

An Overview of Hilbert-Huang Transform-based Earthquake Source Characterization using Strong Motion Data

Swapnil Mache

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Kusala Rajendran

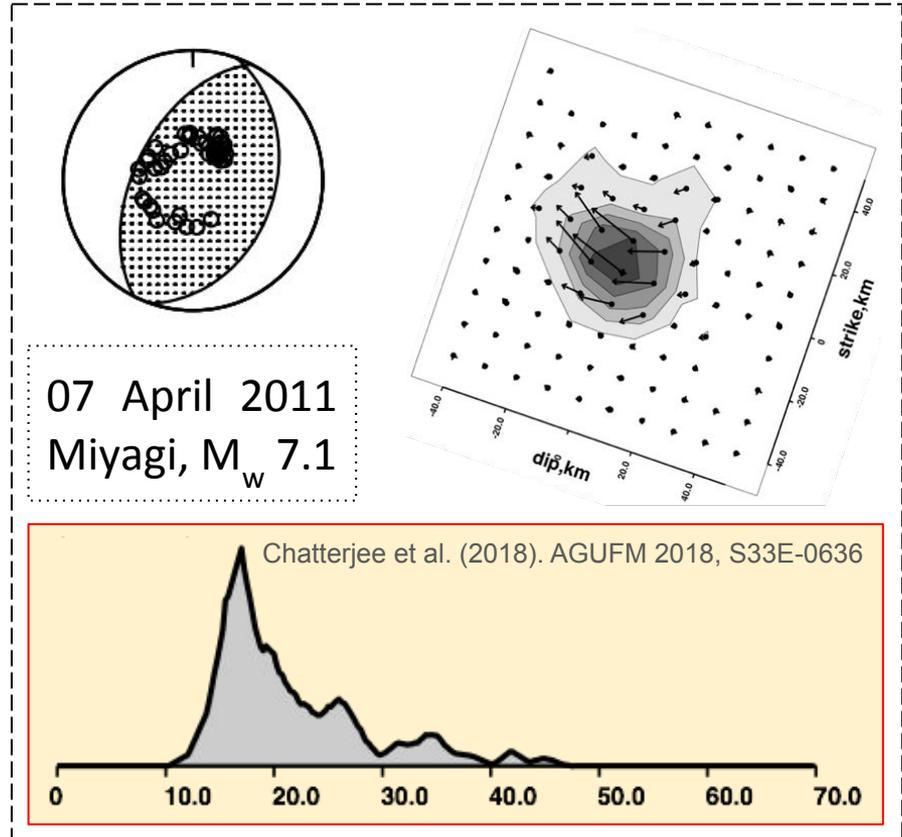
Indian Institute of Science
Bangalore, India

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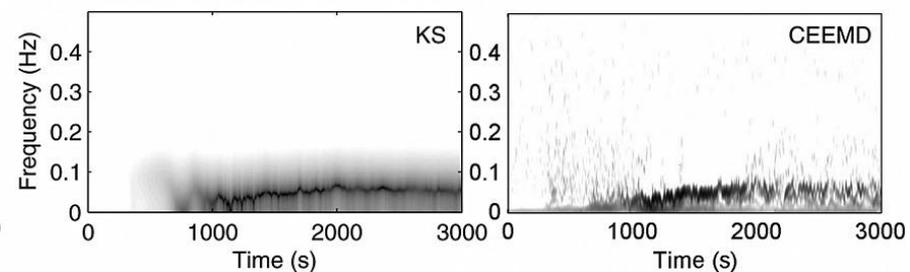
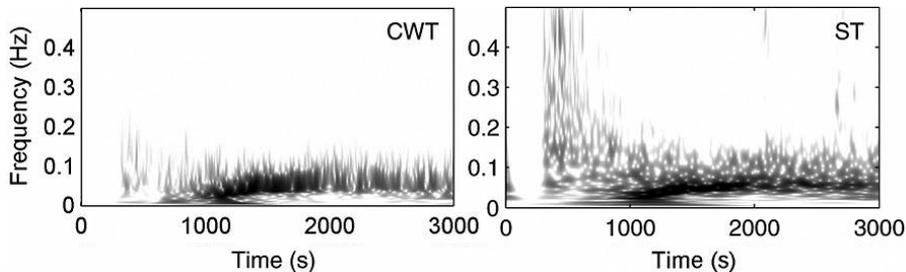
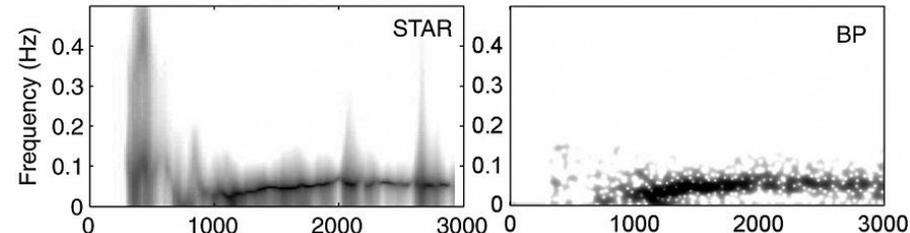
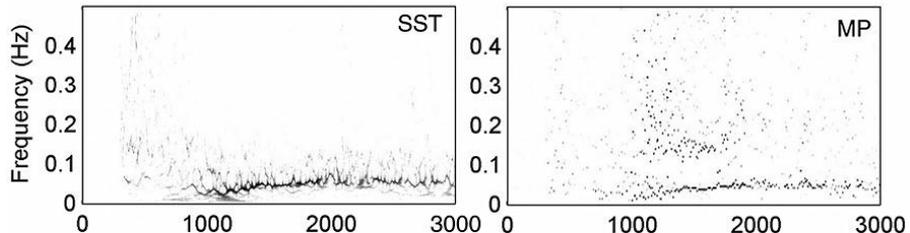
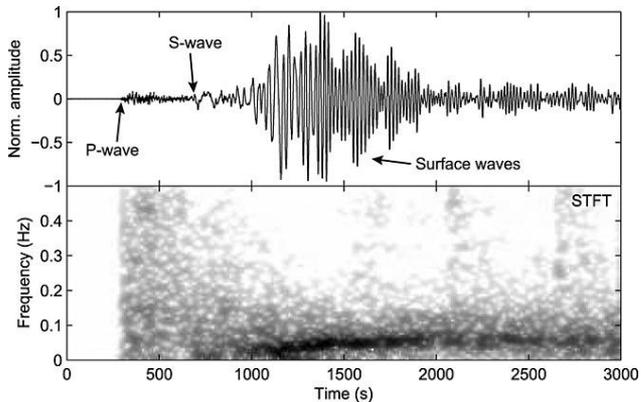
UNIVERSITY OF
OREGON



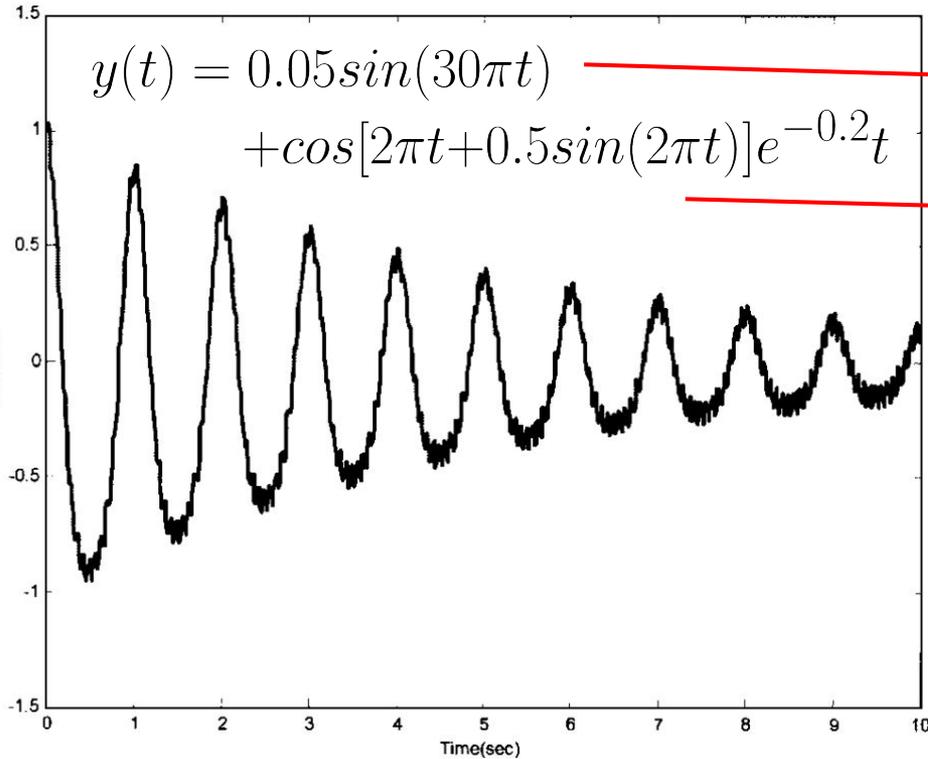
Harnessing time-frequency analysis tools + empirical mode decomposition to represent energy release

11 March 2011
Tohoku, M_w 9.0

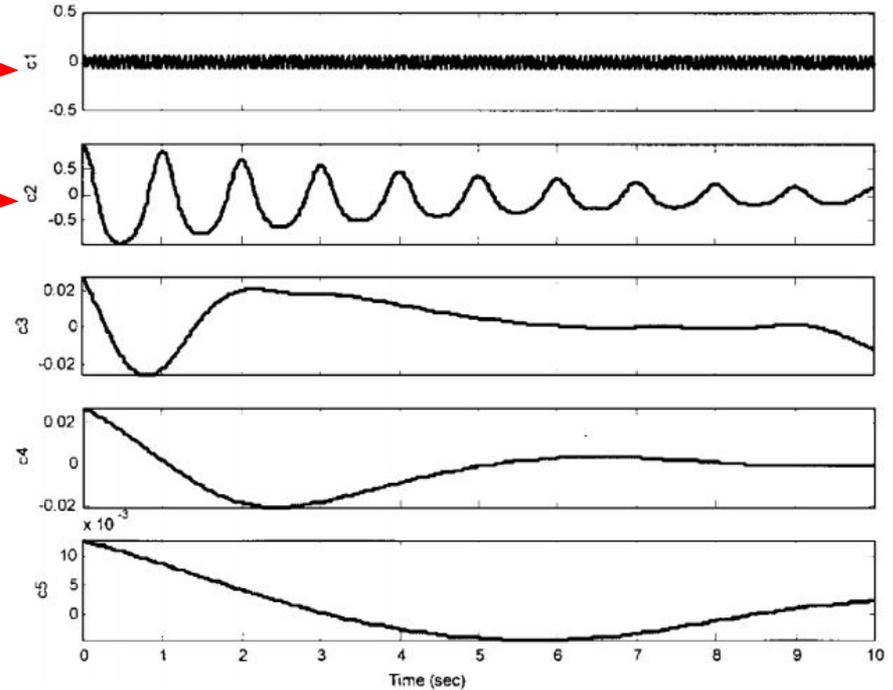
Time-Frequency Representations



Harnessing time-frequency analysis tools + empirical mode decomposition to represent energy release

