

Abstract

Climate change adaptation under resource constraints and future climate uncertainties would benefit from fully probabilistic climate risks assessments. Conducting such risk analyses requires assigning probabilities to the future greenhouse gases (GHG) and land-use scenarios used by global climate models. This paper proposes an approach to estimate the relative likelihood of carbon dioxide (CO₂) concentration scenarios used in key climate change modeling experiments. The approach relies on the comparison of CO₂ emissions from probabilistic simulations of Integrated Assessment Models (IAM) with compatible CO₂ emissions diagnosed by global climate models participating in the Coupled Model Intercomparison Project Phase 5 (CMIP5) and 6 (CMIP6). The approach is demonstrated with five emission simulations from four IAMs, leading to independent estimates of the relative likelihood of CMIP5 Representation Concentration Pathways and CMIP6' Shared Socioeconomic Pathways (SSP) up to 2100. Results suggest that SSP5-8.5 is an unlikely scenario for the second half of the century, but there is no clear consensus on the most likely scenario. Scenario likelihood is affected by a number of potential errors, including sampling errors, differences in emission sources simulated by the IAMs, and the lack of a common experimental framework for IAM simulations. These errors, along with the small IAM ensemble size, limit the applicability of the results. The delivery of fully probabilistic climate risk assessments would benefit from a coordinated probabilistic IAM experiment jointly designed with a coordinated climate modeling experiment where Earth System Model are driven by representative emission pathways.

Plain Language Summary

Climate model simulations are being increasingly used to understand future trends in the severity and frequency of impactful climate hazards and associated physical and socioeconomic risks. To run climate model simulations as part of large scale, coordinated climate projection exercises, climate models are provided with scenarios of greenhouse gases and land-use change over coming decades. However, the scenarios most widely used today for adaptation planning have no assigned probabilities; rather, they are explicitly intended to span a range of arbitrary climate futures. This reduces the applicability of resulting hazards projections for cost/benefit analysis of adaptation investments. To support risk-based adaptation decision making, this study combines five sets of probabilistic carbon dioxide emissions simulated by four Integrated Assessment Models (IAM) with

48 CMIP5 and CMIP6 climate model ensemble results to estimate the probability of future
49 GHG concentration and associated climate scenarios. The results are IAM-dependent,
50 though the majority of individual IAM-based analyses suggest that the high-emissions
51 scenario SSP5-8.5 becomes unlikely as we reach the second half of the century. Based
52 on lessons learned in this exercise, we propose that new sets of IAM and climate model
53 experiments be appropriately designed at their initial stages to better support proba-
54 bilistic climate change risk assessments.

55 1 Introduction

56 Future climate change impacts are captured in multi-model climate experiments
57 designed and coordinated through the Coupled Model Intercomparison Project (CMIP).
58 These climate modeling experiments explore, among other topics, the climate consequences
59 of rising greenhouse gases (GHG) concentrations in the atmosphere (Taylor et al., 2012).
60 Many decision-makers are now using these climate projections to assess hazards and make
61 consequential planning and investment decisions. In many instances however, risk as-
62 sessments are carried out without the benefit of a probabilistic framework quantifying
63 the leading sources of uncertainties affecting projections: climate and carbon cycle sen-
64 sitivity, natural variability, and future GHG emission and concentration scenarios.

65 While the climate community has been diligent in assessing and quantifying cli-
66 mate modelling uncertainties and natural variability (Lehner et al., 2020), and integrated
67 assessment studies routinely evaluate socio-economic uncertainties (Pastor et al., 2020;
68 Capellán-Pérez, 2016), there is very little guidance available regarding the relative prob-
69 abilities of GHG scenarios underpinning the climate change simulations typically used
70 to assess the impacts of climate change. In CMIP3, these transient climate change ex-
71 periments were driven by a family of GHG scenarios called SRES. Despite significant dif-
72 ferences across GHG SRES scenarios, the climate community has, by and large, avoided
73 commenting on their respective likelihood; a common stance has been to consider all emis-
74 sion scenarios as “equally valid with no assigned probabilities of occurrence” (Nakicenovic
75 et al., 2000). Murphy et al. (2009) explains that SRES scenarios have, by design, no as-
76 signed probability.

77 This reluctance to assign probabilities to GHG scenarios has carried into the fol-
78 lowing generations of GHG scenarios. In CMIP5, GHG concentration scenarios are de-

79 fined by Representative Concentration Pathways (RCPs), and “no likelihood or prefer-
80 ence is attached to any of the individual scenarios in the set” (van Vuuren et al., 2011).
81 The same non-commitment holds for CMIP6’ Shared Socioeconomic Pathways (SSPs)
82 (Riahi et al., 2017).

83 From the point of view of users of climate projections, this lack of guidance on the
84 probability of emission scenarios is however a serious impediment to judgment forma-
85 tion, risk analysis and ultimately, effective decision-making (Schneider, 2001; King et al.,
86 2015; Hieronymus, 2020). According to Morgan and Keith (2008): “If judgments about
87 likelihood are not supplied with the scenarios, they will be assumed by the users either
88 explicitly or implicitly. The convention of not communicating information about the rel-
89 ative likelihood of scenarios therefore muddies communication between analysts and users.”
90 A concrete example of this are stakeholders’ frequent requests for climate impacts based
91 on “business-as-usual” scenarios. IAM modelers may have no preference for one scenario
92 over the other, but most people will naturally assume that the continuation of histor-
93 ical trends is more likely than a change in the world’s socioeconomic dynamics. This in-
94 sistence on scenario-agnosticism leaves decision-makers, with no special expertise in GHG
95 scenarios, effectively responsible for assigning implicit or explicit likelihoods to future
96 scenarios in order to craft high-cost, high-consequences adaptation plans (Ho et al., 2019).

97 To be fair, the probability of GHG emission scenarios is not a question climate mod-
98 elers are well qualified to answer. The evolution of anthropogenic GHG emissions is in-
99 fluenced by policy, demography, economy, geopolitics and technology, topics well outside
100 the expertise of climate science. The description of these factors and their interactions
101 are captured by another class of model called Integrated Assessment Models (IAMs) (Sokolov
102 et al., 2005; Moss et al., 2010; Agrawala et al., 2011; Koomey et al., 2019)). The IAM
103 community generates hundreds of different scenarios, predicated on assumptions regard-
104 ing future climate policies, technological advances, demography and energy markets. It
105 is from these IAM simulations that the climate science community has drawn the GHG
106 and land-use scenarios underlying RCPs and SSPs. The selection of model inputs was
107 not meant to capture the most plausible scenarios, but rather to generate a sample of
108 *representative* pathways exploring the “full range of emission scenarios available in the
109 current scientific literature, with and without climate policy” (van Vuuren et al., 2011).

110 The IAMs used in CMIP experiments describe different *storylines*, but there are
111 other avenues to assess emission scenario uncertainties. Indeed, van Vuuren et al. (2008)
112 distinguish between storyline-based alternative scenarios and fully probabilistic scenar-
113 ios. Storylines embody fundamentally different, yet internally consistent, representations
114 of the future that can be represented by an IAM. Fully probabilistic scenarios are cre-
115 ated by assigning probability distributions to key IAM input parameters, and sampling
116 from those distributions to create a set of probabilistic emission pathways. The “condi-
117 tional probability approach” combines both storylines and probabilistic scenarios, argu-
118 ing that it is easier to define probability distributions for IAM parameters in the con-
119 text of a particular storyline.

120 Uncertainty analysis has been identified as one of the current key weaknesses of IAMs
121 (Pastor et al., 2020; Rogelj et al., 2017). For example, one contentious topic relates to
122 the parameterization of climate damages in cost-benefit IAMs. The family of cost-benefit
123 IAMs traditionally relies on median damages, overlooking the low and high tails of the
124 distribution for the climate sensitivity. A lower or higher climate sensitivity implies smaller
125 or larger climate hazards, and costs, for the same CO₂ concentration. If the climate sen-
126 sitivity distribution has “fat tails”, using the median estimate could bias cost assessments
127 (Ackerman et al., 2010; Keen, 2020; Stern, 2013; Weitzman, 2012). A related issue is the
128 possibility of tipping points in the climate system and their impact on damage functions
129 (Lontzek et al., 2015; Cai et al., 2016).

