

# Investigating Recent Changes in MJO Precipitation and Circulation in Multiple Reanalyses

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## Key Points:

- Non-monotonic changes in MJO circulation and precipitation amplitude over the period of 1981-2018 are found in ERA5 and MERRA-2.
- A decrease in the ratio of MJO circulation to precipitation amplitudes is detected and can be explained by weak-temperature-gradient theory.
- Examination of ERA-20C during 1901-2009 demonstrates similar ratio decreases before the satellite era.

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**Abstract**

Recent work using CMIP5 models under RCP8.5 suggests that individual multimodel-mean changes in precipitation and wind variability associated with the Madden-Julian oscillation (MJO) are not detectable until the end of the 21st century. However, a decrease in the ratio of MJO circulation to precipitation anomaly amplitude is detectable as early as 2021-2040, consistent with an increase in dry static stability as predicted by weak-temperature-gradient balance. Here, we examine MJO activity in multiple reanalyses (ERA5, MERRA-2, and ERA-20C) and find that MJO wind and precipitation anomaly amplitudes have a complicated time evolution over the record. However, a decrease in the ratio of MJO circulation to precipitation anomaly amplitude is detected over the observational period, consistent with the change in dry static stability. These results suggest that weak-temperature-gradient theory may be able to help explain changes in MJO activity in recent decades.

**Plain Language Summary**

A recent study examined future projected changes in precipitation and wind strength associated with the Madden-Julian oscillation (MJO) in a set of anthropogenically-forced warming simulations. While they showed that changes in the amplitude of individual MJO-related variables are not detectable until the end of the 21st century, they also demonstrated that a decrease in the ratio of MJO wind to precipitation anomaly amplitude is detectable as early as 2021-2040. To examine whether these MJO changes found in climate models are realistic, changes to MJO variability are assessed in three observational products, and we find that a similar decrease in the ratio of MJO wind to precipitation strength is detectable over 1901-2018. The change in MJO activity is consistent with that expected under climate warming.

**1 Introduction**

The Madden-Julian oscillation (MJO; Madden & Julian, 1971, 1972) is the dominant mode of large-scale tropical precipitation variability on intraseasonal timescales. MJO activity impacts the occurrence of extreme weather events not only in tropics, but also at higher latitudes due to its remote teleconnections (Zhang, 2013). Because of its ability to modulate weather across the globe, with clear implications for lives and property, extensive research is being conducted about the MJO, with increasing attention given to the evolution of the MJO under anthropogenic warming (Maloney et al., 2019). As global temperatures rise, MJO activity is expected to be impacted by competing effects, making the projections of the MJO difficult. For example, an increased basic state vertical moisture gradient in the lower troposphere increases the efficiency with which vertical motion moistens the atmosphere, leading to a strengthening of MJO-associated convection (Arnold et al., 2013; Holloway & Neelin, 2009). In contrast, an increased dry static stability decreases the efficiency by which diabatic heating induces vertical motion (Knutson & Manabe, 1995; Sherwood & Nishant, 2015; Sobel & Bretherton, 2000), which would tend to weaken MJO-associated convection (e.g. Chikira, 2014). Future projections from most global climate models (GCMs) suggest an increase in the amplitude of MJO precipitation under anthropogenic warming, although MJO circulation anomalies weaken, or at least increase less than precipitation (Maloney et al., 2019). Analysis of the reconstructed historical record from instrumental observations and reanalysis shows positive trends of MJO amplitude over the 20th century in surface pressure and precipitation (Oliver & Thompson, 2012) and in the late 20th century in zonal winds (Jones & Carvalho, 2006; Slingo et al., 1999). However, other studies have found no trend in boreal-wintertime MJO amplitude from the 1980s to the 2000s when using an outgoing longwave radiation-related metric (Tao et al., 2015).