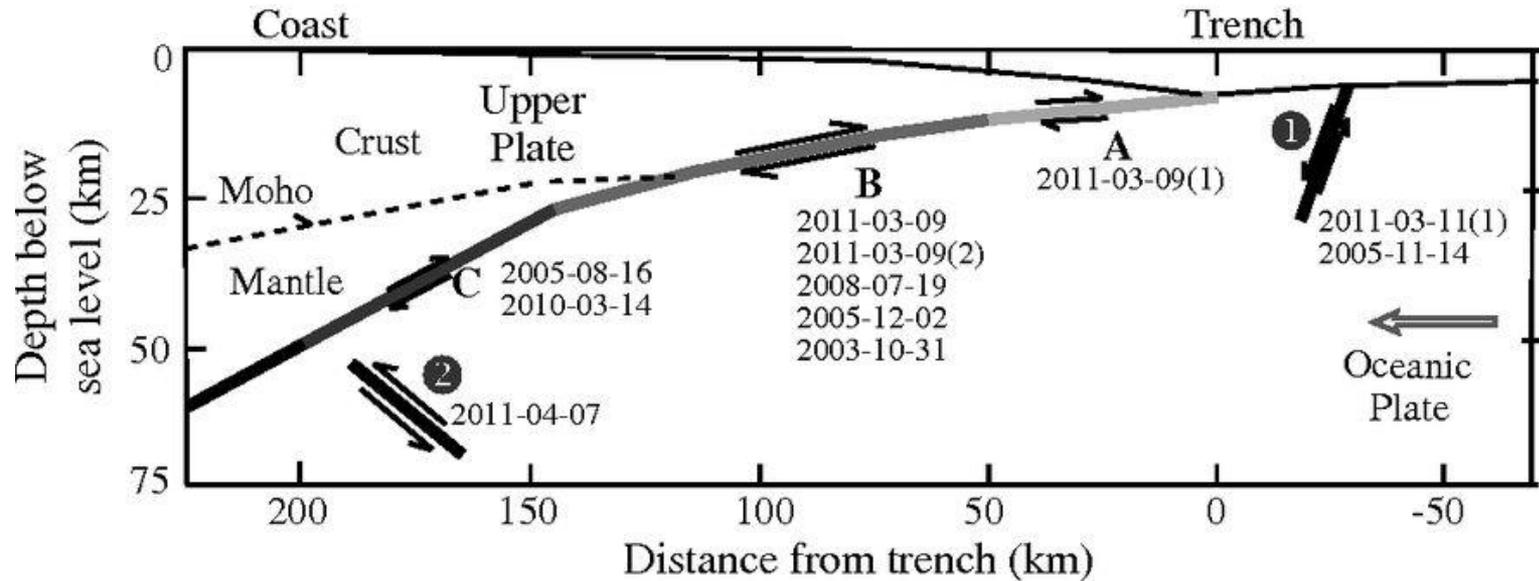


Signal $y(t)$



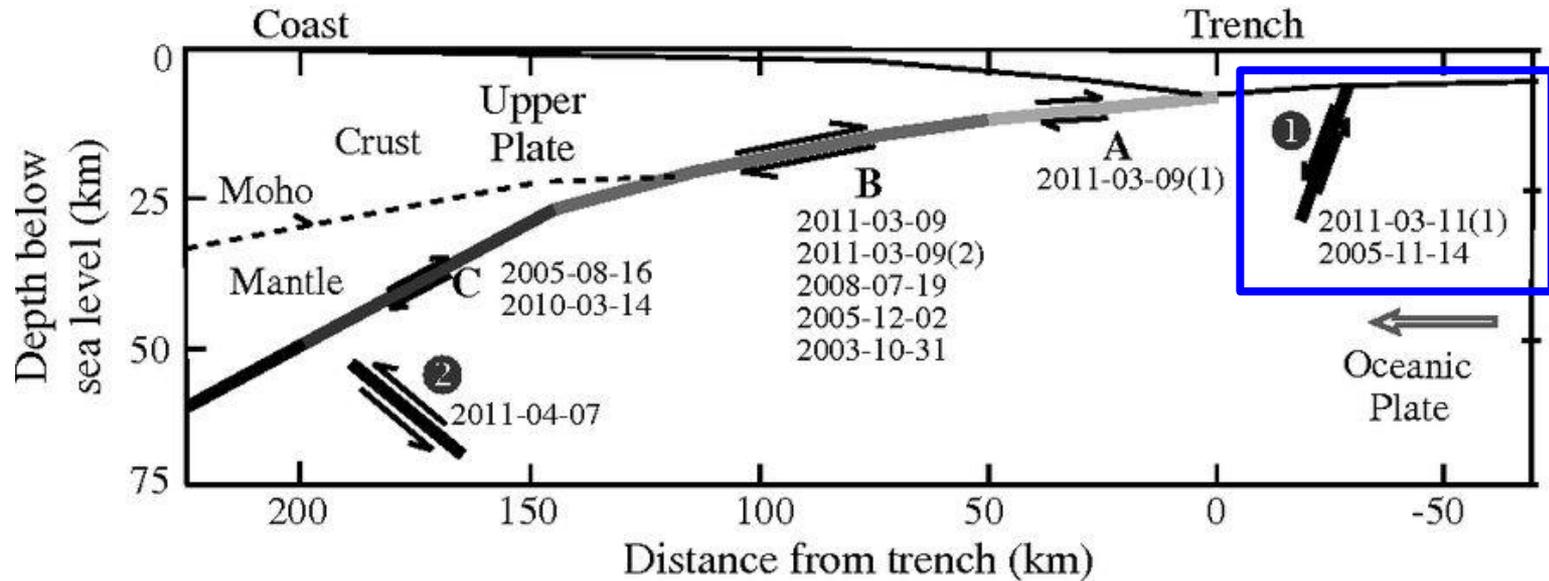
Intrinsic Mode Functions

Heterogeneous energy-release and frequency content depending on tectonic setting and depth



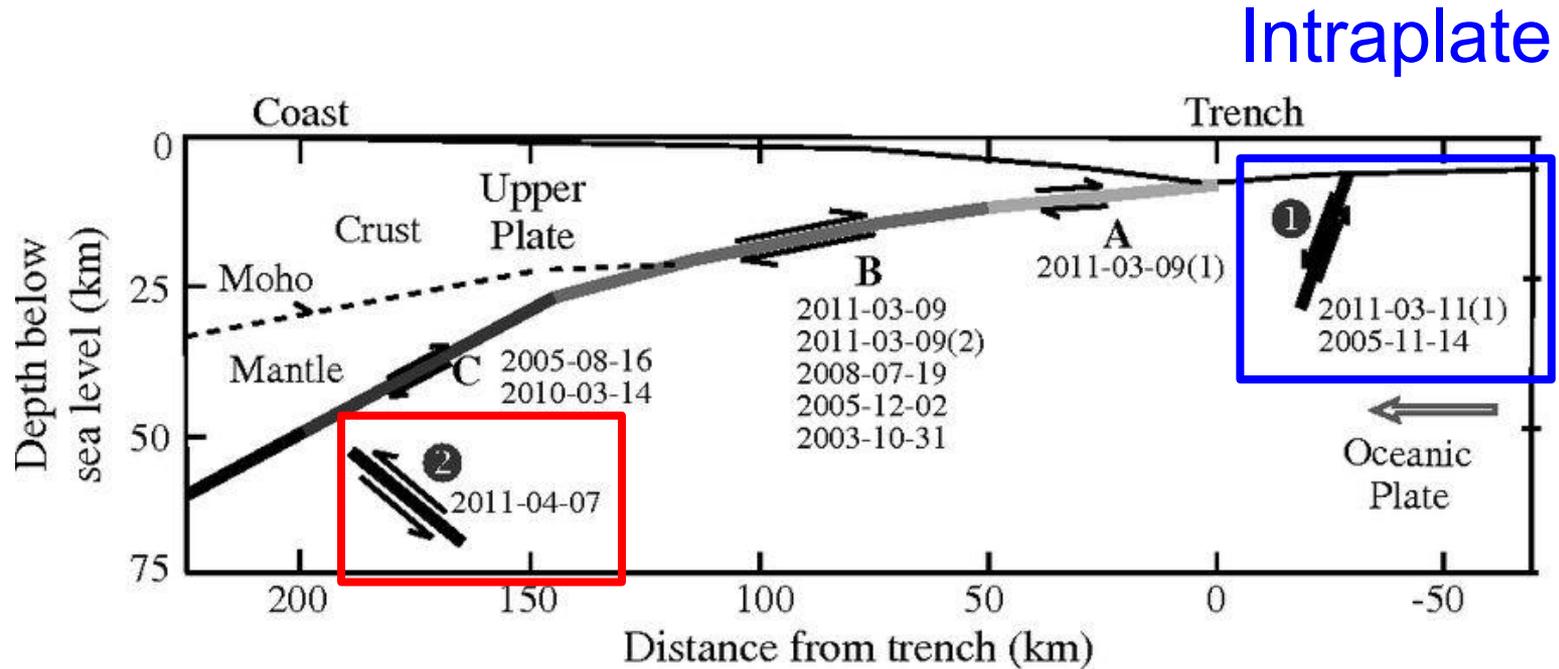
Heterogeneous energy-release and frequency content depending on tectonic setting and depth

Intraplate



Ye, Lay, and Kanamori (2013).
BSSA, 103, 1221-1241

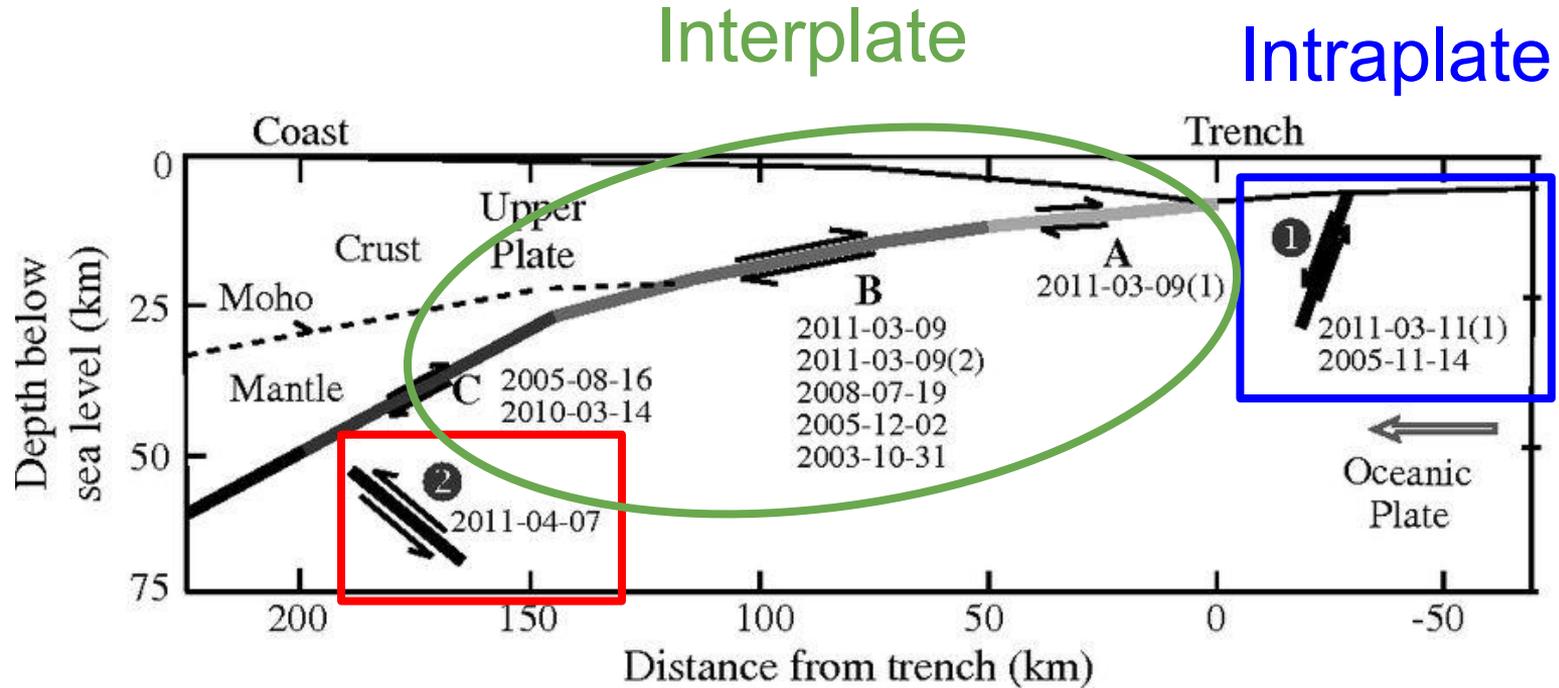
Heterogeneous energy-release and frequency content depending on tectonic setting and depth