130 The need for quantitative probabilistic assessments of uncertainties was expressed
131 back in 2000 in a guidance document to Intergovernmental Panel on Climate Change (IPCC)
132 authors by Moss and Schneider (2000): “We believe it is more rational for scientists de-
133 bating the specifics of a topic in which they are acknowledged experts to provide their
134 best estimates of probability distributions and possible outliers based on their assessment
135 of the literature than to have users less expert in such topics make their own determi-
136 nations.” This comment was followed by the expectation that Bayesian approaches would
137 be most appropriate to describe inherently subjective degrees of belief in our assessment
138 of the state of science.

139 This view on the need for a Bayesian interpretation of uncertainties is often cited
140 in later papers looking into probabilistic emission scenarios. For example, M. D. Web-
141 ster et al. (2002), M. Webster et al. (2003), M. Webster et al. (2008) and M. Webster

142 et al. (2012) sampled an *a priori* parameter distribution of the Emissions Predictions
143 and Policy Analysis (EPPA) model to generate probabilistic GHG emission trajectories.
144 These emissions were then fed into the MIT Integrated Global System Model (IGSM)
145 to compute the posterior distribution for resulting temperature changes.

146 Schneider and Mastrandrea (2005), Sokolov et al. (2009) and Repetto and Easton
147 (2015) similarly assigned probability distribution to parameters of the DICE model to
148 assess the probability of *dangerous* anthropogenic interference with the climate system
149 and assess policy options. The authors stated: We do not recommend that our quanti-
150 tative results be taken literally, but we suggest that our probabilistic framework and meth-
151 ods be taken seriously: they produce relative trends and general conclusions that bet-
152 ter represent a risk-management approach than estimates made without probabilistic rep-
153 resentation of outcomes.”

154 Ward et al. (2012) define a simplistic supply-side model of fossil fuel production
155 to generate resource-constrained CO₂ emissions. Fossil fuel production is broken down
156 at the national level by fuel types. The model makes the hypothesis that known reserves
157 of conventional and unconventional fuel can and will be extracted. Production growth
158 rate is considered an uncertain parameter and sampled from a distribution, with an ini-
159 tial growth rate of 10% for all fuels not currently in production. Model assumptions are
160 deliberately biased toward high production growth, with the intent of outlining the up-
161 per structural limit to CO₂ emissions.

162 Gillingham et al. (2018) ran multiple IAMs to assess the relative contribution of
163 model structure and parametric uncertainty to future temperature, CO₂ concentration
164 and economic output. Model parameters for population, productivity and climate sen-
165 sitivity are sampled from *a priori* probability distribution drawn from the literature. This
166 multi-model approach allowed the authors to assess leading sources of uncertainty and
167 provide probability distributions for output variables.

168 This paper builds on these ideas and leverages outputs from published probabilis-
169 tic emission simulations to estimate the conditional probability for the CO₂ *concentra-*
170 *tion* scenarios within RCPs and SSPs. The paper targets the most popular CMIP tran-
171 sient climate change experiments, in which scenarios impose time-varying GHG concen-
172 trations to global climate models (GCM). Note that newer generation of Earth System
173 Models (ESM) can simulate carbon cycle processes, allowing them to be driven directly

174 with GHG *emissions*; such emission-driven experiments would lend themselves to a much
 175 simpler probabilistic analysis than what is described in this paper.

176 2 Data and Method

177 Contrary to a common misconception, coordinated climate change experiments typ-
 178 ically used in climate impacts studies are not driven by GHG *emission* scenarios, but
 179 use *prescribed* GHG *concentration* scenarios. This is done in part to give climate mod-
 180 els that cannot simulate the carbon cycle an opportunity to participate. For recent CMIP
 181 iterations, emission scenarios drawn from select IAM simulations are converted into con-
 182 centrations using a reduced complexity model called MAGICC (MAGICC6 for CMIP5
 183 (Meinshausen, Raper, & Wigley, 2011), and MAGICC7 for CMIP6 (Meinshausen et al.,
 184 2019)). These GHG concentrations are part of the boundary conditions prescribed to
 185 climate models, along with land-use scenarios, aerosol concentrations, etc. Note that there
 186 are other CMIP experiments where ESMs are driven by emission scenarios, but they usu-
 187 ally count fewer participating models and are currently rarely used in impact assessments.
 188 This will likely change as more models include carbon cycle processes allowing them to
 189 be driven directly by emissions. Figure 1 illustrates how CMIP5 RCP experiments are
 190 tied to IAM emission scenarios.

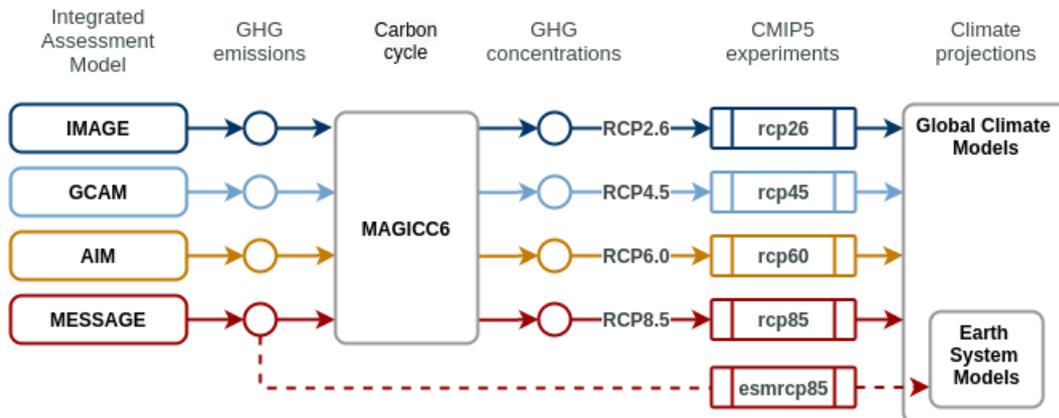


Figure 1. In CMIP5 RCP experiments, global climate models are prescribed greenhouse gas concentrations estimated by MAGICC6 from emission scenarios simulated by four different IAMs: IMAGE, GCAM, AIM and MESSAGE. In contrast, in the `esmrcp85` experiment, ESMs are prescribed GHG emissions directly and use their own carbon cycle processes to compute concentrations. Although details differ, the experimental setup for CMIP6 is conceptually similar.

191 An RCP or SSP scenario is a short-hand to describe an elaborate experimental de-
 192 sign, of which the GHG concentration trajectories is just one component (Eyring et al.,
 193 2015). Climate modeling teams set up their model following this experimental design,
 194 run one or many simulations (realizations), and then archive model outputs according
 195 to precise data and metadata specifications meant to facilitate model intercomparisons.
 196 Model outputs include hundreds of different variables, from which many climate hazards
 197 can be derived: heatwaves, sea level rise, annual maximum precipitation, droughts, etc.
 198 To quantify uncertainties, climate impact studies typically include results from multi-
 199 ple realizations from multiple models driven by multiple GHG concentration scenarios.
 200 With these results in hand, a legitimate question by decision-makers could be for exam-
 201 ple: “considering known uncertainties, what is the probability of precipitation exceed-
 202 ing a given threshold over the period 2030–2050?”

203 2.1 Probabilistic Framework to Assess Climate Hazards

204 Let’s denote a climate hazard as H . Risk analysts and decision makers are inter-
 205 ested in $P(H(t))$, the probability of occurrence of hazard H at some time t in the future.
 206 To lighten the presentation, time dependence t is implicitly assumed in the next equa-
 207 tions. Note also that we’re using the term *probability* to denote a subjective degree of
 208 belief in an hypothesis, not a frequency of occurrence.

209 What CMIP experiments can provide is a probability *conditional* on the experi-
 210 mental design or scenario. If we let S stand for a CMIP scenario, including GHG and
 211 aerosols concentrations, initial conditions, etc., then climate model simulation ensem-
 212 bles can be used to compute $P(H | S)$, the probability of a climate hazard H condi-
 213 tional to the scenario S .

214 Although in principle CMIP offers multiple scenarios to draw from, the climate im-
 215 pact community has mostly relied on concentration-driven scenario experiments. For CMIP5,
 216 these include `rcp26`, `rcp45`, `rcp60`, `rcp85`, which we’ll denote as $\mathbf{S}_{\text{CMIP5}}$, the set of concentration-
 217 driven CMIP5 RCP experiments. For CMIP6, there are nine such ScenarioMIP exper-
 218 iments, but participating models are minimally expected to contribute simulations to Tier
 219 1 experiments: $\mathbf{S}_{\text{CMIP6}} = \{\text{ssp126}, \text{ssp245}, \text{ssp370}, \text{ssp585}\}$ (O’Neill et al., 2016). If
 220 we assume that the future climate will be captured by those sets of scenarios, then the
 221 hazard probability can be estimated by a weighted average of conditional hazard prob-

222 abilities:

$$223 \quad P(H) \approx \sum_{S \in \mathbf{S}} P(H | S)P(S), \quad (1)$$

224 where the weights $P(S)$ are the Bayesian *prior* for each scenario.