Recent evidence suggests that the MJO may undergo structural changes with warming and differences in intensification rate in its associated precipitation and circulation components. Such changes would be important because teleconnections generated by upper-level divergence associated with MJO convection have a large impact on extratropical weather and its predictability (Ferranti et al., 1990; Zhang, 2013). Instead of examining the amplitude of the MJO with a single variable, Maloney and Xie (2013) and Wolding and Maloney (2015) suggest that in the deep tropics where the weak-temperature-gradient (WTG) approximation holds (Sobel & Bretherton, 2000), the amplitude ratio of vertical velocity to precipitation associated with the MJO is constrained by dry static stability. Since the temperature profile in the free tropical troposphere roughly follows a moist adiabat determined by convective adjustment in tropical convecting regions (Knutson & Manabe, 1995), the dry static stability profile may be constrained by future SST warming, thus providing a constraint on future MJO behavior.

A recent study found that the ratio of MJO-associated circulation to precipitation amplitude follows WTG balance in anthropogenic warming simulations (Bui & Maloney, 2019). The WTG approximation can be applied to the thermodynamic equation to produce the following approximate balance in the tropical free troposphere, where horizontal temperature gradients are small (Sobel & Bretherton, 2000),

$$\omega \frac{\partial s}{\partial p} \approx Q_1 \quad (1)$$

where  $\omega$  is the vertical pressure velocity,  $s$  the dry static energy (DSE), and  $Q_1$  the apparent heat source (Yanai et al., 1973). Note that all variables represent the large-scale area average. If it is further assumed that precipitation is proportional to  $Q_1$  in MJO convective regions, and that the vertical structure of  $Q_1$  is not changed (Maloney & Xie, 2013), it follows that at a given level:

$$\Delta \left( \frac{\omega}{P} \right) \propto \Delta \left( \frac{\partial s}{\partial p}^{-1} \right) \quad (2)$$

where  $P$  is the surface precipitation rate, and  $\Delta$  denotes the relative change from a reference state to a new state. Bui and Maloney (2019) examined GCM simulations forced by Representative Concentration Pathway 8.5 (RCP8.5) in a subset of models participating in the Coupled Model Intercomparison Project 5 (CMIP5) that simulated realistic MJOs. While the amplitude changes of MJO precipitation and vertical velocity were individually not detectable until 2080, the *ratio* of MJO vertical velocity to precipitation amplitude showed detectable decreases as early as 2021-2040. Consistent with WTG balance and the proportionality of precipitation to  $Q_1$ , the ratio of MJO vertical velocity to precipitation amplitude matches the change in dry static stability in the simulations, implying that this theory could explain and predict the evolution of the MJO, even in the observational record that has exhibited warming.

Following this work, we investigate the temporal evolution of MJO-related precipitation and circulation amplitude and their ratio in two reanalyses (ERA5 and MERRA-2) to assess whether changes to the MJO can be detected in recent decades. A similar analysis is also applied on a century-long reanalysis (ERA-20C) to further support findings over the past few decades, and to assess recent changes to the MJO in the context of low-frequency variability. Our purpose is to determine whether WTG balance can explain changes in MJO activity in the real world, which could help support projections of MJO under continued anthropogenic warming.

## 2 Data and Methodology

Two reanalysis datasets spanning 1981-2018 are employed to assess changes in MJO amplitude and the background environment in recent decades. The Modern-Era Retrospective analysis for Research and Applications version 2 (MERRA-2; Gelaro et al., 2017)

109 and the European Centre for Medium-Range Weather Forecasts (ECMWF) re-analysis  
 110 (ERA5; Hersbach et al., 2020) are the main datasets used to investigate MJO activity  
 111 in recent decades. The ECMWF twentieth century reanalysis (ERA-20C; Poli et al., 2016)  
 112 is used to evaluate long term changes in MJO behavior over 1901-2009. The MERRA-  
 113 2, ERA5, and ERA-20C datasets have spatial (temporal) resolutions of  $0.5^\circ \times 0.625^\circ$   
 114 (three hours),  $0.25^\circ \times 0.25^\circ$  (one hour), and spectral truncation of T159 (one hour), re-  
 115 spectively. For the purpose of investigating large-scale dynamics, all variables are re-gridded  
 116 to have a common horizontal spatial resolution of  $2.5^\circ \times 2.5^\circ$ . Vertical pressure veloc-  
 117 ity and precipitation are averaged into daily means, and temperature and DSE are orig-  
 118 inally obtained as monthly means. Wolding and Maloney (2015) imply that to good ap-  
 119 proximation the slowly varying background DSE gradient is appropriate to use in equa-  
 120 tion (1) for determining the dominant WTG MJO balance. While the precipitation data  
 121 in both reanalyses is model-generated and comes with substantial caveats, inhomogeneities  
 122 in satellite-observed precipitation over the tropics make it difficult to use to detect cli-  
 123 mate trends (e.g. Yin et al., 2004). Furthermore, the moisture budget in the reanaly-  
 124 ses products is more internally consistent, and thus, we focus on reanalysis precipitation  
 125 for this work.