Intraplate

Intraslab

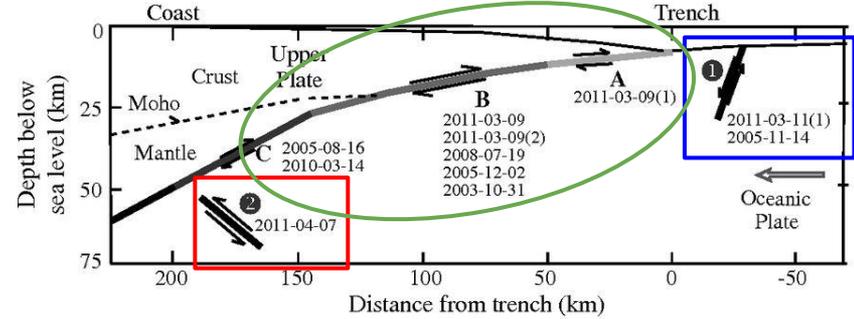
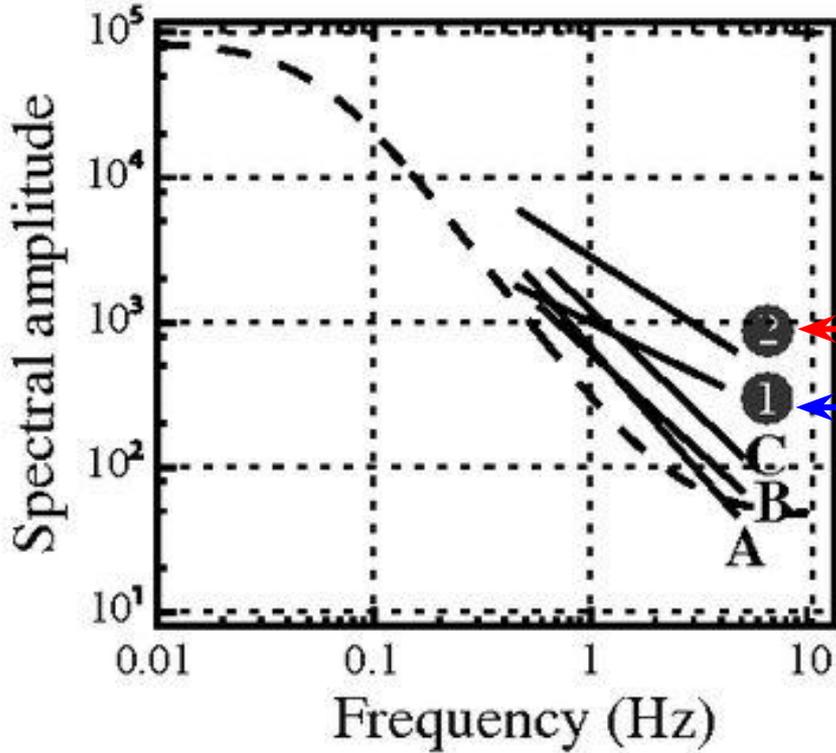
Heterogeneous energy-release and frequency content depending on tectonic setting and depth



Intraslab

Ye, Lay, and Kanamori (2013).
BSSA, 103, 1221-1241

Spectral amplitudes: **Interplate** < **Intraplate** < **Intraslab**

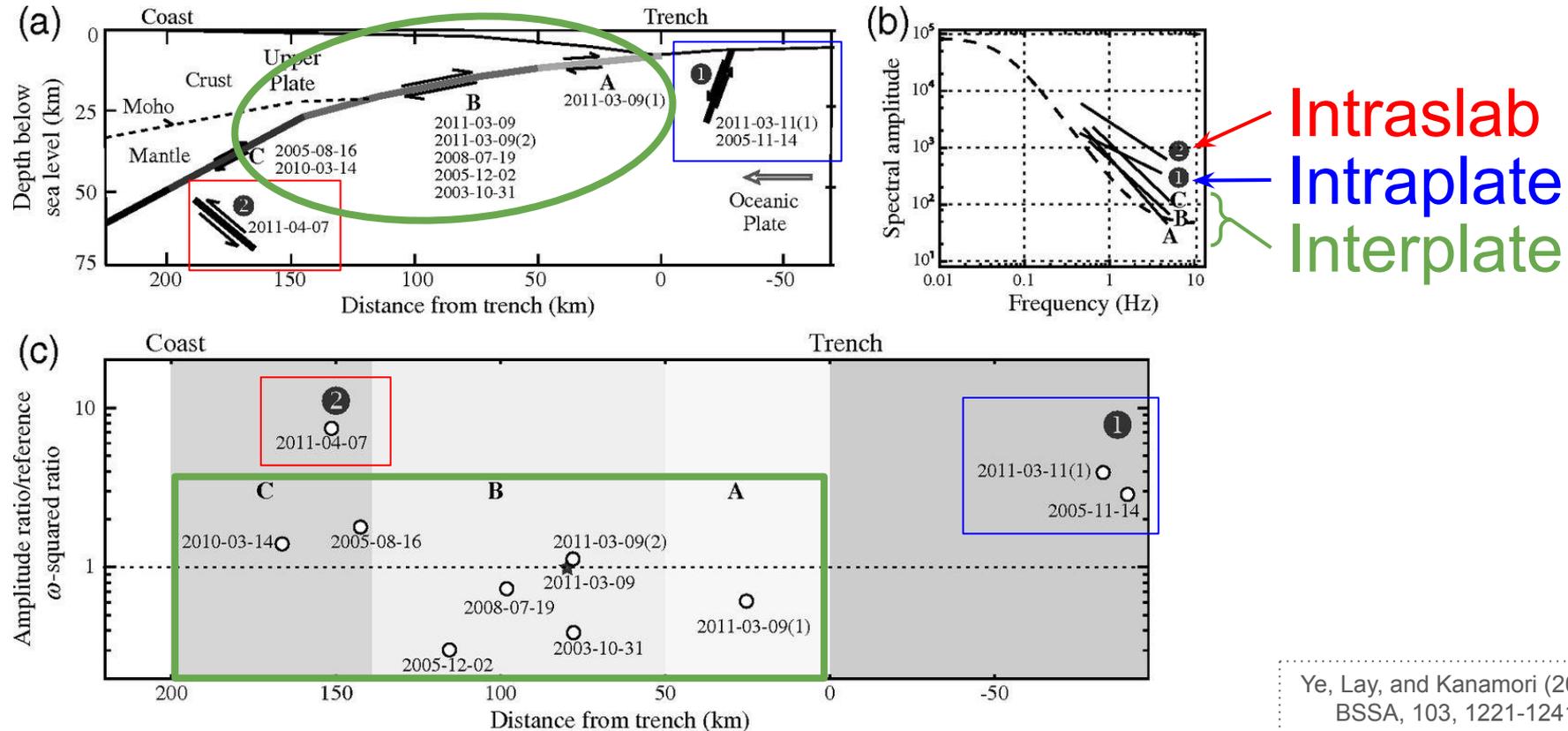


Intraslab

Intraplate

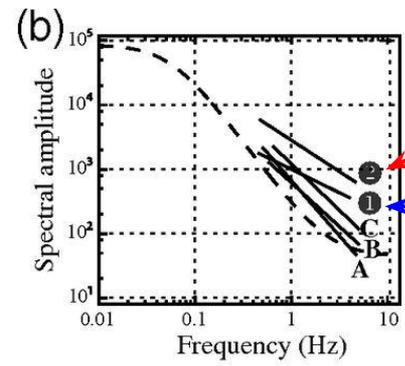
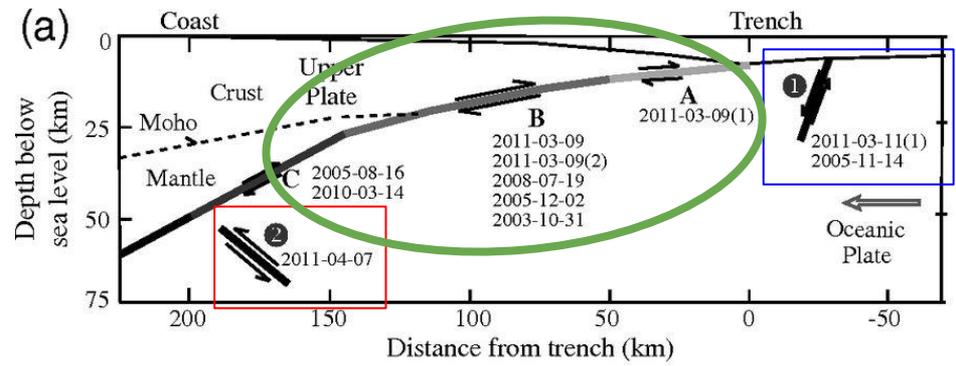
Interplate

Interplate: increasing high-frequency energy and energy/moment with depth

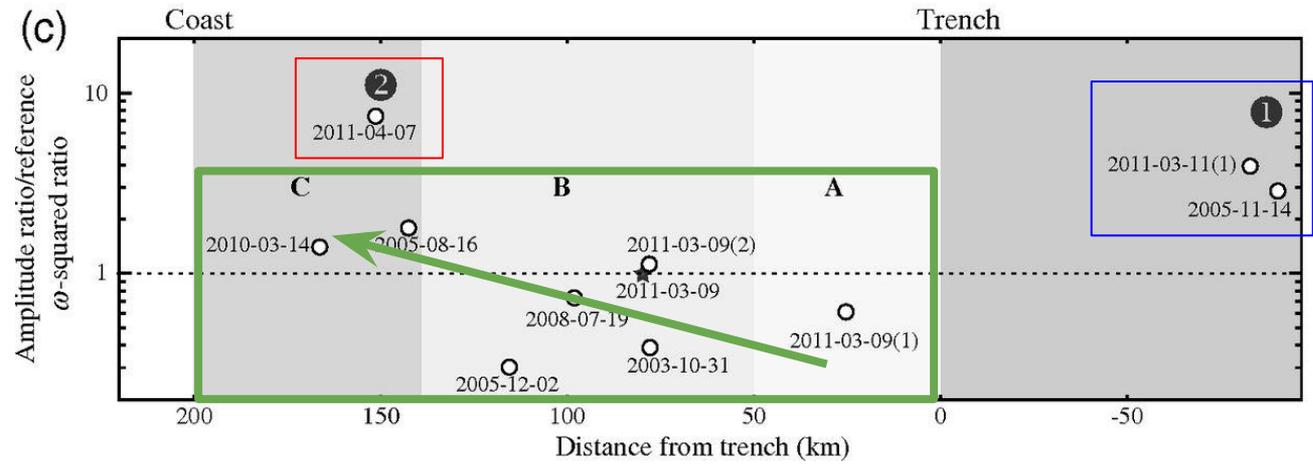


Ye, Lay, and Kanamori (2013).
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Interplate: increasing high-frequency energy and energy/moment with depth

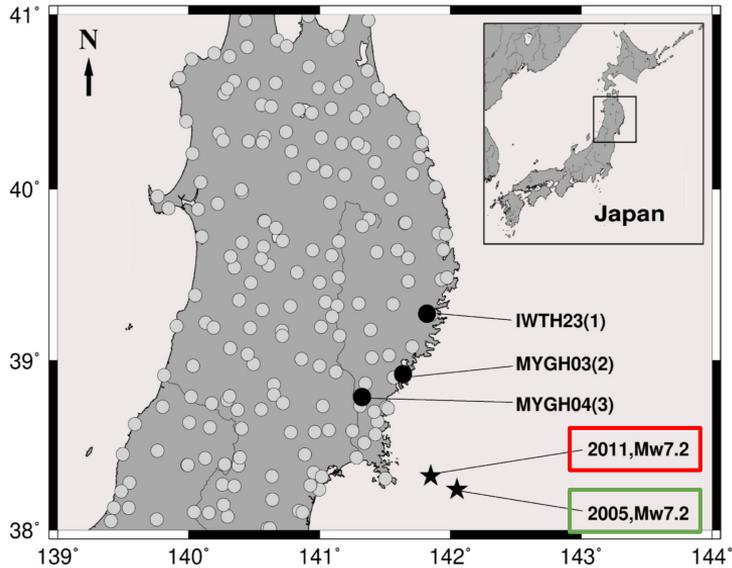


Intraslab
Intraplate
Interplate



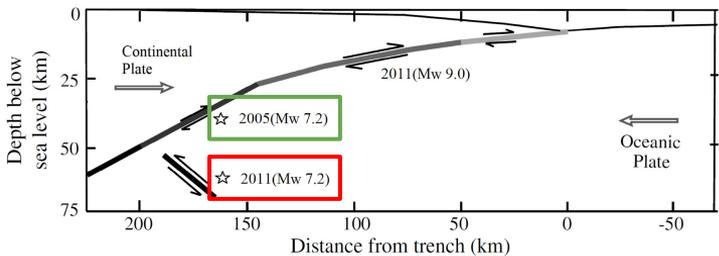
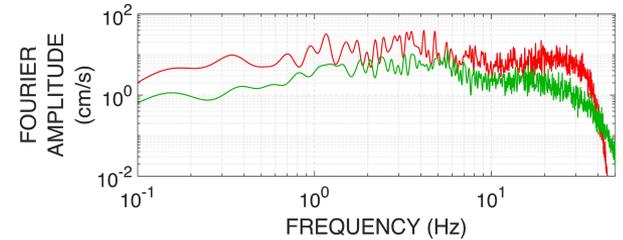
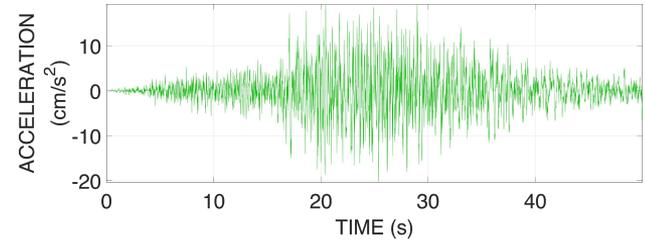
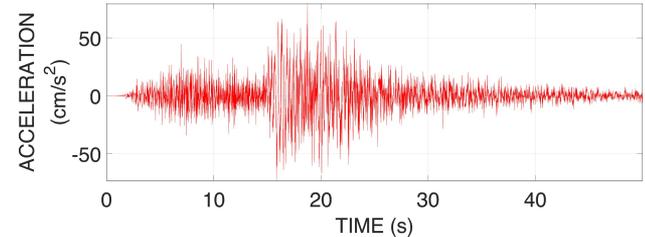
Ye, Lay, and Kanamori (2013).
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Time-frequency analysis of intrinsic mode functions decomposed from earthquake strong-motion data

