

1     **Explicit calculations of Wet Bulb Globe Temperature**  
2     **compared with approximations and why it matters for**  
3     **labor productivity**

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7             **Key Points:**

- 8             • Most climate change heat stress impacts studies which claim to use WBGT, em-  
9             ploy instead ad hoc approximations.
- 10            • We evaluate the biases of two commonly used approximations within both an ide-  
11            alized and the more realistic setting of ERA5 reanalysis data.
- 12            • We provide an accessible and computationally efficient Python implementation  
13            to facilitate widespread uptake of accurate WBGT calculations.

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## Abstract

Wet bulb globe temperature (WBGT) is a widely applied heat stress index. However, most applications of WBGT within the heat stress impacts literature do not use WBGT at all, but one of the ad hoc approximations, typically the simplified WBGT (sWBGT) or the environmental stress index (ESI). Surprisingly little is known about how well these approximations work for the global climate and climate change settings that they are being applied to. Here we assess the bias distribution as a function of temperature, humidity, wind speed and radiative conditions of both sWBGT and ESI relative to a well-validated, explicit physical model for WBGT developed by Liljegren, within an idealized context and the more realistic setting of ERA5 reanalysis data. sWBGT greatly overestimates heat stress in hot-humid areas. ESI has much smaller biases in the range of standard climatological conditions. However, both metrics may substantially underestimate extreme heat especially over subtropical dry regions. These systematic biases demonstrate that sWBGT-derived estimates of heat stress and its health and labor consequences are significantly overestimated over much of the world today. We recommend discontinuing the use of sWBGT. ESI may be acceptable for assessing average heat stress or integrated impact over a long period like a year, but less suitable for health applications, extreme heat stress analysis, or as an operational index for heat warning, heatwave forecasting or guiding activity modification at workplace. Nevertheless, Liljegrens approach should be preferred over these ad hoc approximations and we provide a Python implementation to encourage its widespread use.

## Plain Language Summary

Wet bulb globe temperature (WBGT) is a widely applied heat stress index. However, most applications of WBGT within the climate change heat stress impacts literature do not use WBGT at all, but one of the ad hoc approximations, typically the simplified WBGT (sWBGT) or sometimes the environmental stress index (ESI). But we know little about how well these approximations work for measuring heat stress. Here we evaluate the performance of sWBGT and ESI against a well-validated, explicit physical model of WBGT. sWBGT greatly overestimates heat stress under hot, humid climate. ESI performs much better in measuring average heat stress. But they both may seriously underestimate severe heat stress especially in hot, dry regions. Our results suggest that previous estimates of heat stress and its impact using sWBGT tend to be largely overestimated. We recommend discontinuing the use of sWBGT. ESI may be acceptable for assessing average heat stress, but less suitable for the warning or forecasting of extreme heat, or providing guidance for employees and employers to deal with heat stress at workplace. Nevertheless, the well-validated physical model of WBGT should be preferred over these approximations and we provide a Python implementation to encourage its more widespread use.

## 1 Introduction

Heat stress has caused more deaths than any other extreme weather event, and is recognized to have broad social and economic impacts such as heat-related illness (Barriopedro et al., 2011; Mora et al., 2017; Ebi et al., 2021), conflict (Burke et al., 2009; Schleussner et al., 2016), crime (Shen et al., 2020), electricity demand (Maia-Silva et al., 2020), and labor productivity reduction (Dunne et al., 2013; Kjellstrom et al., 2016; Masuda et al., 2021; Orlov et al., 2020; Hsiang et al., 2017). Heat stress will become a even bigger threat in the future as the world warms (Diffenbaugh & Giorgi, 2012; Meehl & Tebaldi, 2004; Willett & Sherwood, 2010; Sherwood & Huber, 2010; D. Li et al., 2020).

As well reviewed elsewhere, many heat stress metrics have been developed (de Freitas & Grigorieva, 2014; Epstein & Moran, 2006; Havenith & Fiala, 2015). Among these the wet bulb globe temperature (WBGT) is arguably the most popular one, enjoying the

64 advantages of a simple physical interpretation, covering all four ambient factors (tem-  
 65 perature, humidity, wind and radiation) contributing to heat stress, and having well es-  
 66 tablished safety thresholds to guide activity modification within the military (Army, 2003),  
 67 occupational (NIOSH, 2016) and athletic settings (ACSM, 1984). It is constructed as  
 68 a linear combination of natural wet bulb temperature ( $T_w$ ), black globe temperature ( $T_g$ )  
 69 and dry bulb temperature ( $T_a$ ):  $WBGT = 0.7T_w + 0.2T_g + 0.1T_a$  (Yaglou & Minard,  
 70 1957).