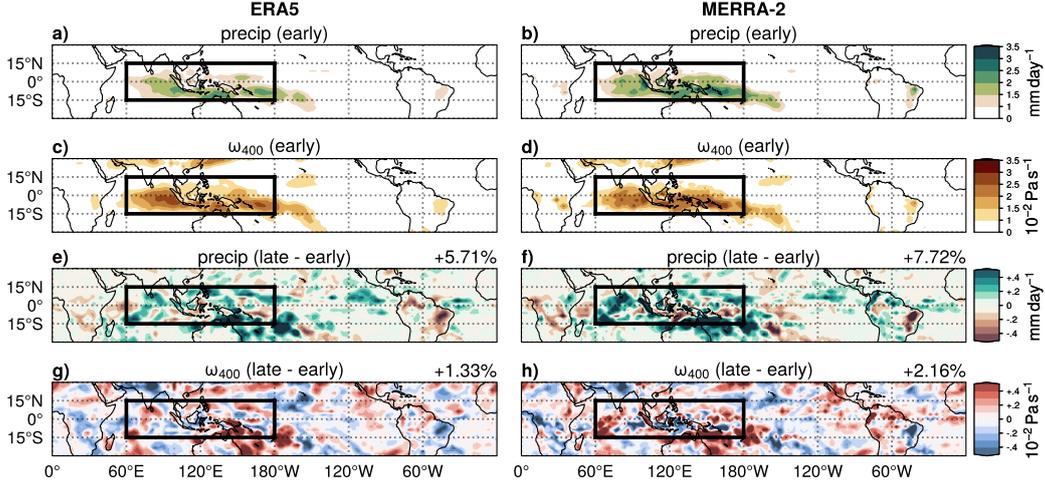
126 For ERA5 and MERRA-2, MJO activity is assessed by its associated precipitation  
 127 and vertical pressure velocity amplitudes, with vertical pressure velocity at 400 hPa ( $\omega_{400}$ )  
 128 used given the top-heavy nature of convection in the MJO (Kiladis et al., 2005). Specif-  
 129 ically, the occurrence of an MJO event is defined as when the magnitude of the outgoing-  
 130 longwave-radiation-based MJO index (OMI; downloaded from NOAA PSL website; see  
 131 Kiladis et al., 2014, for definition) exceeds 1.0. Note that we split our analysis into 19-  
 132 year periods, and so OMI is normalized within each time period (as in Bui & Maloney,  
 133 2019) to reflect possible changes in variance of outgoing longwave radiation fields. Bo-  
 134 real winter (November to April) MJO composites for each of its eight phases are then  
 135 generated for 30-90 day bandpass filtered variables as is commonly done in the MJO lit-  
 136 erature (e.g. Kiladis et al., 2014). Amplitudes of MJO precipitation and  $\omega_{400}$  for each  
 137 location are calculated as the root-mean-square values across the composites of the eight  
 138 MJO phases.

139 Since OMI is defined by satellite OLR fields that are not available prior to 1979,  
 140 MJO activity in ERA-20C is assessed using the standard deviations of precipitation and  
 141  $\omega_{400}$  in the MJO band. The MJO band is defined by bandpass filtering fields to frequen-  
 142 cies of 30-90 days and zonal wavenumbers of 1-5.

143 Boreal winter averages derived from monthly means of temperature and DSE are  
 144 used to assess the background environment changes that could impact MJO activity. Dry  
 145 static stability at 400 hPa is computed using the vertical gradient of DSE between 350  
 146 hPa and 450 hPa.