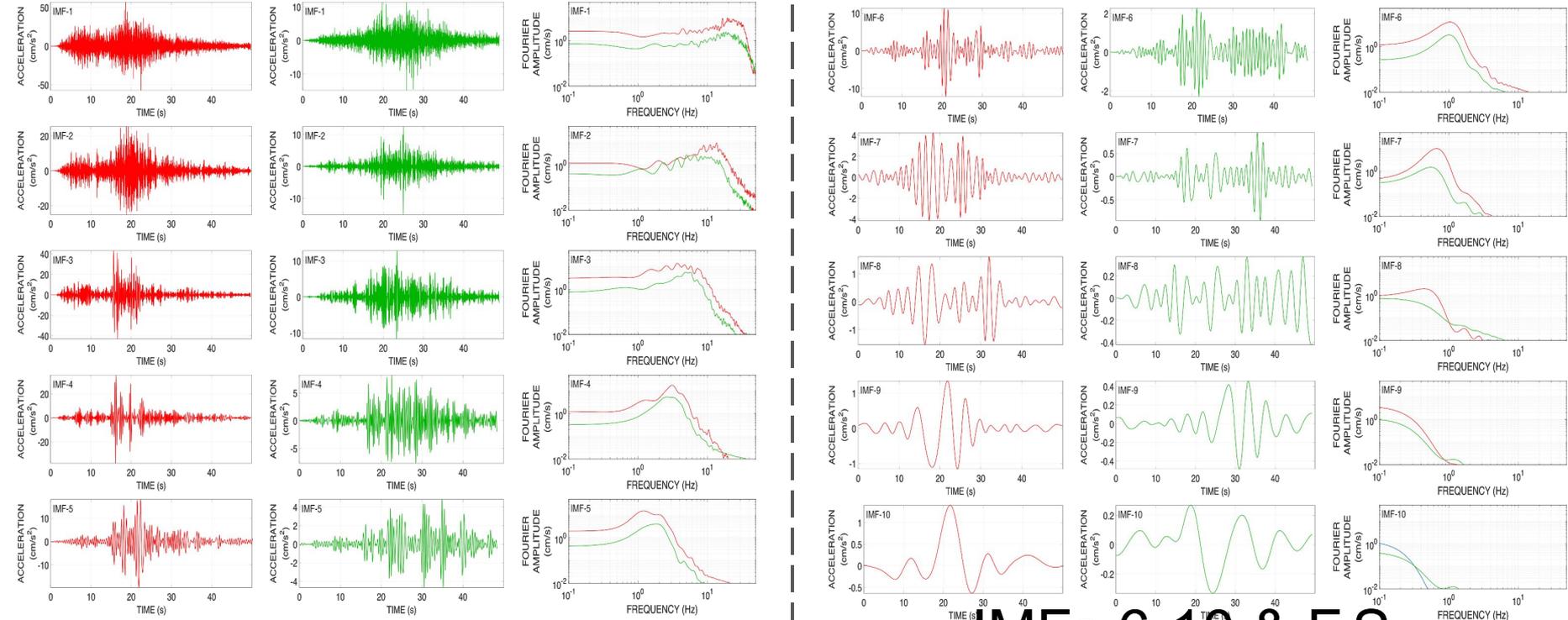


Intraslab

Interplate



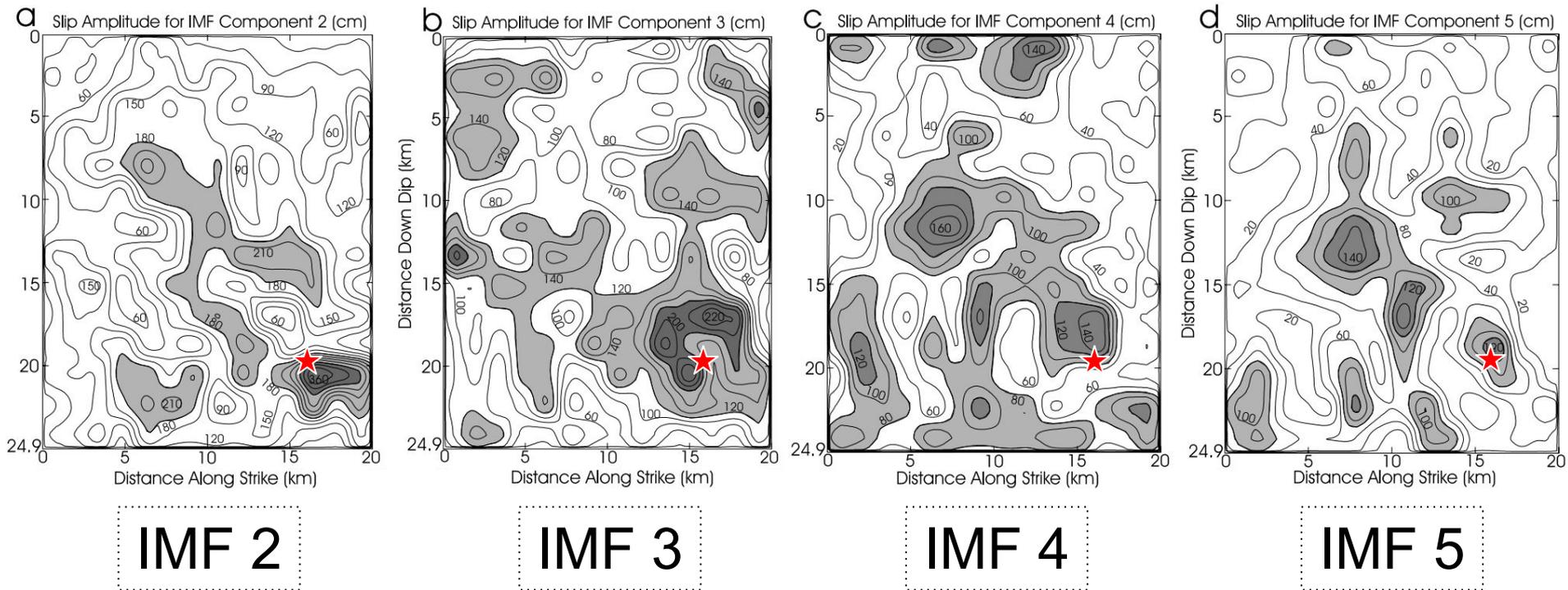
Time-frequency analysis of intrinsic mode functions decomposed from earthquake strong-motion data



IMFs 6-10 & F.S.

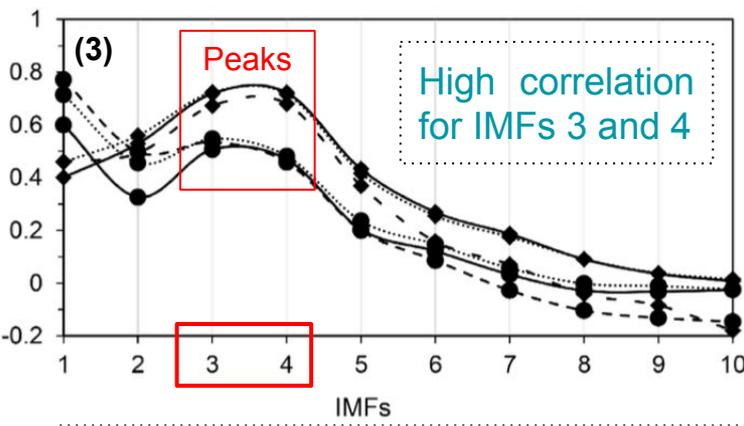
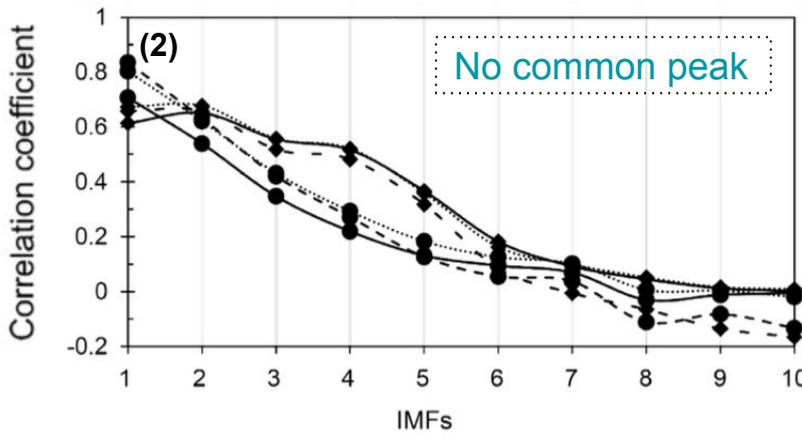
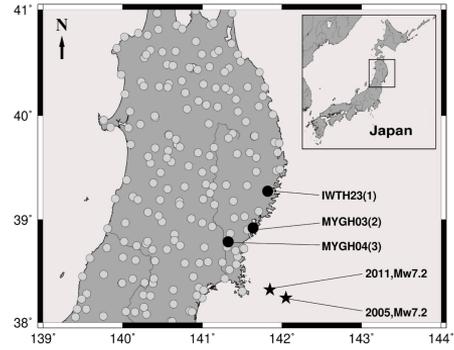
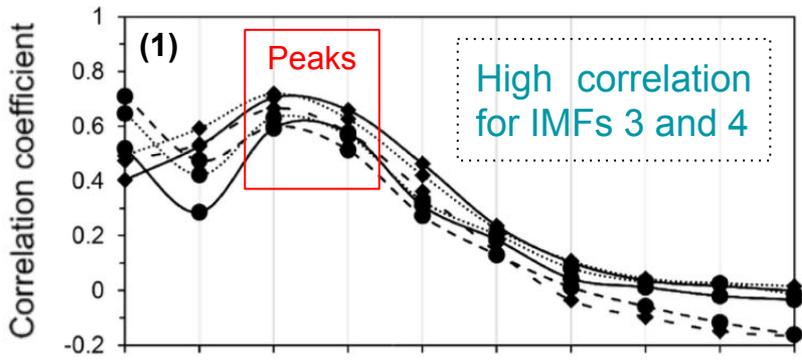
IMFs 1-5 & Fourier Spectra

Studies show source signal contained in combination of IMFs



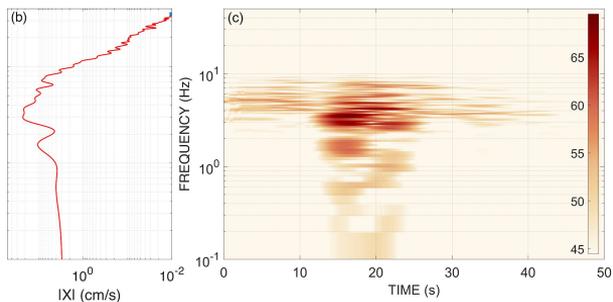
Progression of slip away from **hypocenter** from IMF 2 to 5

High correlation between original signal and IMFs that best capture the original signal—possibly represent the source.

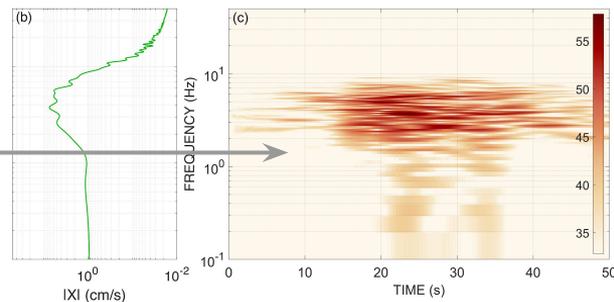


- Tohoku (FFT)
- ◆ Miyagi (FFT)
- Tohoku (STFT)
- ◆ Miyagi (STFT)
- Tohoku (CWT)
- ◆ Miyagi (CWT)

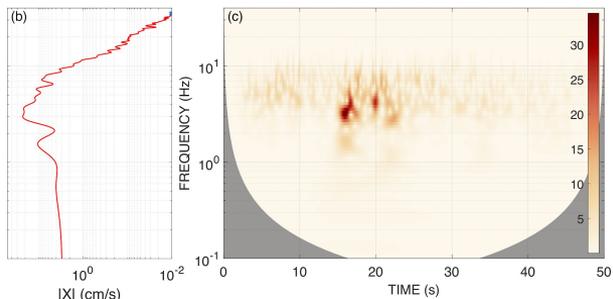
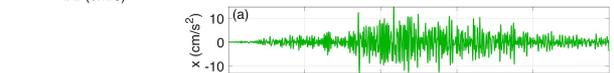
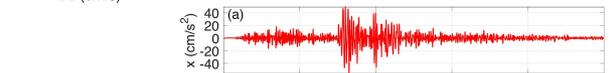
Linear combination of well-correlated IMFs gives a possible time-frequency representation of energy release.