225 The first term on the right hand side of Eq. (1) is what climate impact studies rou-
 226 tinely compute. Its computation can be as simple as a fit of a normal distribution to the
 227 hazards simulated by a multi-model ensemble, or can include considerations regarding
 228 model performance or model independence (Knutti et al., 2017). Our focus in this pa-
 229 per is with the second term, the probability of a given RCP or SPP scenario, or how likely
 230 are the future conditions described in each scenario S . A full answer to this question would
 231 require an evaluation of the joint probability of all scenario components: concentration
 232 trajectory for each individual GHG, land-use changes, aerosols, solar forcing, etc. To re-
 233 duce the scope of the problem, we evaluate the scenario likelihood based only on the global
 234 CO_2 trajectory and ignore the influence of other scenario components.

235 This paper makes the claim that the scenario probability can be estimated condi-
 236 tionally to a set of probabilistic IAM emissions: $P(S) \equiv P(S | \mathbf{E}_{\text{IAM}})$. Using Bayes'
 237 theorem, and assuming RCPs and SSPs can be represented solely by their global CO_2
 238 concentrations C_S , we get

$$239 \quad P(S | \mathbf{E}_{\text{IAM}}) = \frac{P(\mathbf{E}_{\text{IAM}} | S)P(S)}{P(\mathbf{E}_{\text{IAM}})} \\ 240 \quad \propto P(\mathbf{E}_{\text{IAM}} | C_S)P(S). \quad (2)$$

241 The second term on the right-hand side of Equation (2) is the prior for the scenario. It
 242 can be set subjectively by the risk analyst, or calculated based on other evidence. The
 243 next section discusses how to compute the first term, the likelihood of probabilistic emis-
 244 sions given the scenario CO_2 concentration.

245 2.2 Likelihood of Emission Trajectories

246 In Eq. (2), the likelihood term $P(\mathbf{E}_{\text{IAM}} | C_S)$ stands for the probability of CO_2
 247 emission trajectories given a known CO_2 concentration scenario. Comparing concentra-
 248 tions and emissions implies a mechanism to convert one into the other. RCP and SSP
 249 scenarios use the MAGICC model to convert emissions into concentrations, but doing
 250 so here would dismiss carbon cycle uncertainties that are already partially neglected by
 251 concentration-driven experiments (van Vuuren et al., 2011).

252 The approach chosen here is to convert concentrations into *compatible emissions*.
 253 Compatible emissions are the anthropogenic fossil fuel emissions that balance carbon fluxes
 254 between the air, land and ocean when ESM are prescribed a given CO₂ pathway. Indeed,
 255 climate models simulate CO₂ exchanges between the atmosphere, land and ocean. If c_a, c_o
 256 and c_l stand respectively for the carbon stored in the atmosphere, the ocean and the land
 257 surface, then carbon emissions from fossil fuels e modify the total carbon budget:

$$258 \quad e = \frac{\partial c_a}{\partial t} + \frac{\partial c_o}{\partial t} + \frac{\partial c_l}{\partial t}. \quad (3)$$

259 The first term on the right is the time derivative of the CO₂ concentration pathway used
 260 in the experimental design, and the other terms on the right are the carbon fluxes from
 261 the atmosphere into the ocean and land. These fluxes are simulated and archived by cli-
 262 mate models, allowing us to compute e , the *compatible emissions* that would have led
 263 to the concentrations imposed by the experimental design. Differences in the carbon cy-
 264 cle representation of ESMs such as vegetation dynamics, fire-carbon interactions or ocean
 265 biochemistry, appear as inter-model spread in compatible emissions. Compatible emis-
 266 sions are computed for CMIP5 in Jones et al. (2013), and for CMIP6 in Liddicoat et al.
 267 (2021). In the latter, mean fluxes during the preindustrial period are removed from fluxes
 268 over the historical and future scenarios to correct for the fact that some ESMs have not
 269 reached equilibrium.

270 Carbon dioxide emissions compatible with prescribed concentrations are estimated
 271 for the CMIP5 and CMIP6 Tier 1 experiments following the methodology from Liddicoat
 272 et al. (2021). All model simulations for which both `fgco2`, the gas exchange carbon flux
 273 into the ocean, and `nbp`, the carbon flux from the atmosphere into the land, were avail-
 274 able on the Earth System Grid Federation and free from defects are used (the number
 275 of simulations available per model are listed for CMIP5 and CMIP6 in Tables A1 and
 276 A2 respectively). Global fluxes are computed by multiplying ocean and land fluxes by
 277 the respective fractional ocean area (`sftof`) and land area (`sftlf`) as well as the respec-
 278 tive grid cell area (`areacello`, `areacella`), and summing over the entire globe. Annual
 279 fluxes are entered into Equation (3) along with numerically differentiated RCP (Meinshausen,
 280 Smith, et al., 2011) and SSP concentrations (Riahi et al., 2017; Gidden et al., 2019), yield-
 281 ing annual compatible CO₂ emission time series shown in Figure 2. In cases where prein-
 282 dustrial simulations (`piControl`) are available, the mean compatible emissions over the
 283 last 30 years of the preindustrial period (see Tables B1 and B2) are subtracted from his-
 284 torical and future emissions.

285 For each RCP and SSP experiment, we thus have an ensemble of emissions that
 286 are compatible with the CO₂ concentration scenario. If we assume that the probability
 287 density of those compatible emissions can be described by a normal distribution, tak-
 288 ing the mean $\mu_S(t)$ and variance $\sigma_S^2(t)$ of diagnosed emissions for each scenario S lets
 289 us define a time dependent functional form for the IAM emission likelihood:

$$290 \quad P(\mathbf{E}_{\text{IAM}} | C_S) \equiv \mathcal{N}(\mathbf{E}_{\text{IAM}} | \mu_S, \sigma_S). \quad (4)$$

291 To account for the varying number of realizations per model, ensemble statistics are first
 292 evaluated across realizations for each model, then across models within each experiment.
 293 More explicitly, if $e_{S,m,r}$ stands for compatible emission from experiment S , model m
 294 and realization r , and if $E_d[X]$ and $V_d[X]$ stand for the average and variance over dimen-
 295 sion d respectively, then

$$296 \quad \mu_S = E_m[E_r[e_{S,m,r}]],$$

$$297 \quad \sigma_S = \sqrt{V_m[E_r[e_{S,m,r}]] + E_m[V_r[e_{S,m,r}]]}.$$

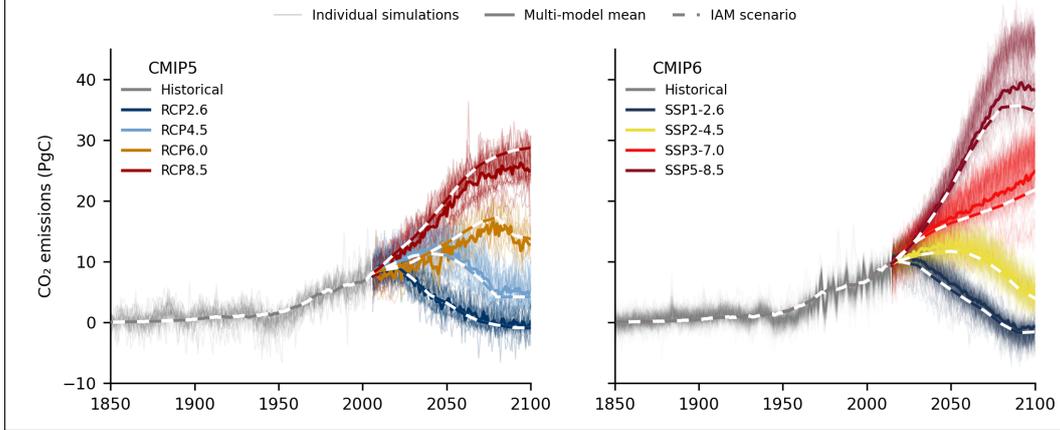


Figure 2. Compatible fossil CO₂ emissions diagnosed from CMIP5 (left) and CMIP6 (right) simulations from historical (gray) and future (color) scenarios. Thin lines denote individual model simulations, thick solid lines the multi-model mean for each experiment, and thick dashed lines the IAM scenario fossil fuel emissions. Note that the mean is not always centered relative to individual simulations, because the mean is first calculated over ensemble members, then over individual models. This is especially visible in the right panel for SSP5-8.5, where a cluster of 50 CanESM5 simulations reaches much higher compatible emission values than other ESMs.