71 Measurement of WBGT requires costly instrument and time-consuming attention  
 72 by experienced operators which prevents it to become a routine meteorological measure-  
 73 ment at weather stations. As a result, several approaches have been developed to ap-  
 74 proximate WBGT, with the simplified WBGT (sWBGT) (ABM, 2010) and environmen-  
 75 tal stress index (ESI) (D. Moran et al., 2001; D. Moran, Pandolf, Laor, et al., 2003) be-  
 76 ing representative of many similar ad hoc approaches.

77 sWBGT (ABM, 2010) is an approximate form requiring only temperature and hu-  
 78 midity and explicitly assuming fixed moderately high solar radiation and low wind speeds  
 79 which implies potential positive or negative biases when these assumptions are not met.  
 80 It has been widely used because of its simplicity for assessing heat stress and the impli-  
 81 cation on athletes and labor (Smith et al., 2018; Willett & Sherwood, 2010; Kakamu et  
 82 al., 2017; Cooper et al., 2016; Lee & Min, 2018; Zhu et al., 2021; Kjellstrom et al., 2009;  
 83 Liu, 2020; Altinsoy & Yildirim, 2014). ESI was constructed via a multiple regression with  
 84 WBGT being the dependent variable and temperature, humidity, solar radiation and their  
 85 interaction terms being independent variables (D. Moran et al., 2001). ESI was validated  
 86 across different climate regimes over Israel and New Zealand based on large databases  
 87 (D. Moran, Pandolf, Shapiro, et al., 2003; D. Moran et al., 2004; D. S. Moran et al., 2004,  
 88 2005). Although a high correlation ( $>0.9$ ) between WBGT and ESI was achieved, the  
 89 residual errors can be up to  $\pm 2^\circ\text{C}$ , and it may be the critical situations (such as extreme  
 90 heat stress) where ESI substantially under- or overestimate WBGT (Havenith & Fiala,  
 91 2015).

92 Outside of the limited conditions for which these approximate forms were devel-  
 93 oped, little is known about how well these approximations work for the global climate  
 94 and climate change settings that they are being applied to. Although a few studies had  
 95 quantified biases of sWBGT or ESI based on local meteorological measurements (D. Moran  
 96 et al., 2004; D. S. Moran et al., 2004, 2005; Grundstein & Cooper, 2018), the results are  
 97 not readily transferable to other regions with different climate conditions. A recent study  
 98 employed both sWBGT and ESI to assess labor reduction due to intensifying heat stress,  
 99 and found vast differences between the two metrics (de Lima et al., 2021). However, it  
 100 is not clear which one is more close to the reality. Given the expected biases of both met-  
 101 rics, and their large discrepancies in indicating labor loss, it is necessary to assess the  
 102 magnitude of these biases and the consequent influences on heat stress impact assess-  
 103 ment, which is crucial for determining the suitability of each metric under certain ap-  
 104 plication scenarios.

105 Aside from the simple approximations of WBGT described above, physical mod-  
 106 els on the energy balance of WBGT sensors have also been developed which enable a di-  
 107 rect simulation of WBGT measurements from weather station observations or climate  
 108 model output (Gaspar & Quintela, 2009; C. H. Hunter & Minyard, 1999; Bernard & Pour-  
 109 moghani, 1999; Liljegren et al., 2008; Dervede & Gilbert, 1991). Among them, the model  
 110 developed by Liljegren et al. (2008) is a highly sophisticated one being well calibrated  
 111 and validated (with a RMS difference of less than  $1^\circ\text{C}$ ) (Liljegren et al., 2008; Lemke &  
 112 Kjellstrom, 2012). However, Liljegren's approach has seen limited applications (Takakura  
 113 et al., 2017, 2018; Casanueva et al., 2020; Jacobs et al., 2019; Orlov et al., 2019) poten-  
 114 tially because it is complex and computationally intensive. Moreover, Liljegren's code  
 115 was written in C and FORTRAN language which may be not familiar to most end-users.

116 To resolve this issue, we rewrote the code in Cython which is fast, easy to use in Python,  
117 and scales well for large dataset such as climate model output.

118 Here we treat Liljegren's model as a ground truth, and explores the bias distribu-  
119 tions of sWBGT and ESI within both an idealized context and the more realistic set-  
120 ting of ERA5 reanalysis data. The paper is structured as follows. Section 2 introduces  
121 more details on the metrics and Liljegren's model, as well as data source and analysis  
122 methods. Section 3 presents bias quantification results including first the bias distribu-  
123 tion within an idealized context as a function of temperature, humidity, wind speed and  
124 radiative conditions, and second the error structure introduced within ERA5 reanaly-  
125 sis data. In section 4, the potential consequences of these biases are examined through  
126 an example application of labor productivity estimation. Section 5 discusses the impli-  
127 cation of our results. Section 6 concludes by highlighting the main findings and provid-  
128 ing suggestions.