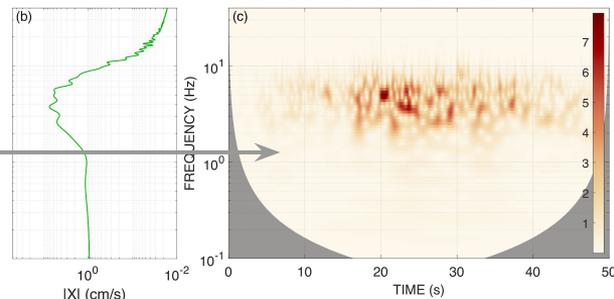
← Spectrograms →



IMF 3 + 4



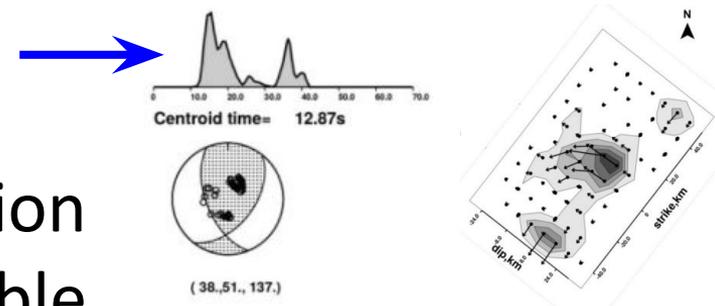
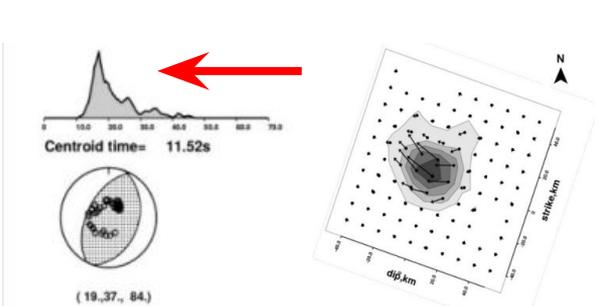
← Scalograms →



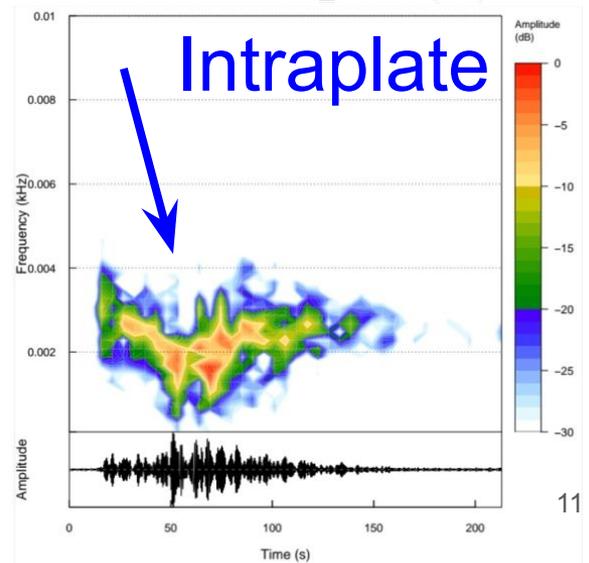
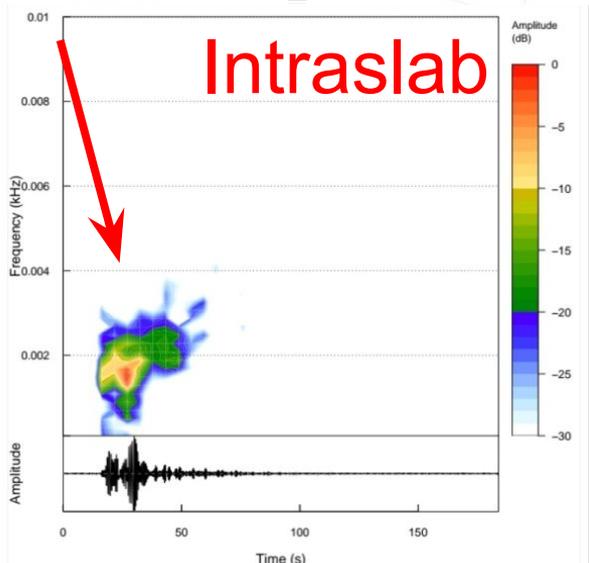
Intraslab

Interplate

Joint study of teleseismic and strong-motion data connecting the energy release obtained from both



Shape and duration of MRF comparable with high-energy pulses & multiple patches in spectrograms



Chatterjee et al. (2018). AGUFM 2018, S33E-0636

Improved resolution using the Hilbert-Huang Transform (HHT) = EMD + Hilbert Spectral Analysis

Hilbert transform, $\hat{c}_k(t) = \frac{1}{\pi} \int_{-\infty}^{+\infty} \frac{c_k(\tau)}{(t - \tau)} d\tau$

Convolution with $1/t$.
Focus on local properties of signal

Analytic signal, $c_k(t) + j\hat{c}_k(t) = a_k(t)e^{j\theta_k(t)}$

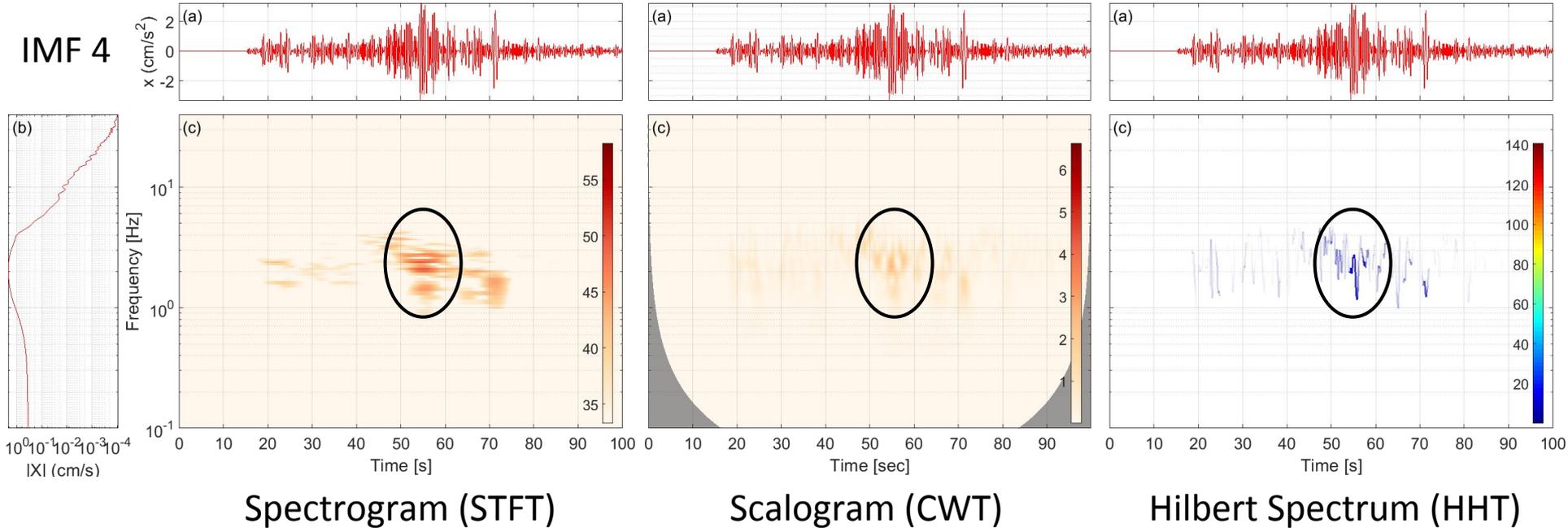
Amplitude $a_k(t)$ and frequency of each IMF as a $f(\text{time})$

Instantaneous frequency, $\omega_k(t) = \frac{d\theta_k(t)}{dt}$

Local measure of frequency

Hilbert energy spectrum : **Amplitude² [$a_k^2(t)$]** values on time-frequency plane

HHT gives better resolution over spectrogram & scalogram

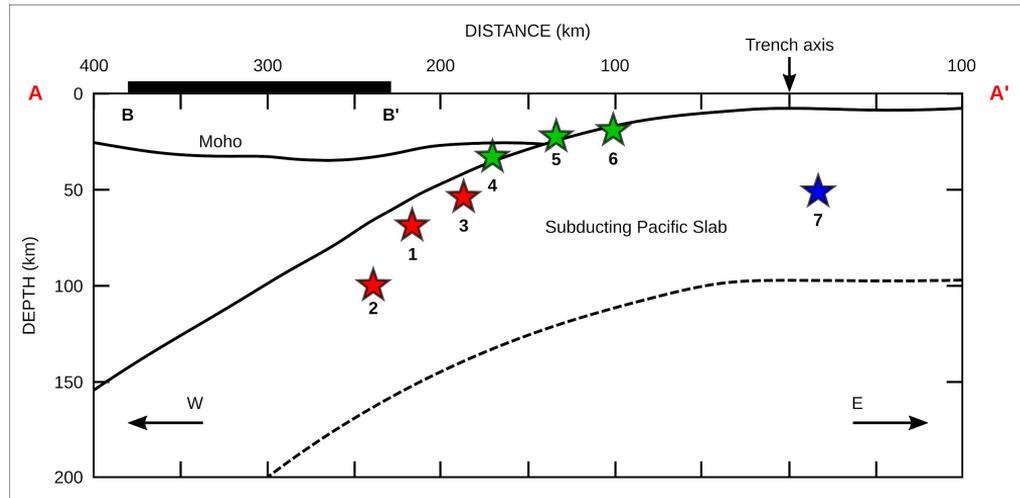
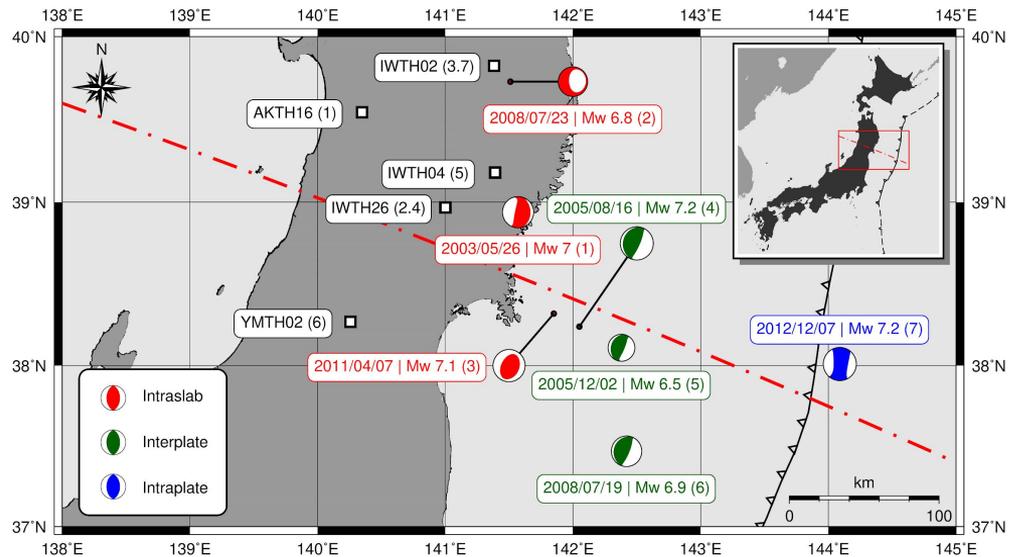