298 Table 1 shows the total number of simulations and models available to compute those
 299 statistics for CMIP5 and CMIP6. Note that for RCP6.0, only seven different models were
 300 available.

Table 1. Number of simulations and models with at least one simulation available for each CMIP5 and CMIP6 experiment. For a break-down per model, see Tables A1 and A2.

	Historical	RCP2.6	RCP4.5	RCP6.0	RCP8.5
Model name					
Simulations	35	23	27	10	27
Models	13	11	13	7	13

	Historical	SSP1-2.6	SSP2-4.5	SSP3-7.0	SSP5-8.5
Model name					
Simulations	233	121	155	131	112
Models	22	17	16	18	16

301 2.3 Probabilistic IAM Emission Simulations

302 Probabilistic emission simulations are taken from five different papers, two of those
 303 using the same IAM. These papers were selected opportunistically based on two main
 304 criteria: ensembles of probabilistic CO₂ emission time series up to 2100 were available
 305 publicly or from the authors, and the simulations did not explicitly constrain emissions
 306 to meet policy ambitions. Note that these IAMs were not necessarily intended to yield
 307 *predictive* emissions, hence results derived from those simulations should be not be in-
 308 terpreted too literally. They are used here mainly to illustrate the potential of proba-
 309 bilistic IAM simulations to inform climate risks. To lighten the text, each paper is iden-
 310 tified by an abbreviation.

311 Fyke and Matthews (2015) [FM15] have developed a reduced-form numerical car-
 312 bon emission model based on differential equations describing the exchange of carbon
 313 between geological and exogenous (atmosphere, ocean and biosphere) reservoirs. The fluxes
 314 between those reservoirs depend on extraction and consumption rates, which in turn de-
 315 pend on availability and prices for fossil fuel and its alternatives. The model counts 28

316 parameters, 17 of which have significant uncertainty. For each of these uncertain param-
 317 eter, a probability distribution describing its uncertainty was defined based on published
 318 estimates and expert judgment. The parameters were sampled ($n=100,000$) from their
 319 prior distributions using a latin hypercube sampler, and time series (2012–2100) of car-
 320 bon emissions generated from the model equations (Figure 3). The parameters whose
 321 uncertainty had the greater impact on emissions are the minimum future non-fossil en-
 322 ergy cost, the maximum size of potential fossil energy resources and the maximum po-
 tential carbon pricing.

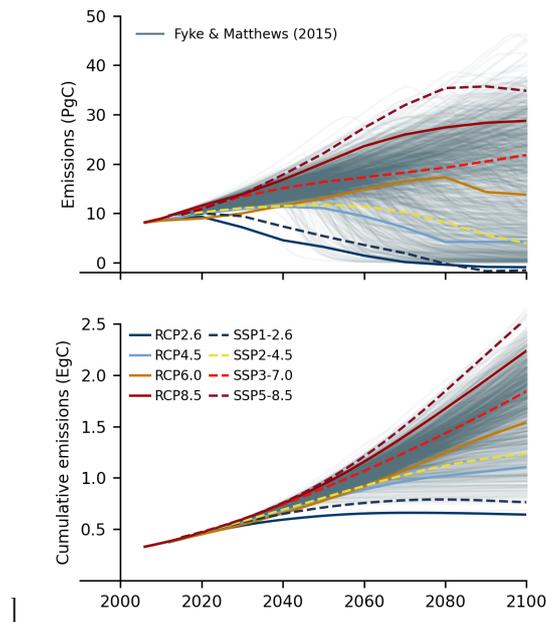


Figure 3. Stochastic emissions and cumulative emissions from Fyke and Matthews (2015) (gray), overlaid with IAM emissions from CMIP5 RCPs (solid lines) and CMIP6 SSPs (dashed lines).

323

324 Capellán-Pérez et al. (2016) [CP16] leverage the GCAM IAM, combined with a prob-
 325 abilistic assessment of recoverable energy resources, supply-cost curves and climate sen-
 326 sitivity, to analyze the relative importance of these factors in the temperature response
 327 at the end of the century. The study focuses on energy availability considerations, us-
 328 ing the “remaining ultimately recoverable resources” (RURR) approach to estimate non-
 329 renewable energy sources. It uses a Monte Carlo approach, where uncertain parameters
 330 are sampled ($n=1,000$) from their respective *prior* distribution, and then fed into GCAM-
 331 MAGICC to obtain CO_2 emissions (Figure 4), total radiative forcing and the global tem-

332 perature response over the period 2005–2100. GCAM-MAGICC is run in baseline mode,
 333 meaning that no climate policy are imposed. The results reveal that the coal RURR un-
 334 certainty is the determinant factor among fossil fuel resources considered. It also shows
 335 that not accounting for the values in the upper ranges of fossil fuel availability can lead
 to an underestimate of total radiative forcing by the end of the century.

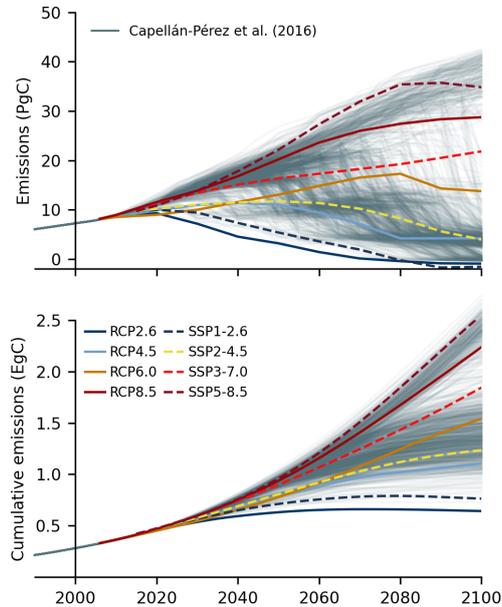


Figure 4. Stochastic emissions and cumulative emissions from Capellán-Pérez et al. (2016) (gray), overlaid with IAM emissions from CMIP5 RCPs (solid lines) and CMIP6 SSPs (dashed lines). Note that the abrupt jumps in the emission time series are likely due the lack of geological constraints to fossil fuel extraction rates. Non-renewables availability is modeled using supply-cost curves, and when a resource is depleted, its extraction drops to zero the following year.

336

337 Raftery et al. (2017) [R17] propose a model based on the country-level Kaya iden-
 338 tity, where the future carbon emissions of a country are given by the product of popu-
 339 lation, gross domestic product (GDP) per capita and carbon intensity (carbon emitted
 340 by GDP). Probabilistic population projections up to 2100 are taken from United Nations
 341 (2015), reflecting data up to 2015. A joint Bayesian hierarchical model for the GDP and
 342 carbon intensity is calibrated on data from 1960–2010. The model assumes an evolving
 343 world technology frontier, to which countries' GDP converge at country-specific rates,
 344 and that all countries have reached a carbon intensity peak and are now on a declining
 345 trend. Model parameters are sampled by Monte Carlo ($n=100,000$) and the distribution

346 of emissions (Figure 5) analyzed to assess the relative importance of population (2%),
 347 GDP (50%) and carbon intensity (48%). The model does not include explicit future cli-
 348 mate policies, but the fact that model parameters are calibrated on historical data en-
 349 sures that the influence of past and current policies are included in future projections.