147 Our focus is on the time evolution of the amplitudes of MJO precipitation and  $\omega_{400}$   
 148 in the Indo-Pacific warm pool region (the IPWP region;  $15^\circ\text{S}-15^\circ\text{N}$ ,  $60^\circ\text{E}-180^\circ$ ) where  
 149 the MJO is most active, as shown in the boxed region in Figure 1. Area-averaged MJO  
 150 precipitation and  $\omega_{400}$  amplitudes over the IPWP region are used as metrics to quan-  
 151 tify overall MJO activity.

152 Composites obtained from 19-year running windows are extensively used in this  
 153 study, similar to the averaging window length of 20 years used in Bui and Maloney (2019).  
 154 This window length is chosen to reduce noise from decadal variations, but also to retain  
 155 enough data points to show the time evolution of MJO activity. Since the entire time  
 156 period analyzed is 38 years in ERA5 and MERRA-2, the first and the last 19 years of  
 157 the record are the only two periods that are truly independent, and we refer to these as  
 158 the *early period* (1981-1999) and the *late period* (2000-2018). The conclusions in this study  
 159 are not sensitive to the choice of window length used between 15 years and 25 years (Fig-  
 160 ure S1).



**Figure 1.** The boreal winter composite amplitudes of (a, b) MJO precipitation and (c, d) MJO  $\omega_{400}$  during the early period (1981-1999), and (e-h) their difference from the late period (2000-2018), from (left column) ERA5 and (right column) MERRA-2. The black rectangle encloses the Indo-Pacific warm pool region, and the percentage values shown in the upper right corners of (e-h) are the area-averaged relative changes over the region.

Relative change ( $\Delta$ ) in percent is the main metric used to define changes in this study. Specifically, for any quantity  $X$ , the relative change compared to its reference state ( $X_{ref}$ ) is defined by:

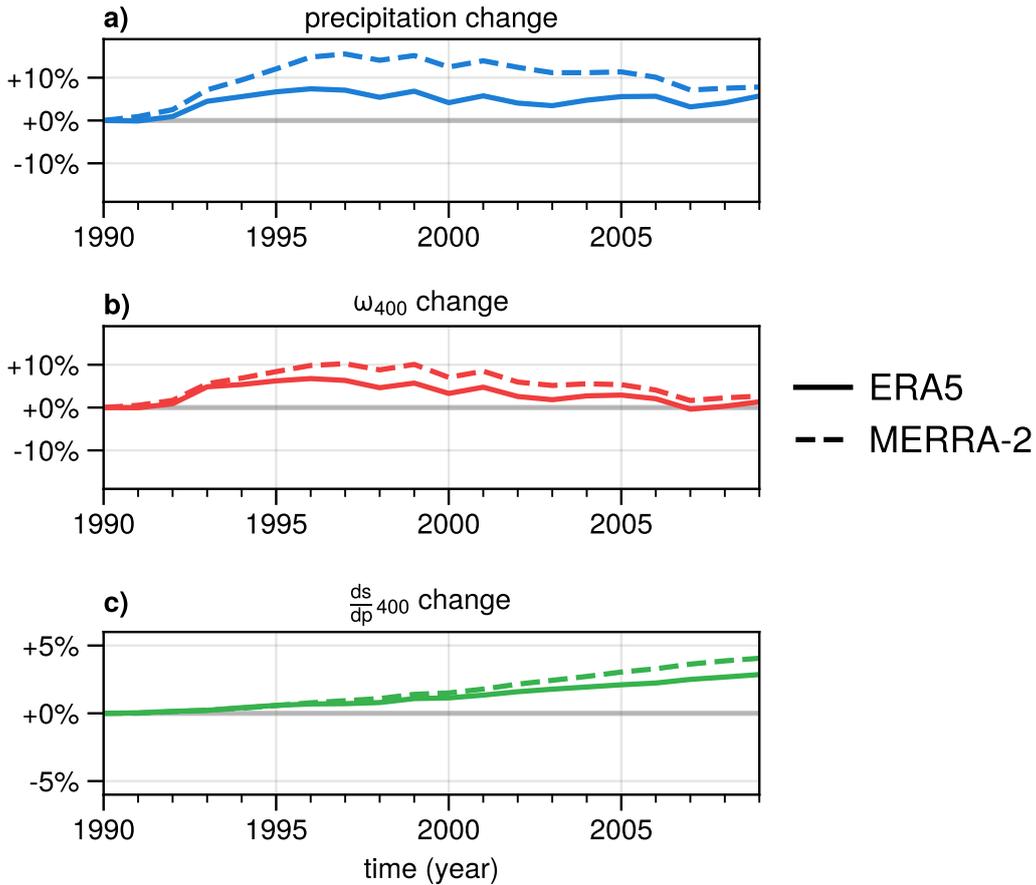
$$\Delta(X) = \frac{X - X_{ref}}{X_{ref}} \cdot 100\% \quad (3)$$

