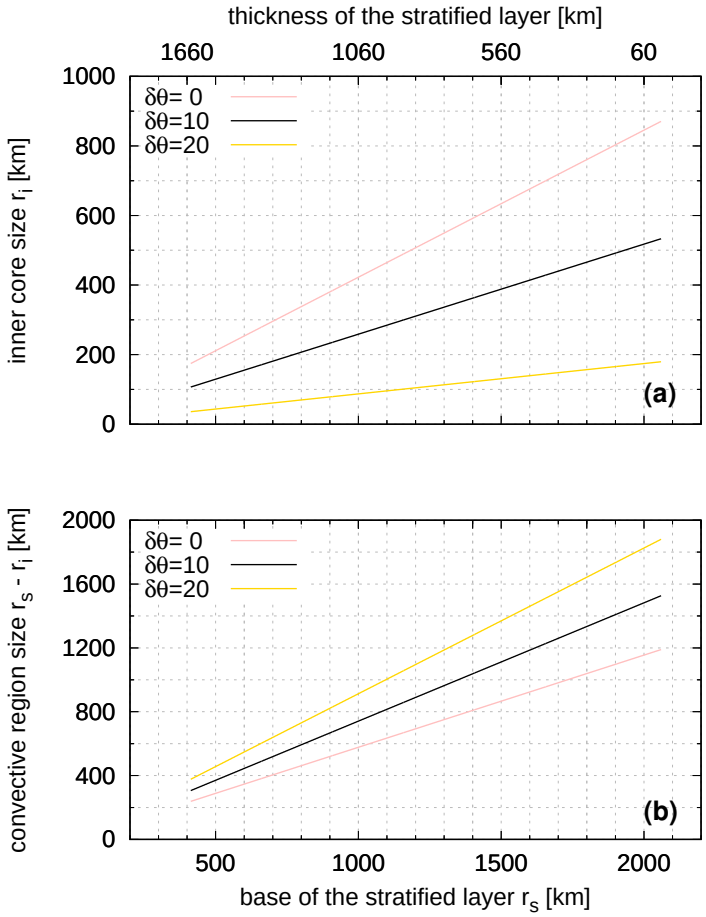

Figure 7. Mercury's inner core size r_i (a) and the thickness of the convective region (b) vs. the radius of the base of the stratified layer r_s (or the layer thickness, see top horizontal scale), for three values of $\delta\theta$ (see legend).

rameters with a small but non-zero resolution can be resolved by the inversion. In this respect, we are cautious in choosing a minimum resolution R_{min} which would be relevant for robust results. We find that a value of $R_{min} \geq 0.4$ is a diligent choice for a required minimum resolution. The model solutions 1, 2 and 4 largely meet this criterion, and maps of these models are in good agreement when truncated to spherical harmonic degree $l < 9$. However, we focus on magnetic field Model 4 in the following, because Models 1 and 2 tend to show small-scale structures along the magnetic equator that arise from spherical harmonic degrees $l > 8$ which we consider uncertain.

Our analysis reveals features of Mercury's magnetic core field that could provide insights to characterize the planet's internal structure and the dynamo action in its core. The morphology of Mercury's non-axisymmetric magnetic field that is shown in Figures 4b and d resembles (perhaps incidentally) the geomagnetic field in the form of two high-latitude normal flux patches (e.g. Gubbins, 2003; Jackson et al., 2000). The axisymmetric and non-axisymmetric parts of Mercury's magnetic field may be due to different processes. In this context it has been proposed that a stratified layer outside the dynamo region of Saturn leads to the axisymmetrization of its magnetic field (Stevenson, 1982; Stanley, 2010). Similar mechanisms are likely to be at work inside Mercury (Christensen, 2006; Christensen & Wicht, 2008).

Mercury's internal structure is still unresolved by geodetic analyses and there is a debate concerning the existence and possible size of a solid inner core. If a solid inner core exists, it was argued that its radius is likely to be smaller than ∼1000 km (Van Hoolst et al., 2012; Cao et al., 2014; Dumberry & Rivoldini, 2015; Peale et al., 2016). Based on estimates of Mercury's gravity field, tidal Love number and pole coordinates, Mercury's inner core radius is in the range 883 to 1026 km (Genova et al., 2019). However, reported values of Mercury's inner core size are still under debate and estimates derived from a geodetic analysis of Mercury's orbital motion give a larger range of 370-1200 km (from combining the first and third quartiles of Margot et al., 2018).

Based on the above estimates from geodetic analyses we consider Mercury's inner core size to be r_i =500-1000 km. For r_i =500 km and $\delta\theta = 0°$ Figure 7(a) gives a stratified layer thickness of ∼880 km which leaves ∼680 km for the convective region to maintain a dynamo. For $r_i = 500$ km and $\delta\theta = 10°$ the stratified layer thickness is ∼130 km and the convective region is ∼1430 km, while for $r_i = 500$ km and $\delta\theta = 20°$ a so-

lution does not exist. Furthermore, an inner core size of r_i =1000 km is out of range for the considered $\delta\theta$ values (Figure 7(a)). Because the large scale field of Mercury favors a substantial stratified layer, and because large r_i constrains $\delta\theta$ to small admissible values, we conclude that the inner core size tends towards the small end of the considered r_i range.