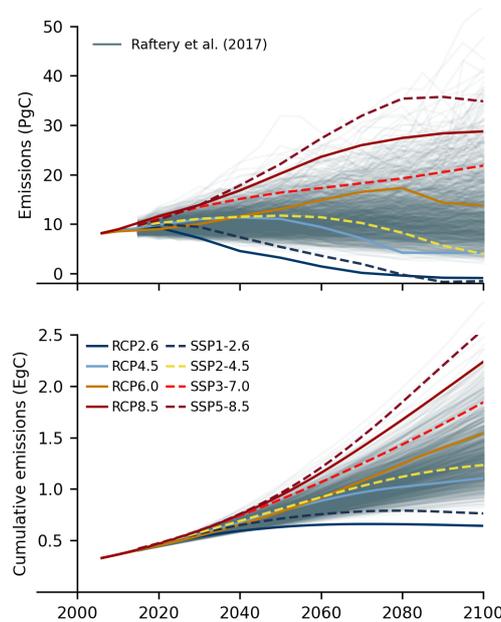


Figure 5. Stochastic emissions and cumulative emissions from Raftery et al. (2017) (gray), overlaid with IAM emissions from CMIP5 RCPs (solid lines) and CMIP6 SSPs (dashed lines).

350

351 Liu and Raftery (2021) [LR21] uses the same model as Raftery et al. (2017), but
 352 with five additional years of population (United Nations, 2019), economic and emission
 353 data. Slower growth in emissions between 2010–2015, compared to 1960–2010 period,
 354 explains the lower global annual emissions (Figure 6).

355 Capellán-Pérez et al. (2020) [CP20] describe the MEDEAS-W IAM developed in
 356 the course of the homonymous EU project (Modeling Energy System Development un-
 357 der Environmental and Socioeconomic constraints). The model counts nine modules: econ-
 358 omy, energy demand, -availability, -infrastructures and -return on energy invested, min-
 359 erals, land-use, water, climate/emissions, and social and environmental impact indica-
 360 tors. The model is meant to inform decision-making regarding the transition to sustain-
 361 able energy systems, and grants considerable attention to biophysical constraints to growth

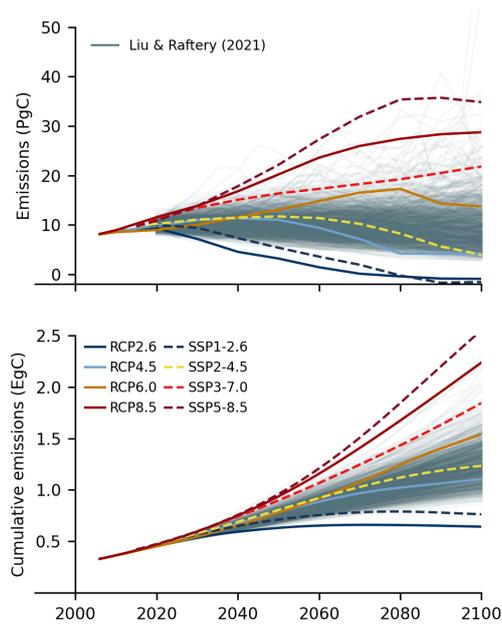


Figure 6. Stochastic emissions and cumulative emissions from Liu and Raftery (2021) (gray), overlaid with IAM emissions from CMIP5 RCPs (solid lines) and CMIP6 SSPs (dashed lines).

362 and energy availability, mineral and energy investments for energy shifts, sectoral eco-
 363 nomic structure, and climate change damages. The model accounts for the character-
 364 istics of 25 energy sources and technologies, including reserves, extraction rate, intermit-
 365 tency of some renewable energy sources and requirements for storage and overcapacity.
 366 The model assumes technological improvements at economic sectoral and technologies
 367 level, but also constraints to the potential for renewables due to for example lower qual-
 368 ity siting and thermodynamical limits to generation efficiency. A non-linear climate dam-
 369 age function affects production and growth rate, consistent with the interpretation of “dan-
 370 gerous climate change” beyond CO_2 concentration thresholds. Monte-Carlo simulations
 371 ($n=1,000$) are run to perform an uncertainty analysis for 72 inputs. CO_2 emissions (1995–
 372 2100) simulated for the reference (Ref) scenario (a conditional probability approach based
 373 on the business-as-usual storyline) are shown in Figure 7.

374 Comparing and contrasting the above studies highlights several themes. Firstly,
 375 it is notable that each of the studies make contrasted model choices. For example, R17
 376 and LR21 construct a data-driven statistical model framework that applies the simple
 377 Kaya identity at multiple points of time to develop emission time series. In contrast, FM15,
 378 CP16 and CP20 use more sophisticated time stepping numerical models with inherent

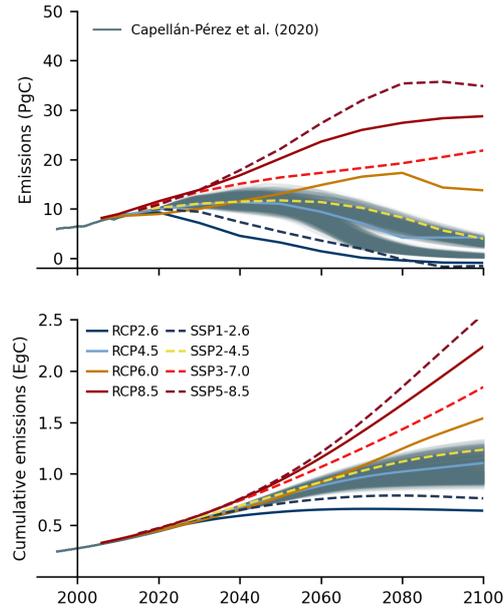


Figure 7. Stochastic emissions and cumulative emissions from Capellán-Pérez et al. (2020) (gray), overlaid with IAM emissions from CMIP5 RCPs (solid lines) and CMIP6 SSPs (dashed lines).

379 system dynamics, albeit with very different numerical methods: FM15 treat the global
 380 fossil fuel resource volume as an endogenous model component, whereas CP16 treat the
 381 same as an exogenous input variable and focus numerical efforts on estimating prices con-
 382 sistent with cleared markets, a concept which is entirely absent in the FM15 approach.
 383 In CP20, the total amount of reserves is fixed, but the extraction rate is subject to phys-
 384 ical constraints (maximum extraction curves).

385 Secondly, the studies described here apply notably different methods to sample ex-
 386 ogenous inputs to the respective model frameworks. R17 arguably dedicate the most ef-
 387 fort towards this aspect, in applying a hierarchical (multi-level) Bayesian model frame-
 388 work approach for estimating modeled input parameters. Indeed, the term “model” in
 389 their study primarily applies to the statistical models which derive the inputs for the Kaya
 390 Identity relationship, rather than the functional equation itself. In contrast, FM15 use
 391 relatively simpler sampling of a larger number of uncertain, scalar, model parameters based
 392 on a normal distribution-weighted latin hypercube sampling approach that does not dis-
 393 criminate potential interdependencies between parameters. Providing further contrast,
 394 CP16 sample input parameters from empirical distribution functions for key input pa-

395 rameters, with distribution functions for important input parameters developed from avail-
396 able published literature values. In CP20, 72 uncertain parameters are sampled from uni-
397 form distributions, with ranges that go from $\pm 20\%$ around the reference scenario for most
398 parameters, to $\pm 50\%$ or even $[-50\%, +100\%]$ for the most uncertain parameters. As with
399 model design diversity, there is significant long-term potential for convergent evolution
400 towards optimal input parameter sampling practices, but also short-term challenges in
401 comparing inter-study results because of differences in both sampled parameters, and
402 statistical sampling methods.

403 A critical difference across studies is the definition of CO₂ emissions and the pro-
404 cesses that contribute to them. FM15 simulate emissions from fossil fuel combustion only,
405 while R17 and LR21 also include cement production. CP16 emissions account for indus-
406 trial processes, fossil fuel combustion and land-use change, and in CP20 losses from en-
407 ergy transformation and distribution are included as well.

408 Despite model methodological differences, there are also several fundamental sim-
409 ilarities between the studies. Per selection criteria, all papers adopted methodologies for
410 model design and simulation production that avoided any predefinition of final results
411 to which the model simulations are forced to meet (so-called “perfect foresight” or “pol-
412 icy optimization” modeling). This contrasts fundamentally with the RCP and SSP sce-
413 nario families which are constrained by design to match radiative forcing levels in 2100.
414 It also contrasts with scenarios exploring pathways consistent with avoidance of exceedance
415 of particular temperature thresholds (*e.g.* 2°C above preindustrial temperature). Avoid-
416 ing the “perfect foresight” approach is a necessary precondition for any fully-scoped prob-
417 abilistic assessment of future emissions, because it allows probabilistic assessments to de-
418 velop in a free-running manner without a priori constraints on final emission levels, ra-
419 diative forcing anomalies, or temperature targets.