where  $X_{ref}$  denotes the quantity over the early period (1981-1999).

### 3 Results

First, we explore the spatial structure of MJO activity in the two reanalyses. The amplitude of MJO precipitation and  $\omega_{400}$  maximize in the IPWP region (Figures 1a-d) in both reanalyses during the early period. The changes in MJO precipitation and  $\omega_{400}$  amplitude between the late period and the early period have rich spatial structures, which are similar between the reanalyses (Figures 1e-h). Increases in both amplitudes occur to the south of India, at the southern edge of the Pacific warm pool, and near the Philippines. Decreases in both amplitudes occur near 5°S over the Maritime Continent. The regions of large amplitude of the MJO do not change substantially between the early and late period, allowing us to assess the temporal change in MJO activity within the IPWP region. The area-averaged amplitude of MJO precipitation and  $\omega_{400}$  in the IPWP region both show increases in the late period relative to the early period with precipitation intensifying by 5.6% in ERA5 and 7.6% in MERRA-2, and  $\omega_{400}$  intensifying by 1.2% in ERA5 and 2.1% in MERRA-2. Most important for this study, MJO precipitation amplitude intensifies more than MJO  $\omega_{400}$  amplitude in both reanalyses, although MJO activity in MERRA-2 is strengthened slightly more than in ERA5.

The 19-year running area-averaged MJO precipitation and  $\omega_{400}$  amplitude in the IPWP region increase between the early and the late periods of the record, while the amplitude in MERRA-2 exhibit larger changes than those in ERA5. However, both reanalyses demonstrate qualitatively similar fluctuations in between: in the early 90s, both of the amplitudes rise quickly, followed by a plateau and then a slight decrease afterward



**Figure 2.** Relative change in 19-year wintertime running composites of (a) MJO precipitation amplitude, (b) MJO  $\omega_{400}$  amplitude, and (c) dry static stability at 400 hPa with respect to the early period. The x-axis denotes the central years of the associated time window, for example, 2000 denotes the period of 1991-2009. The y-axis denotes the relative change to the early period.

187 (Figures 2a-b). The strengthening of the boreal-wintertime MJO activity during the late  
 188 20th century is consistent with previous studies examining observed zonal wind changes  
 189 at 200 hPa and 850 hPa (Jones & Carvalho, 2006). Moreover, both reanalyses agree that  
 190 throughout most of the record, MJO precipitation amplitude shows larger positive changes  
 191 than MJO  $\omega_{400}$  amplitude.

192 While we attempted to explain the fluctuating pattern in MJO precipitation and  
 193  $\omega_{400}$  amplitude, we could find no obvious connections between them and interannual to  
 194 decadal variability in surface air temperature. The evolution of surface air temperature  
 195 in the IPWP region (Figure S2b) and its evolution relative to the whole tropics (Figure  
 196 S2c) do not resemble the variability in the MJO amplitude time series, which have dif-  
 197 ferent trends from the early 90s onward (Figures 2a-b). Commonly used Pacific SST in-  
 198 dices that capture interannual to decadal variability also do not show similar variabil-  
 199 ity to the MJO amplitude time series (compare Figures 2a-b with Figure S3 SST-indices).