Improving resolution

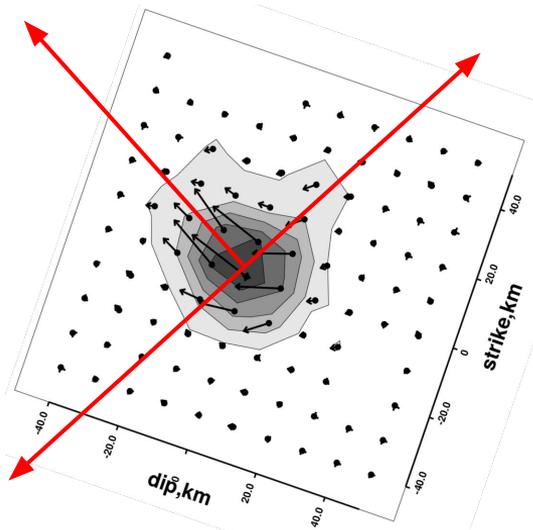


Proposing station and IMF-selection criteria and expanding the analysis

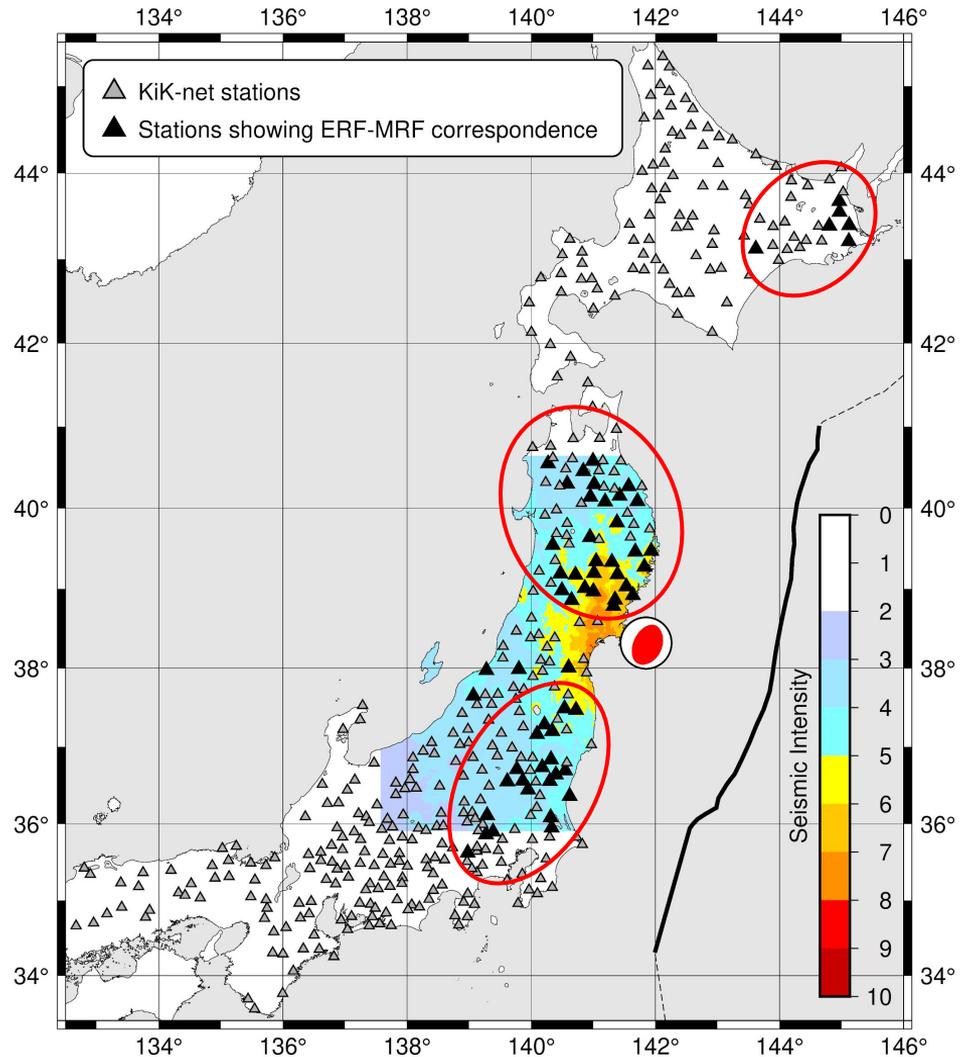
- Strong motion data (KiK-net, NIED, Japan)
- Borehole sensors (> 100 m)
- Vertical component



"Best" stations?
In the direction of rupture
propagation and
orthogonal to it.

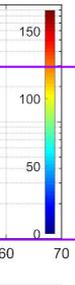
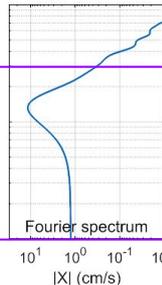
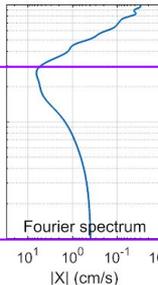
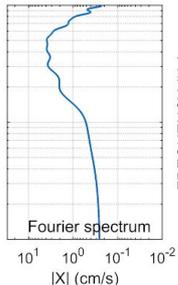
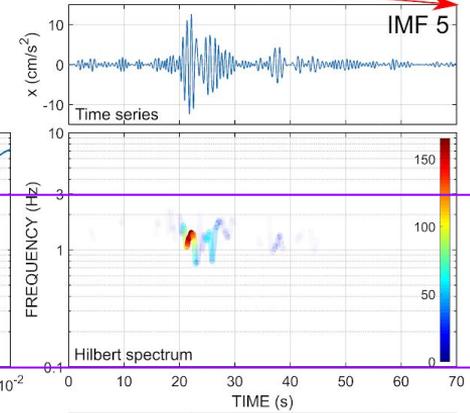
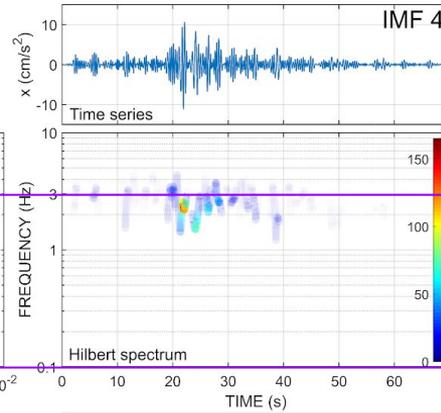
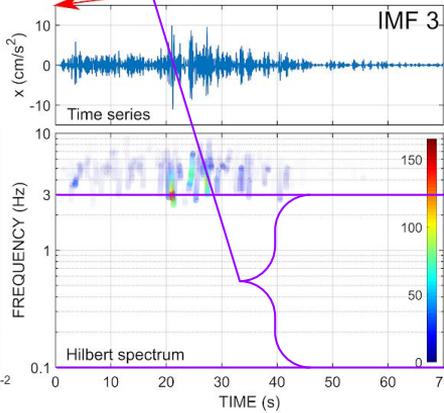
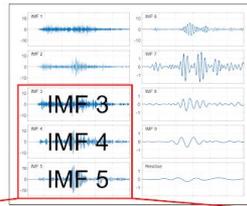


07 April 2011 Miyagi, M_w 7.1

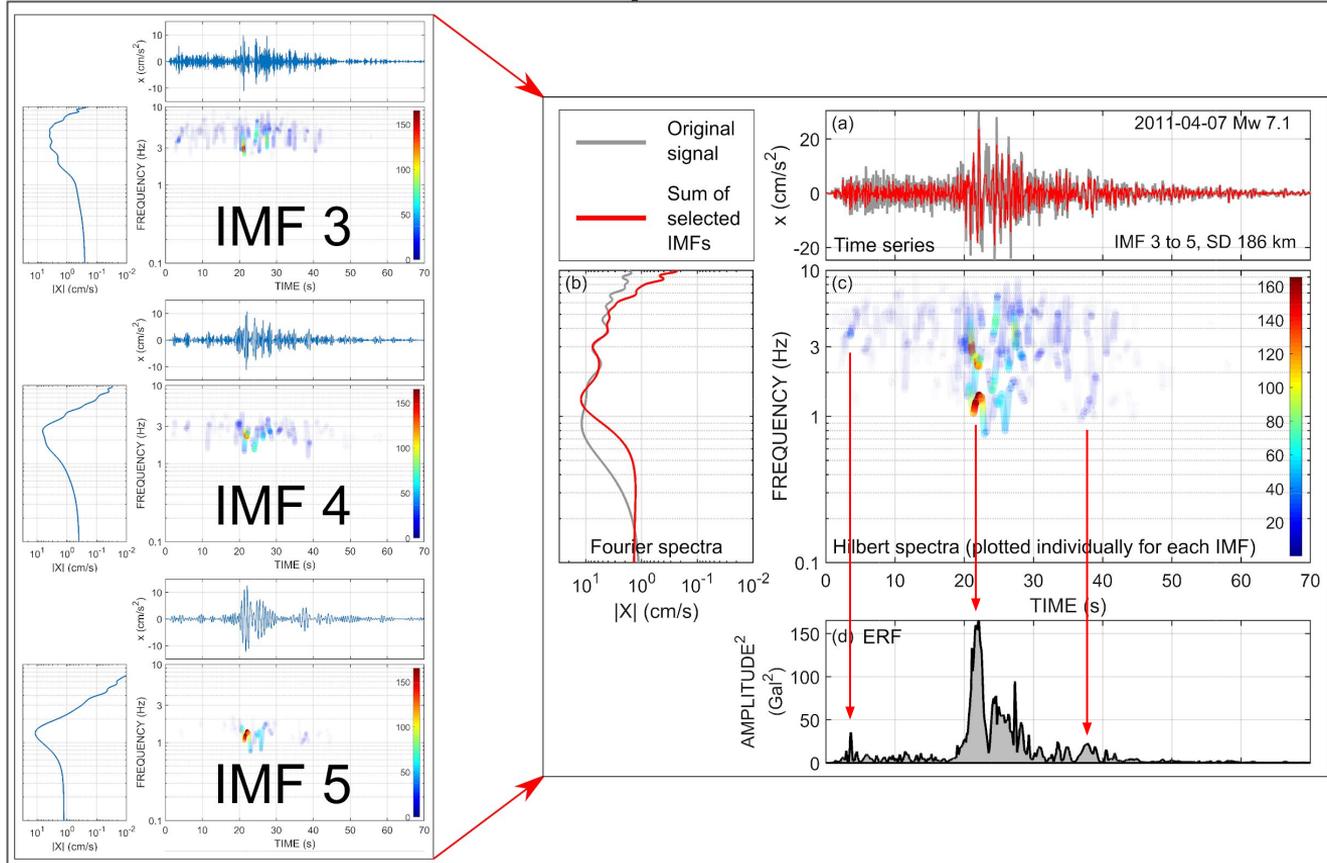


"Best" IMFs? Based on the frequency band, not the IMF number.