420 A second similarity between studies is their focus on evaluating the likelihood of
421 exceeding global temperature thresholds, and its sensitivity to various factors. FM15 de-
422 scribe the long-term likelihood of exceeding various global temperature change levels.
423 Beyond the climate response to cumulative emissions, these likelihoods are most sensi-
424 tive to minimum non-fossil energy prices, maximum fossil energy resources and maxi-
425 mum carbon price. R17 focus on the likelihood of exceeding the 2°C threshold by 2100,
426 with results that are largely influenced by the gross domestic product per capita and car-

427 bon intensity, and much less by population growth uncertainty. LR21 conduct a country-
428 level analysis, estimating the likelihood that countries will meet their nationally deter-
429 mined contributions, and keep warming below 2°C. CP16 describe the likelihood of sur-
430 passing RCP emissions levels by 2100 and crossing the 2°C warming threshold in 2100.
431 A sensitivity analysis covering resource related uncertainties indicate the dominant source
432 of uncertainty are the remaining ultimately recoverable coal resources. CP20 is primar-
433 ily devoted to the description of the MEDEAS modeling framework, and uses its Monte
434 Carlo simulations to assess the robustness of the results, rather than estimate the prob-
435 ability of outcomes.

436 2.4 Annual vs Cumulative Emissions

437 Key climate change features, such as global air temperature change, surface ocean
438 temperature rise and sea level rise are nearly linearly related to cumulative emissions (Matthews
439 et al., 2009; Williams et al., 2012). Given our objective is to assess the probability of such
440 climate impacts, it makes sense then to compute Eq. (4) on cumulative emissions rather
441 than annual emissions. This however complicates the analysis, because results now hinge
442 on the year from which we start cumulating emissions.

443 Historical CMIP5 and CMIP6 experiments start in 1850, while future scenarios start
444 in 2006 for CMIP5 and 2015 for CMIP6. On the other hand, the five probabilistic IAM
445 emissions simulations presented above start in 1990, 1995, 2010, 2012 and 2015. To align
446 all results to a common starting point, all emissions are accumulated from 1750 onward,
447 using observations taken from the Global Carbon Budget project (Friedlingstein et al.,
448 2020) to fill gaps. For example, probabilistic cumulative emissions from FM15, starting
449 in 2012, are incremented by the 2011 observed cumulative emission. Diagnosed compat-
450 ible cumulative emissions for `historical` simulations are similarly incremented by ob-
451 servations from the year prior to the start of the experiment (1849 for CMIP6, and 1861
452 for CMIP5 to account for missing data in some simulations). Future simulations are matched
453 with historical simulations from the same model, and whenever possible, the same re-
454 alization.

2.5 Data Access and Analysis Software

CMIP5 and CMIP6 CO₂ land and ocean fluxes, grid cell areas and land-sea fractions were downloaded from ESGF using SynDA (Nasser et al., 2020). Probabilistic emission simulations were obtained from authors (FM15, CP16, CP20), or reproduced by running publicly available code (R17, LR21, see Appendix B). Computations were carried out in the Python programming language using xarray (Hoyer & Hamman, 2017), pandas (McKinney, 2010), NumPy (Harris et al., 2020) and SciPy (Virtanen et al., 2020), and graphics created with Matplotlib (Hunter, 2007). Analysis-ready data and code to reproduce results from this paper are available at the Federated Research Data Repository (<https://doi.org/10.20383/102.0549>).

3 Results

The following sections discuss different types of emissions, and to avoid confusion, we use the following terminology. *Scenario emissions* refer to CO₂ emissions pathways defined in RCP and SSP scenarios. *Compatible emissions* are inferred from carbon fluxes simulated by CMIP models using Eq. (3). Finally, *probabilistic emissions* denote ensembles of CO₂ emission trajectories simulated by the probabilistic IAMs described in section 2.3.

The mean and standard deviation of compatible cumulative emissions for RCPs and SSPs are shown in Figure 8. For CMIP5 experiments RCP6.0 and 8.5, compatible cumulative emissions are considerably smaller than scenario emissions. In other words, less carbon emissions are needed in CMIP models than in MAGICC6 to reach the same CO₂ concentration. This could suggest that positive carbon feedbacks might be more powerful in GCMs than in MAGICC6, or that MAGICC6 has more effective ocean or land carbon sinks. See Jones et al. (2013) and Friedlingstein et al. (2014) for further discussions. The inverse is true for CMIP6, where the ensemble mean of compatible emissions are systematically larger than SSP scenario emissions. Note that although RCP8.5 and SSP5-8.5 have approximately the same radiative forcing in 2100, their CO₂ concentrations are different, and the differences in emissions are not unexpected. These differences have important repercussions for the interpretation of scenario probability.

The mean and standard deviations shown in Figure 8 parameterize the normal distribution of Eq. (4), which acts as the likelihood term in Eq. (2). To clarify, Eq. (4) es-

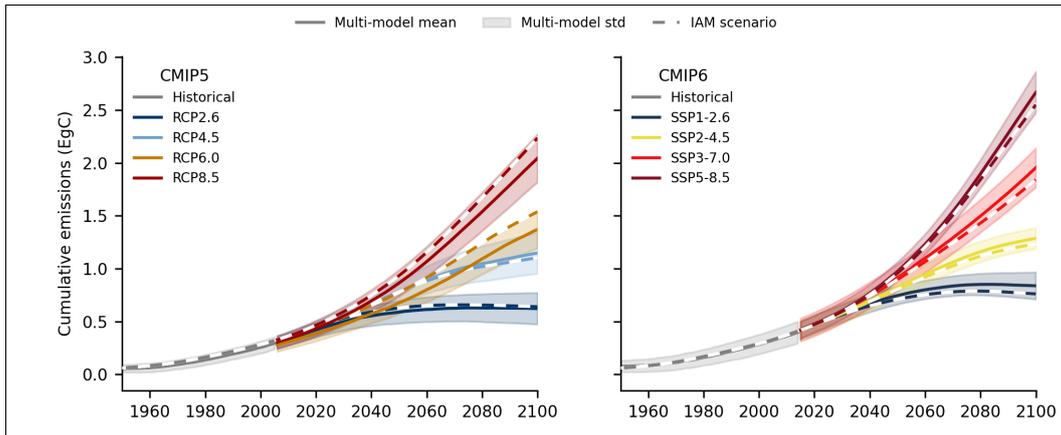


Figure 8. Mean and standard deviation of cumulative compatible emissions diagnosed from carbon fluxes in CMIP5 RCP (left) and CMIP6 SSP (right) Tier 1 experiments.

486 essentially evaluates the overlap between the distribution of compatible cumulative emis-
 487 sions for each scenario, and the distribution of probabilistic IAM cumulative emissions.
 488 This is illustrated in Figure 9 for one ensemble of probabilistic emission and one year.

489 The resulting relative likelihoods computed for CMIP5 and CMIP6 GHG scenar-
 490 ios and the five probabilistic emission simulations are presented in Figure 10. A *poste-*
 491 *rior* distribution can be obtained by multiplying these likelihoods with a *prior* for each
 492 scenario (Eq. 2). The likelihood time series are included in the supplementary material
 493 to enable assessments with different subjective *priors*. One notable feature is that high-
 494 end emission scenario RCP8.5 remains reasonably likely in all five IAMs until around
 495 2060, despite the fact that it lies in the upper tail of probabilistic emissions from R17,
 496 LR21 and CP20. This is due to Eq. (4) evaluating scenario likelihood against compat-
 497 ible emissions, which for RCP8.5 are smaller than scenario emissions (see Fig. 2). An-
 498 other feature worth highlighting is the low likelihood of RCP2.6 in all IAMs. Interest-
 499 ingly, for R17, LR21 and CP20, SSP1-2.6 is more likely than SSP3-7.0 by the end of the
 500 century.

501 As mentioned earlier, results from this probability assessment should not be inter-
 502 preted too literally. For one, probabilistic CO₂ emissions are not directly comparable among
 503 the different IAMs. The CO₂ emission processes simulated by each probabilistic IAMs
 504 are different, some including cement production and industrial uses, while others do not.