200 To sum up, both MJO precipitation and  $\omega_{400}$  amplitude increase from the early  
 201 period to the late period in the IPWP region in both reanalyses, although the time evo-  
 202 lution is non-monotonic and the amplitude of the change varies between the reanalyses.  
 203 The timeseries of the amplitudes are not easily explained by tropical SST variability. How-

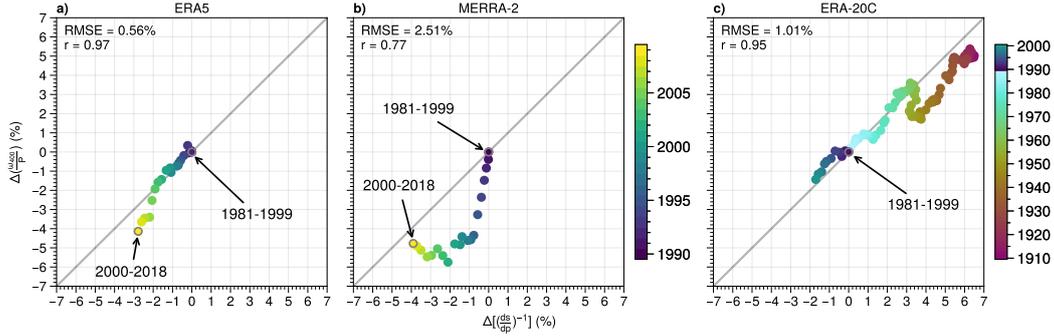
204 ever, a robust result common among different time periods and reanalyses is that the  
 205 increase in MJO precipitation amplitude is always stronger than in MJO  $\omega_{400}$  amplitude,  
 206 consistent with what WTG balance would predict based on the increasing tropical static  
 207 stability with SST warming observed in recent decades (Figure 2c; see also e.g. Sherwood  
 208 & Nishant, 2015). We explore this contention more below.

209 Given a change in dry static stability, the theoretical change in the ratio of MJO  
 210  $\omega_{400}$  to precipitation amplitude can be computed if one assumes that WTG balance holds  
 211 (equation 1) and that the vertical structure of  $Q_1$  associated with the MJO is not changed  
 212 (equation 2). Previous modeling studies have shown good agreement between static sta-  
 213 bility changes and this ratio when applied to MJO-associated wind and precipitation vari-  
 214 ance (Maloney & Xie, 2013; Wolding & Maloney, 2015; Wolding et al., 2016; Bui & Mal-  
 215 oney, 2018). As the climate system warms, tropical dry static stability increases in the  
 216 troposphere because the atmospheric profile in the deep tropics roughly follows a moist  
 217 adiabat set by the surface temperature in convecting regions (Knutson & Manabe, 1995).  
 218 Consistently, increasing dry static stability has been observed in recent years as surface  
 219 temperature has increased (Allen & Sherwood, 2008). Because surface temperature has  
 220 increased since 1981 (Figure S2a), equation (2) would argue for a greater change in MJO  
 221 precipitation amplitude compared to MJO  $\omega_{400}$  amplitude.

222 Figure 3a-b displays the temporal evolution of the inverse of dry static stability and  
 223 the ratio of MJO  $\omega_{400}$  to precipitation amplitude (MJO  $\omega_{400}/P$ ; see equation 2) in ERA5  
 224 and MERRA-2. The grey diagonal line denotes the predicted theoretical relationship be-  
 225 tween MJO  $\omega_{400}/P$  and inverse static stability assuming WTG theory holds and the ver-  
 226 tical structure of the MJO remains unchanged. Between the late period and the early  
 227 period (the two outlined endpoints), the decrease of the inverse of dry static stability is  
 228 2.8% in ERA5 and 4.0% in MERRA-2, and the decrease of MJO  $\omega_{400}/P$  is 4.2% in ERA5  
 229 and 4.9% in MERRA-2. Consistent with WTG theory, MJO  $\omega_{400}/P$  and the inverse of  
 230 dry static stability show comparable decreases between the early period (1981-1999) and  
 231 the late period (2000-2018). Agreement is also good in ERA5 for interim periods, espe-  
 232 cially until about 2000 (Figure 3a). Considering the complicated temporal evolution of  
 233 MJO precipitation and  $\omega_{400}$  amplitude (Figure 2), WTG balance provides a reasonable  
 234 explanation for the evolution of MJO  $\omega_{400}/P$  over the past 38 years, especially when con-  
 235 sidering the start and end of the record.