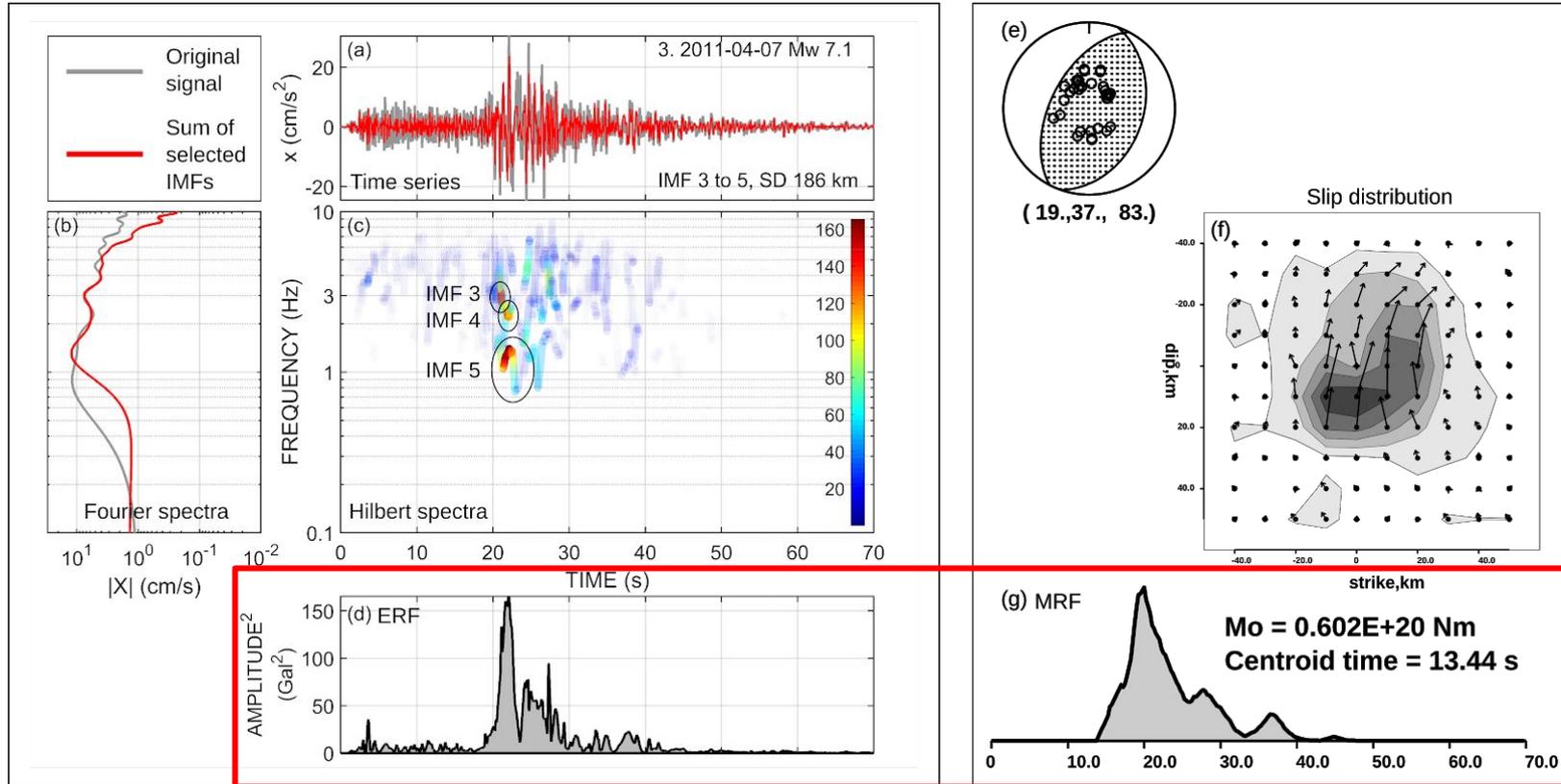
Frequency band
0.1 - 3 Hz



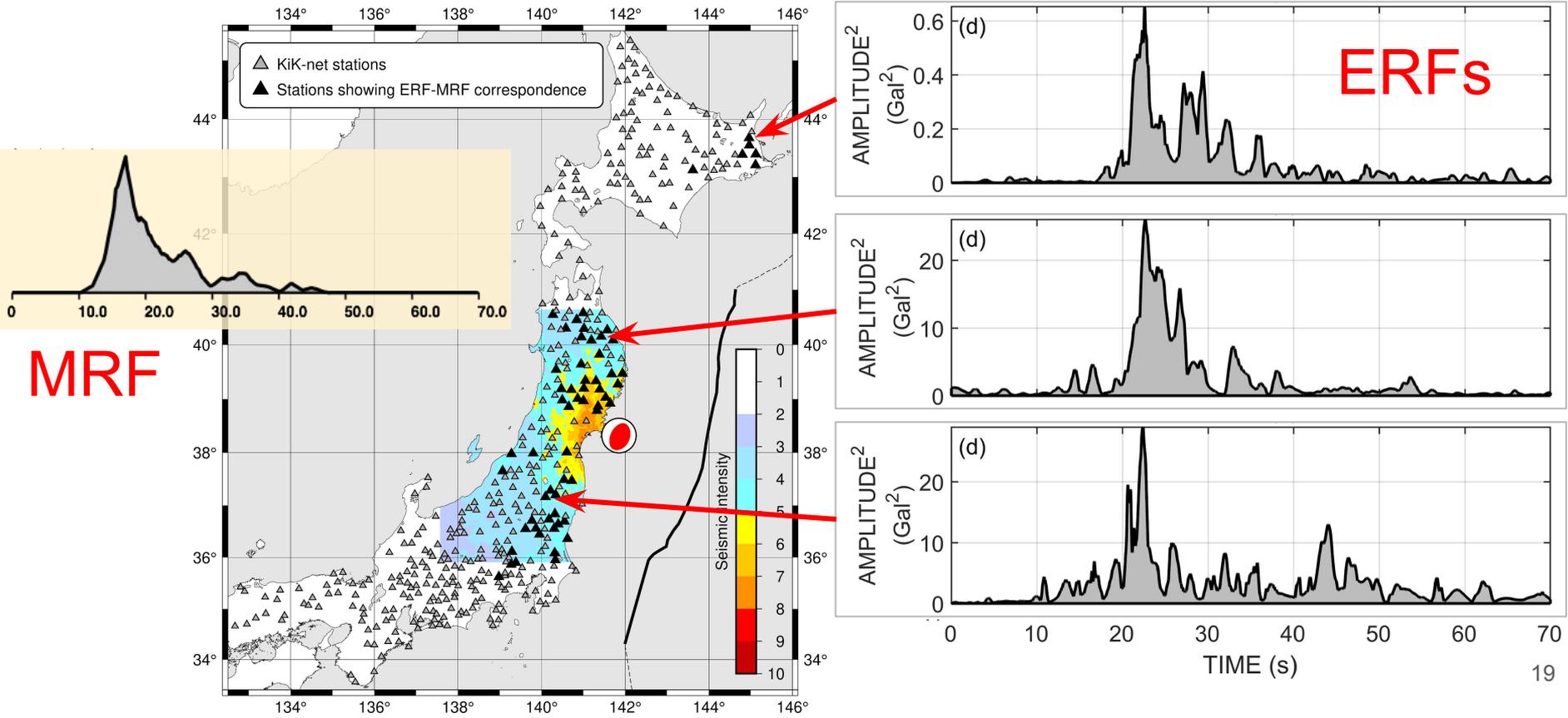
Generating an 'Energy Rate Function' by picking maximum energy values in the Hilbert spectra of the selected IMFs.



Correspondence of the ERF with the MRF, with a few caveats (Time-frequency analysis vs. Waveform inversion)



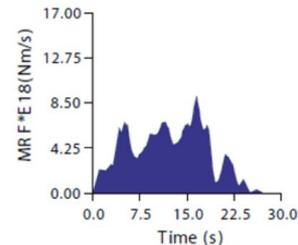
ERF-MRF correspondence observed at "best" stations (In the direction of rupture propagation and orthogonal to it).



ERF-MRF correspondence for other tectonic settings

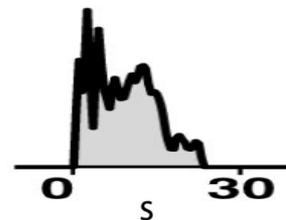
ERF-MRF correspondence for other tectonic settings

Interplate (2005 Miyagi-Oki): Complex rupture; rough ERF & MRFs.



Yaginuma et al.
(2006). *Earth, planets and space*,
58(12), 1549-1554.

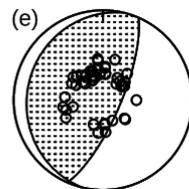
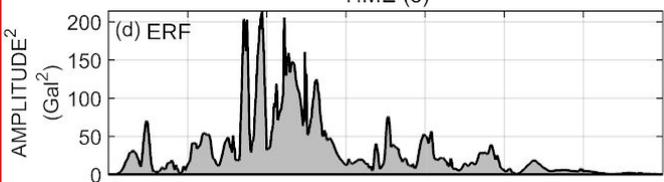
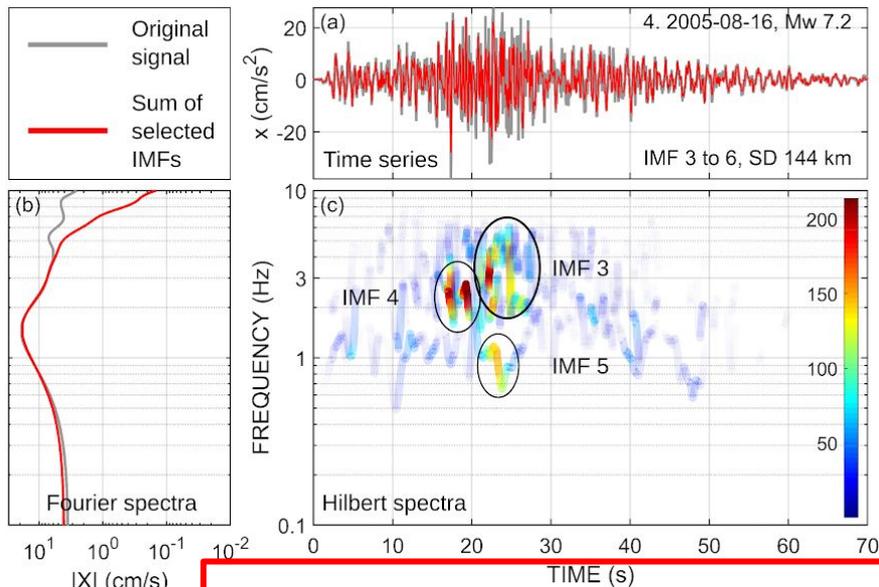
$M_0 = 0.9 \times 10^{20}$ Nm
Depth 36 km



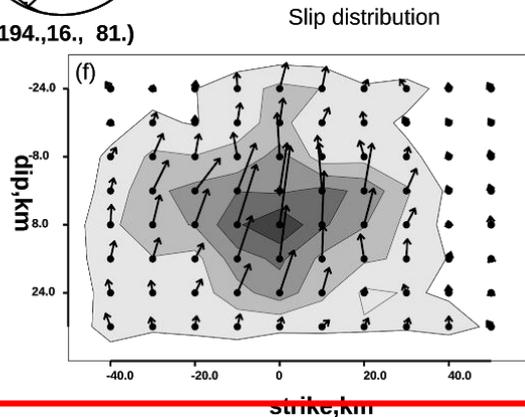
Lay et al. (2012).
JGR: Solid Earth,
117(B4).

ERF-MRF correspondence for other tectonic settings

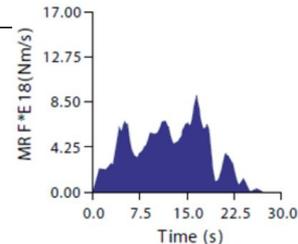
Interplate (2005 Miyagi-Oki): Complex rupture; rough ERF & MRFs.



(194, 16, 81.)

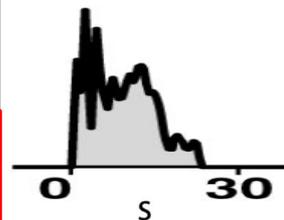


(g) MRF plot showing AMPLITUDE² versus TIME (s). The plot shows the moment rate function for the earthquake, with a peak around 14.24 s. The moment magnitude is $M_0 = 0.769E+20$ Nm and the centroid time is 14.24 s.



Yaginuma et al. (2006). *Earth, planets and space*, 58(12), 1549-1554.

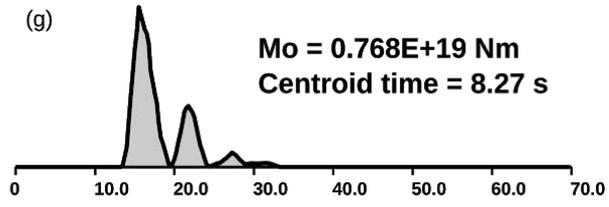
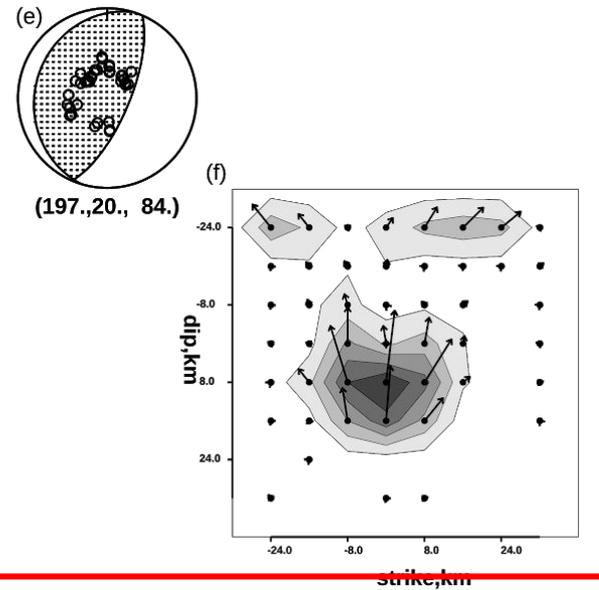
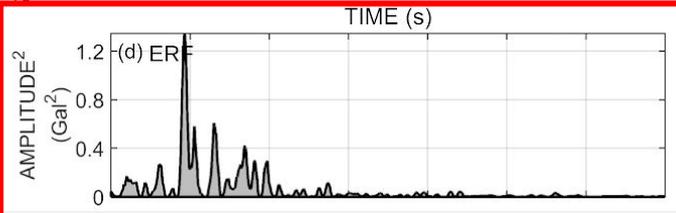
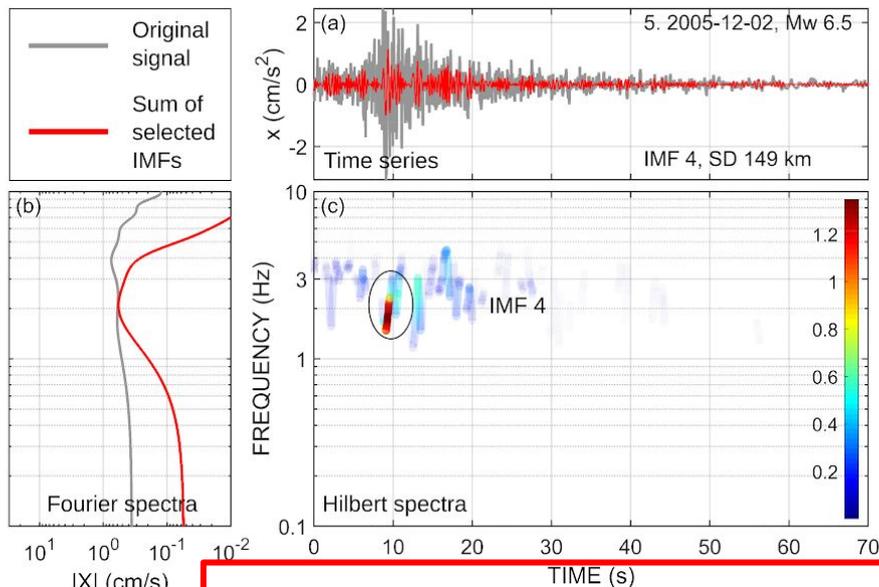
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Lay et al. (2012). *JGR: Solid Earth*, 117(B4).