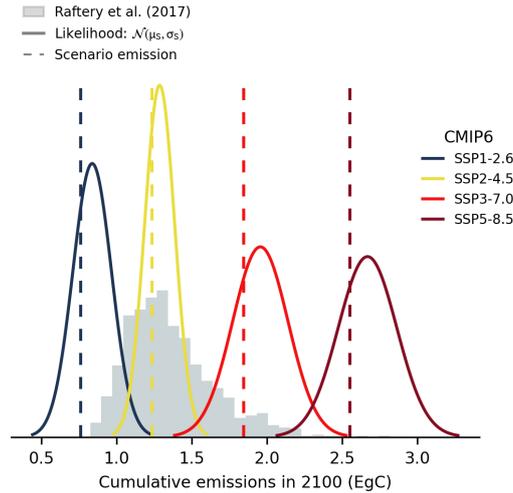


Figure 9. Illustrative histogram of cumulative emissions from Raftery et al. (2017) compared to the likelihood term (full line) for the four different SSP scenarios in 2100. SSP scenario emissions (dashed line) are shown for reference.

505 Also, emissions from CP16 and CP20 account for land-use changes, while compatible emis-
 506 sions do not. Those differences directly affect the estimated likelihoods.

507 Secondly, each IAM deals with policies very differently. Capellán-Pérez et al. (2020)
 508 include numerous policies regarding low carbon technologies, energy efficiency, recycling,
 509 transportation and afforestation. Fyke and Matthews (2015) includes policy-related pa-
 510 rameters such as a maximum carbon price, a carbon tax or non-fossil energy unit cost.
 511 In contrast, Capellán-Pérez et al. (2016), Raftery et al. (2017) and Liu and Raftery (2021)
 512 include no explicit parameterization for climate policies.

513 Finally, the relatively small number of IAMs and the fact that multi-model ensem-
 514 bles are not homogeneous across experiments artificially distorts the likelihood estima-
 515 tion. For instance, in CMIP5 we would expect each RCP's likelihood to start at 25%,
 516 because in 2006 the four RCPs have exactly the same CO₂ concentration. With iden-
 517 tical CO₂ concentration, the diagnosed emissions and their statistics should be very sim-
 518 ilar, except for small variations due to natural variability. Small ensemble sizes and dif-
 519 ferences in model make-up can shift the mean and variance of compatible emissions com-
 520 pared to the other RCPs, artificially perturbing the likelihood. This example gives a sense

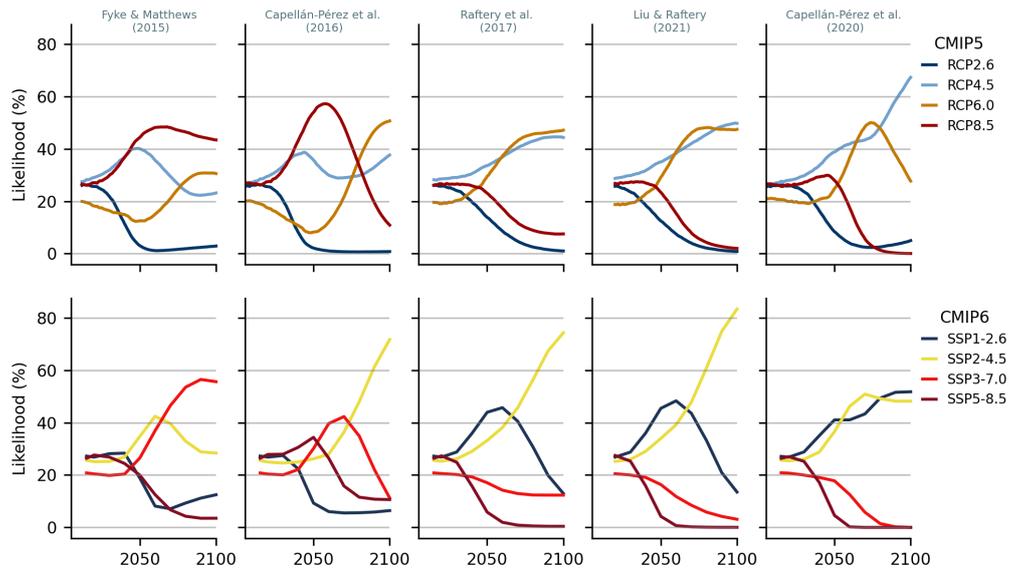


Figure 10. Bayesian likelihood for CMIP5 RCPs (top) and CMIP6 SSPs (bottom) CO₂ concentration pathways conditional on the probabilistic IAM CO₂ cumulative emission simulations ensembles from FM15, CP16, R17, LR21 and CP20. In theory, all scenarios should start with a likelihood close to 25% because the CO₂ concentration are identical at the start of each experiment. Discrepancies seen in CMIP5 RCP6.0 and SSP3-70 are due to differences in the CMIP ensemble make-up.

521 of the magnitude of the sampling error's influence on the results, and cast doubts on the
 522 applicability of these likelihoods for actual decision-making.

523 4 Discussion

524 The motivation for this paper is grounded in the day-to-day experience of climate
 525 service providers. Climate services strive to translate the best available climate science
 526 into actionable information. Because key climate projection experiments are run with
 527 GHG concentration scenarios, derivative products such as climate impact assessments
 528 or risk analyses are also conditional on GHG concentrations. In applications such as en-
 529 gineering or flood zone mapping, where a single value reflecting a level of risk is required,
 530 the lack of guidance on scenario probability acts as a barrier to climate adaptation.

531 One argument against assigning probabilities to emission scenarios is that it would
 532 be affected by *reflexive uncertainty* originating from human feedback to new informa-
 533 tion (Dessai & Hulme, 2004; van Vuuren et al., 2008). That is, the act of assigning prob-

534 abilities to scenarios would change the probability of these scenarios, making future cli-
535 mate change “unquantifiable”. Although this argument might hold in the abstract, the
536 idea that an academic paper would have a significant influence on global carbon emis-
537 sions can nowadays only be met with irony.

538 The reluctance of the climate community to assign probabilities to future GHG emis-
539 sion scenarios has led to the study of alternative decision-making approaches, often re-
540 ferred to as “Decision Making under Deep Uncertainty” (Stanton & Roelich, 2021). One
541 suggestion stemming from these efforts is to switch the focus of discussions from *agreement-*
542 *on-assumptions*, e.g. climate modeling assumptions, to *agreement-on-decisions* in order
543 to find solutions that perform well under a wide array of future conditions and minimize
544 regret (Kalra et al., 2014). Although valuable and illuminating, it is not clear how these
545 concepts apply to decisions bound by strict regulatory frameworks, such as engineering
546 or flood safety. Asking practitioners to overhaul laws, professional norms and regulations
547 to account for climate change’ deep uncertainties is sure to delay adaptation actions.

548 In the absence of a fully probabilistic decision-making framework, real-world adap-
549 tation decisions are made by non-experts, based on *ad hoc* selection of climate scenar-
550 ios based on data availability, the precautionary principle, personal opinions or hearsay.
551 Even among experts, debates around the relative likelihood of climate change scenar-
552 ios often struggle with the emission *vs* concentration aspects of climate change exper-
553 iments (Hausfather & Peters, 2020a; Schwalm et al., 2020a; Hausfather & Peters, 2020b;
554 Schwalm et al., 2020b). The argument that “RCP8.5 is unlikely because it requires an
555 implausible increase in coal use” may be true for the scenario’s emissions (Ritchie & Dowlatabadi,
556 2017), but on its own doesn’t imply that impacts derived from the concentration-driven
557 rcp85 CMIP experiment are also unlikely. As long as climate hazards are determined
558 by concentration-driven modeling experiments, arguments referring to emissions’ like-
559 lihood will have to account for uncertainties in carbon cycle simulations and carbon feed-
560 backs.

561 Ideally, climate change experiments would be carried out by Earth System Mod-
562 els (ESM) driven by an ensemble of representative *emission* pathways, instead of rep-
563 resentative *concentration* pathways. Carbon cycle feedbacks would be free to fully play
564 their role, instead of being curtailed by prescribed CO₂ concentrations. The diagnosis

565 of compatible emissions would become unnecessary, because ESM emission pathways could
566 be directly compared with IAM simulated emissions.

567 Similarly, with only five probabilistic emission ensembles to draw from (two shar-
568 ing the same model structure), it is clear that inter-model spread is not an accurate proxy
569 for prediction uncertainties. Ideally, a coordinated multi-IAM experiment would be car-
570 ried out, where dozens of independent modeling teams would contribute *predictive* sim-
571 ulations covering the same period, starting from the same initial conditions, and archiv-
572 ing their outputs using standardized variable definitions. IAM simulation outputs should
573 map to ESM driving variables to facilitate the assignment of probabilities to represen-
574 tative *emission* pathways.