236 As many MJO studies use zonal wind amplitude as a metric of MJO activity (e.g.  
 237 Slingo et al., 1999; Jones & Carvalho, 2006), we also examine the amplitude of MJO 850  
 238 hPa zonal wind ( $u_{850}$ ) for reference. The evolution of the ratio of MJO circulation to pre-  
 239 cipitation amplitude is defined here using  $u_{850}$  (MJO  $u_{850}/P$ ). Although using  $u_{850}$  is  
 240 not a direct application of WTG balance in equation (2), the amplitude of horizontal ve-  
 241 locity should scale with vertical velocity through divergence if the vertical structure doesn't  
 242 change (Maloney & Xie, 2013). Under such conditions, we would expect a qualitatively  
 243 similar decrease in the ratio of MJO  $u_{850}$  to precipitation amplitude. Figure S4 shows  
 244 that  $u_{850}$  amplitude relative to precipitation does decrease in a qualitatively similar way,  
 245 although with stronger decreases relative to  $P$  than for  $\omega_{400}$ .

246 Although MJO  $\omega_{400}/P$  generally follows the change in the inverse of dry static sta-  
 247 bility, there exist deviations from theoretical predictions, with maximum differences of  
 248 about 1.5% in ERA5 and 4% in MERRA-2. To place these values in a larger scale con-  
 249 text, we compare Figure 3a-b to Figure 3c that shows results from ERA-20C spanning  
 250 1901-2009. The theoretical estimate works well in ERA-20C over the whole century, with  
 251 about 7-8% decreases in both MJO  $\omega_{400}/P$  and inverse static stability over the century.  
 252 The maximum deviation of MJO  $\omega_{400}/P$  change in ERA-20C is about 2% from theo-  
 253 retical values predicted by the inverse of dry static stability. Deviations of ERA5 from  
 254 theoretical values are even smaller than this, while deviations in MERRA-2 are larger.  
 255 As described below, deviations of MERRA-2 from the theoretical estimate may occur  
 256 due to the imperfect assumption of proportionality of  $Q_1$  at 400 hPa and  $P$ .



**Figure 3.** Relative change in (x-axis) the reciprocal of dry static stability at 400 hPa and (y-axis) the ratio of MJO  $\omega_{400}$  to precipitation amplitude over the IPWP region between 19-year running windows and the early period. Colors indicate the central year of the running window. The grey diagonal line denotes the change in the ratio predicted by WTG balance assuming vertical heating structure is unchanged (equation 2). Root-mean-square error (RMSE) of MJO  $\omega_{400}/P$  relative to theoretical predictions are provided in each panel. Correlation coefficients ( $r$ ) between the two variables are also provided to show how coherent they change. Note that the MJO-associated quantities are defined using OMI for (a) ERA5 and (b) MERRA-2 whereas standard deviations in the MJO wavenumber-frequency band are used for (c) ERA-20C.

257 In MERRA-2, equation (2) overestimates the decrease in MJO  $\omega_{400}/P$  in the in-  
 258 tervening periods but works well for the two endpoints. MJO  $\omega_{400}/P$  in MERRA-2 shows  
 259 stronger decreases than ERA5 during the interim period largely because it has a larger  
 260  $P$  amplitude change than ERA5. The exact reasons for differences between the two anal-  
 261 yses are unclear, although they may depend on the different behavior of tropical con-  
 262 vection simulated by the two reanalysis models. The differing dry static energy profiles  
 263 changes between ERA5 and MERRA-2 for the IPWP region (Figures S5) not only indi-  
 264 cate differing static stability changes, but also circumstantially suggest different changes  
 265 to the convective heating structure between datasets given the regulation of tropical tropo-  
 266 spheric temperature by convective heating. Such structure changes would affect how  
 267 well the balance in equation (2) reflects equation (1), considering the assumption about  
 268 the proportionality of  $P$  to  $Q_1$  at 400 hPa. MERRA-2 exhibits more warming in the lower  
 269 troposphere than ERA5, presumably associated with increased condensational heating  
 270 and precipitation generation there, which would produce greater decreases in MJO  $\omega_{400}/P$   
 271 than that expected by looking at the 400 hPa level in isolation. The rate of increase in  
 272 low-level warming in MERRA-2 is particularly strong until the 19-year period centered  
 273 on 1997, possibly consistent with the greater MJO precipitation amplitude increase in  
 274 MERRA during that time than ERA5 (Figure 2), although translating mean state convec-  
 275 tive structure changes to those on subseasonal timescales should be done with care.