The thickness of the stratified layer at the top of Mercury's core is also unknown. Smith et al. (2012) suggested that a 200 km thick and solid FeS-layer at the interface of a silicate mantle and the metallic core may explain the planet's moment of inertia. However, this setup was questioned by Hauck et al. (2013) who derived models without an FeS-layer to reproduce the gravity field observations and libration data. The thickness of such a layer depends on the available Sulfur and its solubility in the metallic core determined by the widely unknown core temperature and reduction conditions (Hauck et al., 2013). In most numerical dynamo simulations that attempt to explain observations of Mercury's magnetic field a thick layer is assumed, from several hundred km (e.g. 600 km in Christensen, 2006; Christensen & Wicht, 2008) up to half the core radius (Takahashi et al., 2019). The stratified layer weakens and diffuses the non-axisymmetric field via a skin effect, which could explain its low intensity and dominant axisymmetry.

Considering a stratified layer thickness of 500-1000 km (or r_s =1560-1060 km), we obtain r_i ∼660-90 km and a dynamo region of ∼1420-610 km, respectively with ranges corresponding to the different $\delta\theta$ values (Figure 7). The small inner core scenario (with $\delta\theta = 20°$) seems unlikely to produce a detectable tangent cylinder effect. We therefore favor again the solutions for low $\delta\theta$ which correspond here to inner core sizes of ∼660-450 km and convective region sizes of approximately 900-610 km.

6 Conclusion

In this study, we investigate the morphology of Mercury's magnetic core field and the smallest possible spatial scales that can be resolved from the MESSENGER measurements. Our spherical harmonic analysis demonstrates that features of the time-averaged magnetic core field of spherical harmonic degree $l = 8$ can be robustly resolved, independent of the model prior. Higher spherical harmonic degrees are likely aliased by undetermined magnetic signatures. Moreover, we detect non-axisymmetric features of the

core magnetic field that are absent in the dipole offset model (Anderson et al., 2012; Johnson et al., 2012).

For the first time, Mercury's non-axisymmetric core field is identified and studied to infer the internal structure of its core. We find non-axisymmetric flux patches at high northern latitudes. We interpret these features as the signature of convective columns adjacent to the inner core tangent cylinder. The deviation from axisymmetry introduced by these patches is far less pronounced than at Earth's geomagnetic field due to the masking by Mercury's dominant axisymmetric field.

We take advantage of the mean latitude of these two patches to constrain Mercury's internal structure. We establish a relation between the inner core size and the thickness of the stratified layer below the CMB as a function of the latitude of the magnetic flux patches. While various combinations of these two quantities are possible, a combined interpretation of our results and those from geodetic analyses limits the range of the inner core radius to ∼500-660 km. Accordingly the stratified layer thickness is ∼880-500 km, leaving ∼900-610 km for the convective dynamo region, respectively. Furthermore, our results favor little (if any) shift between the locations of magnetic flux patches and the tangent cylinder at the top of the dynamo region, in apparent contrast to the offset observed at Earth's core.

Finally we emphasize that our analysis is based on a data set of the MESSENGER mission over the northern hemisphere only. This puts limits on the magnetic field models and the inferences concerning Mercury's internal structure. The future Bepi-Colombo mission will unravel these details of Mercury's magnetic core field.

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The authors declare that they have no competing interests.

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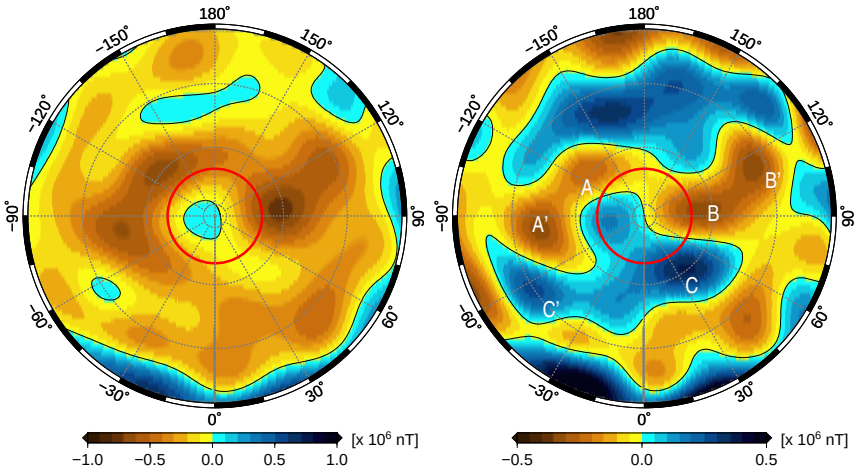

Figure A.1. North polar views of the radial magnetic field component (left) and its non-axisymetric part (right) at Earth's core surface. The red circles represent the diameter of Earth's inner core.

A Earth's core field

Figure A.1 shows the radial geomagnetic field component and its non-axisymetric part at Earth's core surface in the year 2015. The maps are based on the 12$^{\text{th}}$International geomagnetic reference field (Thébault et al., 2015). The model was truncated at spherical harmonic degree $l = 10$. The maps show also the projection of the inner core tangent cylinder on the CMB.