575 Together, these ESM and IAM coordinated experiments would provide researchers
576 with the basic materials to conduct probabilistic climate change impact assessments, and
577 answer a long-standing request from the climate service community and its stakehold-
578 ers.

579 **5 Conclusion**

580 This paper adopts the argument that “it is very unhelpful to presume that all fu-
581 tures are equally likely” (Mckibbin et al., 2004), and suggests an approach to estimate
582 GHG scenario probability using probabilistic emissions simulated by IAMs. Because cli-
583 mate models are driven by *concentration* pathways, CO₂ emissions compatible with those
584 concentrations are estimated from CMIP5 and CMIP6 simulated carbon fluxes. For each
585 RCP and SSP, these compatible emissions are compared with the probabilistic CO₂ emis-
586 sions from five IAMs to estimate scenario’s relative likelihood.

587 Although IAMs vary considerably in their structure and assumptions, the likeli-
588 hoods obtained share similar traits. All rank RCP2.6 as the least likely until 2075. Al-
589 though RCP8.5 depicts extremely high emissions, it remains relatively likely up until 2060.
590 This is due to the fact that compatible emissions for high-end scenarios are considerably
591 lower than their corresponding scenario emissions. For three IAMs out of five, SSP1-2.6
592 ends up more likely than SSP3-7.0 and SSP5-8.5 by the end of the century, with SSP5-
593 8.5’ likelihood dropping to zero in three IAMs.

594 The approach presented suffers from a number of caveats that cast doubts on the
595 reliability of results. The objective is not necessarily for these likelihoods to be used in

596 practice, but rather to illustrate the potential of probabilistic IAMs to inform scenario
597 probability. Hopefully new climate and IAM experiments can be designed that will bet-
598 ter address the need for fully probabilistic climate change risk assessments.

599 Appendix A CMIP Simulations Availability

600 Search requests on ESGF for CMIP5 and CMIP6 simulations were last updated
 601 in August 2021. A simulation is considered available if both variables `fgco2` and `nbp` are
 602 present for the historical period and at least one future experiment. In CMIP5, mod-
 603 els MRI-ESM1 and CMCC-CESM were not considered due to the presence of abnormal-
 604 ities in the data. Also, INMCM4 was kept out of the analysis because it does not rep-
 605 resent land-use changes.

Table A1. Number of simulations storing land and ocean carbon fluxes for each CMIP5 tran-
 sient scenario experiment.

	Historical	RCP2.6	RCP4.5	RCP6.0	RCP8.5
Model name					
CanESM2	5	5	5	0	5
GFDL-ESM2G	1	1	1	1	1
GFDL-ESM2M	1	1	1	1	1
HadGEM2-CC	3	0	1	0	3
HadGEM2-ES	4	4	4	4	4
IPSL-CM5A-LR	6	4	4	1	4
IPSL-CM5A-MR	3	1	1	0	1
IPSL-CM5B-LR	1	0	1	0	1
MIROC-ESM	3	1	1	1	1
MIROC-ESM-CHEM	1	1	1	1	1
MPI-ESM-LR	3	3	3	0	3
MPI-ESM-MR	3	1	3	0	1
NorESM1-ME	1	1	1	1	1

606 Appendix B Preindustrial mean emissions

607 Even in the absence of anthropogenic carbon emissions, some models exhibit non-
 608 zero carbon fluxes. This may be due to models not having reached equilibrium, or in other
 609 cases to how they account for river outgassing. To try to avoid attributing these fluxes
 610 to fossil fuel emissions, the mean preindustrial compatible emissions are subtracted from

611 compatible emission time series of the historical and future periods. Tables B1 and B2
612 present the mean compatible emissions computed over the last 30 to 50 years of the piControl
613 simulation.

Table A2. Number of simulations storing land and ocean carbon fluxes for each CMIP6 Tier 1 ScenarioMIP experiment.

	Historical	SSP1-2.6	SSP2-4.5	SSP3-7.0	SSP5-8.5
Model name					
ACCESS-ESM1-5	29	10	12	10	10
CESM2	11	3	3	3	3
CESM2-FV2	3	0	0	0	0
CESM2-WACCM	3	1	5	3	5
CESM2-WACCM-FV2	3	0	0	0	0
CMCC-ESM2	1	1	1	1	1
CNRM-ESM2-1	9	5	10	5	5
CanESM5	65	50	50	50	50
CanESM5-CanOE	3	3	3	3	3
EC-Earth3-CC	1	0	1	0	0
GFDL-ESM4	1	1	0	1	0
INM-CM4-8	1	1	1	1	1
INM-CM5-0	3	1	1	5	1
IPSL-CM5A2-INCA	1	1	0	1	0
IPSL-CM6A-LR	32	6	11	11	6
MIROC-ES2L	31	10	30	10	10
MPI-ESM-1-2-HAM	3	0	0	3	0
MPI-ESM1-2-LR	9	10	10	10	10
MRI-ESM2-0	1	0	0	0	1
NorESM2-LM	3	1	3	3	1
NorESM2-MM	3	1	1	1	1
UKESM1-0-LL	17	16	13	10	4

Table B1. Mean preindustrial compatible emissions from the CMIP5 piControl experiment.

		Emissions (PgC)
Model name	Member	
CanESM2	r1i1p1	-0.07
GFDL-ESM2G	r1i1p1	0.22
HadGEM2-CC	r1i1p1	0.34
HadGEM2-ES	r1i1p1	-0.29
IPSL-CM5A-MR	r1i1p1	0.00
IPSL-CM5B-LR	r1i1p1	-0.10
MIROC-ESM	r1i1p1	0.09
MPI-ESM-LR	r1i1p1	-0.06
NorESM1-ME	r1i1p1	0.17

Table B2. Mean preindustrial compatible emissions from the CMIP6 piControl experiment.

		Emissions (PgC)
Model name	Member	
ACCESS-ESM1-5	r1i1p1f1	-0.21
CESM2	r1i1p1f1	-0.06
CESM2-FV2	r1i1p1f1	-0.07
CESM2-WACCM	r1i1p1f1	-0.09
CNRM-ESM2-1	r1i1p1f2	-0.71
CanESM5	r1i1p1f1	-0.09
CanESM5-CanOE	r1i1p2f1	-0.07
INM-CM4-8	r1i1p1f1	1.12
INM-CM5-0	r1i1p1f1	1.15
IPSL-CM6A-LR	r1i1p1f1	-0.01
MIROC-ES2L	r1i1p1f2	0.11
MPI-ESM1-2-LR	r1i1p1f1	-0.03
MPI-ESM1-2-LR	r2i1p1f1	0.15
MRI-ESM2-0	r1i2p1f1	0.41
UKESM1-0-LL	r1i1p1f2	-0.09

614 **Open Research**

615 Compatible emissions, probabilistic emissions, scenario emissions and observations
616 used in this paper are available at the Federated Research Data Repository at [https://](https://doi.org/10.20383/102.0549)
617 doi.org/10.20383/102.0549, along with code to compute the likelihood, create graph-
618 ics and tables.

619 CMIP data was downloaded from the Earth System Grid Federation using Synda.

620 SSP scenario emissions shown in figures 2 to 9 are based on data from the SSP database
621 hosted by the IIASA Energy Program at <https://tntcat.iasa.ac.at/SspDb>

622 Time series of CO₂ concentrations for RCP and SSP scenarios were obtained from
623 International Institute for Applied Systems Analysis (IIASA) RCP and SSP databases.

624 Observed CO₂ time series from the Global Carbon Budget were obtained from
625 the Integrated Carbon Observing System (<https://www.icos-cp.eu/>).

626 Probabilistic emissions from FM15 are available at [https://github.com/JeremyFyke/](https://github.com/JeremyFyke/CEPM/blob/results/results/carbon_emissions.h5)
627 [CEPM/blob/results/results/carbon_emissions.h5](https://github.com/JeremyFyke/CEPM/blob/results/results/carbon_emissions.h5)

628 Code to generate probabilistic emissions from R17 can be found at [https://github](https://github.com/PPgp/CO2projections)
629 [.com/PPgp/CO2projections](https://github.com/PPgp/CO2projections).

630 Code to generate probabilistic emissions from LR21 can be found at [https://github](https://github.com/PPgp/BayesianClimateProjections)
631 [.com/PPgp/BayesianClimateProjections](https://github.com/PPgp/BayesianClimateProjections).

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