276 An examination of MJO anomaly amplitudes of  $Q_1$  at 400 hPa and precipitation  
 277 suggests a weaker consistency between the two quantities in MERRA-2 (Figure S6), con-  
 278 sistent with possible vertical structure changes. However, while the change in the ratio  
 279 of  $\omega_{400}$  to  $Q_1$  amplitude at 400 hPa generally follows dry static stability in ERA5, the  
 280 agreement is not as good as in MERRA-2 (Figure S7), which might also explain some  
 281 of the differing behavior in Figure 3. The reasons for this discrepancy are unclear.

## 4 Summary

The changes to MJO precipitation and  $\omega_{400}$  amplitude from 1981 to 2018 are examined in three reanalysis datasets, ERA5, MERRA-2, and ERA-20C. Both amplitudes in ERA5 and MERRA-2 individually increased from the early period (1981-1999) to the late period (2000-2018) (Figure 1). However, their temporal behavior is non-monotonic in that both amplitudes intensify from 1981 to 1997 and slowly weaken or remain constant thereafter (Figure 2a-b). Interannual-to-decadal surface temperature variability (Figure S2; Figure S3) shows no simple relationship with this non-monotonic behavior in MJO activity changes.

When viewed together, amplitude changes of MJO precipitation are larger than MJO  $\omega_{400}$  throughout the past four decades relative to the early period (1981-1999). A preferential strengthening of MJO precipitation amplitude relative to MJO  $\omega_{400}$  amplitude is predicted by WTG balance with a warming climate, in that increasing dry static stability in response to SST warming in recent decades makes vertical motion more efficient at compensating latent heat release in deep convective regions. The fractional amplitude changes in the ratio of MJO  $\omega_{400}$  to precipitation between 1981-1999 and 2000-2018 approximately match inverse dry static stability changes with climate warming, consistent with WTG balance (Figure 3a-b). A similar result is shown in ERA-20C between 1901-1919 and 1991-2009.

While trends in these reanalyses appear to generally follow WTG balance, differences exist in the behavior of the three reanalyses. MJO precipitation and  $\omega_{400}$  amplitude increases are larger in MERRA-2 than in ERA5, especially in intermediate periods between the beginning and end of the record, although they show qualitatively similar time series variability (Figure 2). Decreases in MJO  $\omega_{400}/P$  also fit the theoretical prediction based on the inverse of dry static stability better in ERA5 and ERA-20C than in MERRA-2 across all 19-year periods examined in terms of RMSE, and these differences may be associated with differences in the simulated structure of tropical deep convection, which remains a topic for further investigation.

The present paper provides a preliminary assessment of MJO activity changes in precipitation and vertical velocity over the past four decades that include both anthropogenic forcing and natural variability, and uses a century-long dataset to assess recent changes in the context of natural variability over the longer record. Our results based on observations support those previously derived from climate models (e.g. Bui & Maloney, 2019) suggesting that decreases in MJO  $\omega_{400}/P$  occur as surface temperatures warm due to anthropogenic forcing. Nevertheless, discrepancies between results from ERA5 and MERRA-2 leave lingering questions about the degree to which changes to the MJO can be explained by WTG theory, including the assumption that  $Q_1$  has no vertical structural changes in response to climate warming. Further work using a broader set of observational data including tropical sounding and other in situ records are needed to affirm the validity of equation (2) for explaining MJO behavior.

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