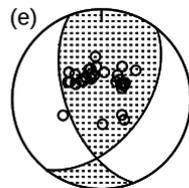
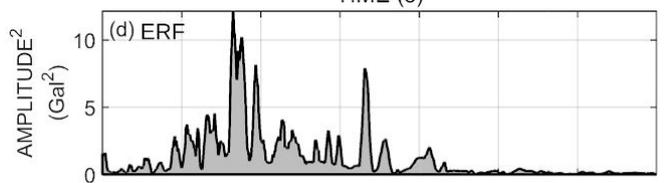
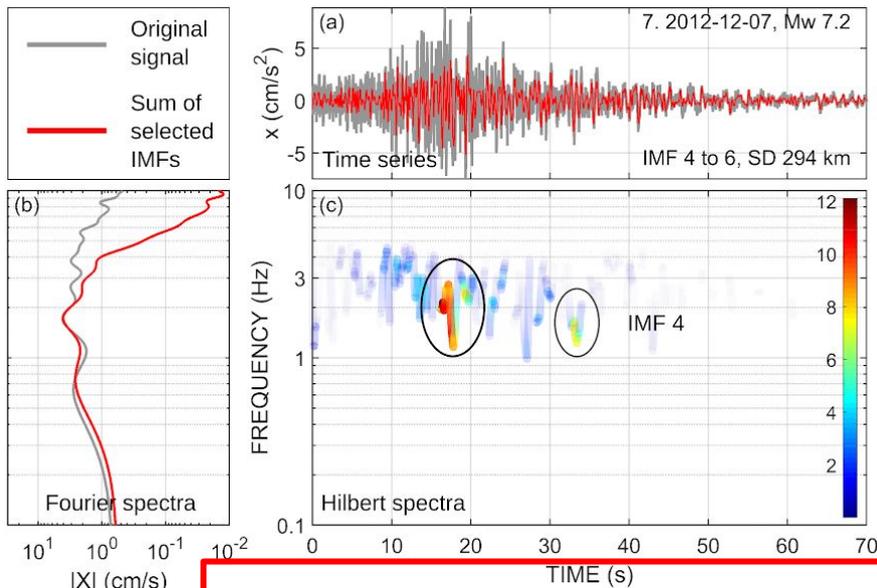
ERF-MRF correspondence for other tectonic settings

Interplate (2005 Honshu): Low seismic intensity stations; one IMF.

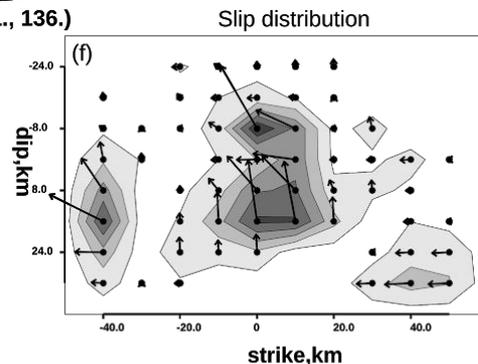


ERF-MRF correspondence for other tectonic settings

Intraplate (2012 Kamaishi): Complex rupture; 2 independent events



(38.51, 136.)



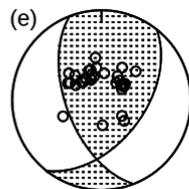
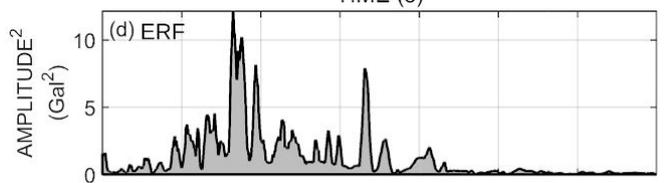
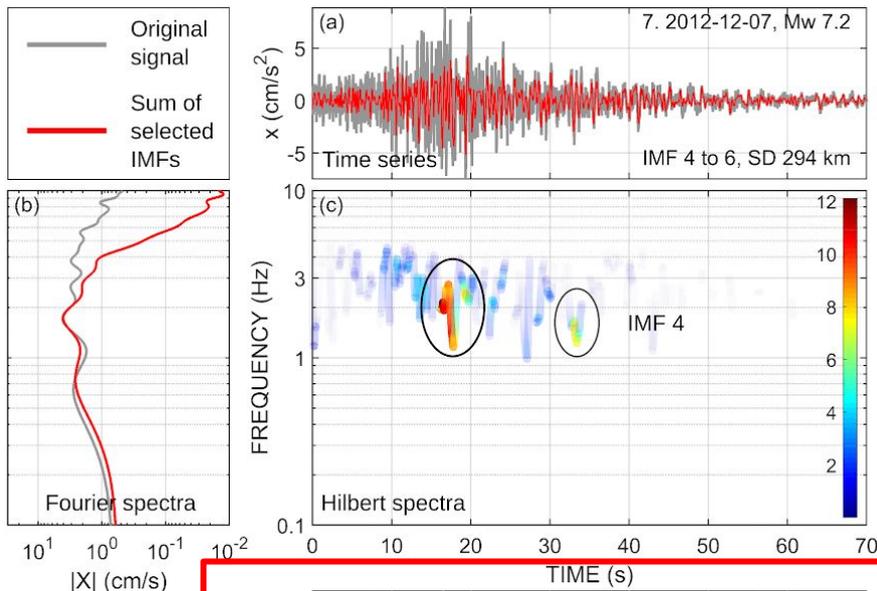
(g) MRF plot showing the amplitude squared in Gal^2 versus time in seconds. The plot shows two distinct peaks, indicating two independent rupture events. The y-axis ranges from 0 to 10, and the x-axis ranges from 0 to 70.0.

(g) MRF

$M_0 = 0.960E+20 \text{ Nm}$
Centroid time = 13.03 s

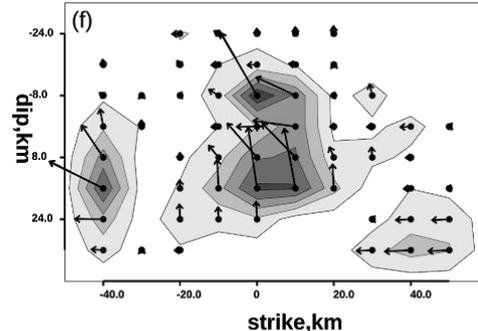
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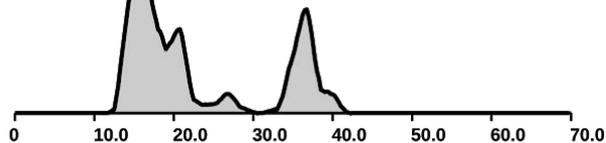
(38., 51., 136.)

Slip distribution

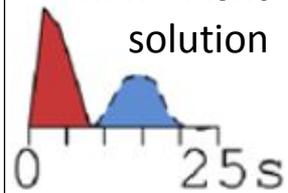


(g) MRF

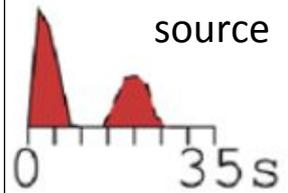
Mo = 0.960E+20 Nm
Centroid time = 13.03 s



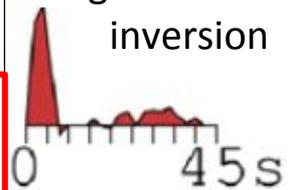
min.-misfit
solution



double thrust
source

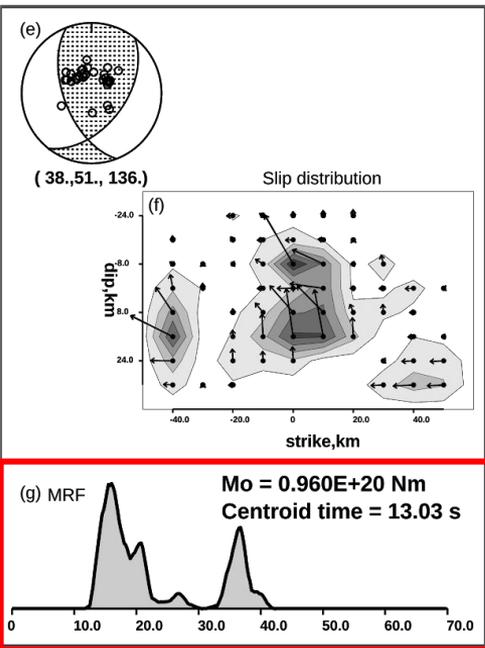


single-source
inversion

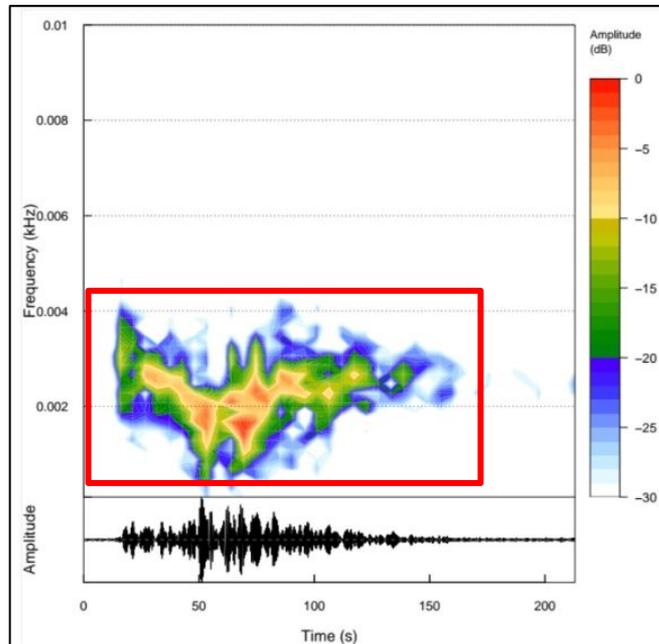


Craig, T. J., Copley, A., & Jackson, J. (2014). *GJI*, 197(1), 63-89.

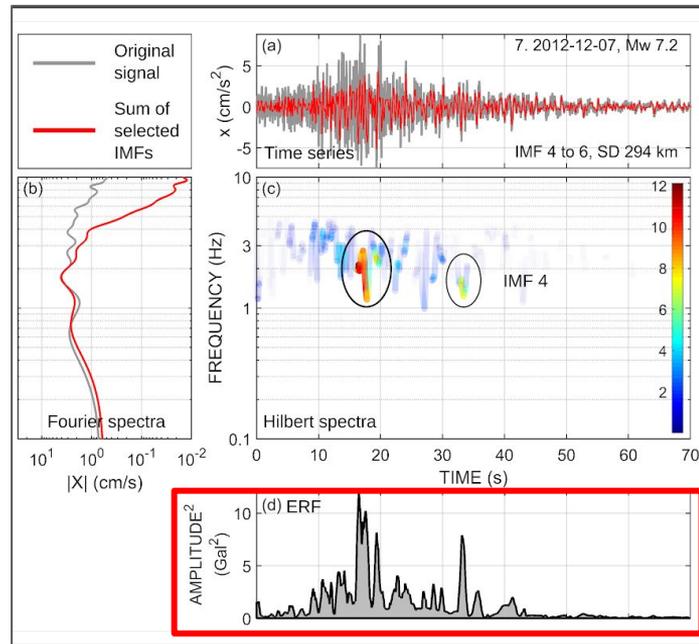
In conclusion, the combination of EMD with TFA tools is useful for quick interpretation of earthquake energy release.



Waveform inversion



Spectrogram (strong-motion)



HHT-ERF (strong-motion)