## 129 2 Data and methods

### 130 2.1 sWBGT, ESI and Liljegren's model

131 Here we present the formulas of sWBGT, ESI and Liljegren's model. Parameter  
132 definitions and their units within all equations are summarized in the list of notation.  
133 sWBGT was developed for heat stress assessment in sports medicine and formulated as  
134 (ACSM, 1984):

$$135 \textit{sWBGT} = 0.567(T_a - 273.15) + 0.393e_a + 3.94 \quad (1)$$

136 ESI was designed as an approximation to WBGT via a multiple regression model (D. Moran  
137 et al., 2001), and structured as (D. Moran, Pandolf, Shapiro, et al., 2003):

$$138 \textit{ESI} = 0.62(T_a - 273.15) - 0.007RH + 0.002S_{down} + 0.0043(T_a - 273.15) \cdot RH - 0.078(0.1 + S_{down})^{-1} \quad (2)$$

139 Liljegren's model is physically based relying on fundamental principles of heat and  
140 mass transfer. It performs energy budget analysis on both natural wet bulb and black  
141 globe sensors, which boil down to two separate equations for  $T_w$  (eq. 3) and  $T_g$  (eq. 5)  
142 (Liljegren et al., 2008) that need to be solved by iteration:

$$143 T_w = T_a - \frac{\Delta H}{c_p} \frac{M_{H2O}}{M_{Air}} \left( \frac{Pr}{Sc} \right)^{0.56} \left( \frac{e_w - e_a}{P - e_w} \right) + \frac{\Delta F_{net}}{Ah} \quad (3)$$

144 where  $\Delta F_{net}$  refers to net radiative gain by the wick:

$$\Delta F_{net} = \frac{1}{2} \pi DL \epsilon_w (L_{down} + L_{up}) - \pi DL \sigma \epsilon_w T_w^4 + \left( \pi DL + \frac{\pi D^2}{4} \right) (1 - \alpha_w) (1 - f_{dir}) S_{down} \\ + \left( DL \sin \theta + \frac{\pi D^2}{4} \cos \theta \right) (1 - \alpha_w) f_{dir} \frac{S_{down}}{\cos \theta} + \pi DL (1 - \alpha_w) S_{up} \quad (4)$$

$$145 T_g^4 = \frac{L_{down} + L_{up}}{2\sigma} - \frac{h(T_g - T_a)}{\epsilon_g \sigma} + \frac{S_{down}(1 - \alpha_g)}{2\epsilon_g \sigma} \left( 1 - f_{dir} + \frac{f_{dir}}{2 \cos \theta} \right) + \frac{1 - \alpha_g}{2\epsilon_g \sigma} S_{up} \quad (5)$$

146 where  $S_{down}$ ,  $S_{up}$ ,  $L_{down}$  and  $L_{up}$  denote surface downward and upwelling solar and long-  
147 wave radiation respectively. The latter three radiation components were approximated  
148 as:

$$149 L_{down} = \sigma \epsilon_a T_a^4 \quad (6)$$

$$150 L_{up} = \sigma \epsilon_{sfc} T_{sfc}^4 = \sigma T_a^4 \quad (7)$$

$$S_{up} = \alpha_{sfc} S_{down} \quad (8)$$

In Liljegren's model, air temperature, humidity, wind speed and surface downward solar radiation are required as inputs for solving  $T_w$  and  $T_g$ . For details of the calculation procedure, please refer to Liljegren et al. (2008). Liljegren's model was originally written in FORTRAN and C-language programs. We rewrote it in Cython language for implementation in Python. Please find the code availability in the Acknowledgement section.

## 2.2 Bias quantification within an idealized context

Bias distributions of sWBGT and ESI are first identified within an idealized context as a function of four input variables. We apply Liljegren's model in its original form to assessing biases of both metrics across artificially selected ranges of air temperature (20-50°C), relative humidity (5-95%), 2m wind speed (0.13, 0.5, 1.0, 2.0, 3.0m/s), and surface downward solar radiation (0, 300, 500, 700, 900w/m<sup>2</sup>). The focus is on conditions under which biases are exceptionally large.

## 2.3 Bias quantification using ERA5 reanalysis data

With diverse climate regimes spanning across the globe, biases of different magnitudes and/or signs are expected to occur over different regions. It would be useful to reveal the spatial distribution of biases and identify locations where sWBGT/ESI is exceptionally biased and their applications would cause serious under- or over-estimation of heat stress and downstream impacts.

ERA5 reanalysis data (Hersbach, H. et al., 2018; Bell, B. et al., 2020) are used to identify the bias spatial structure in a more realistic setting. Since all four radiation components are available from the ERA5 archive, the approximations in equation 6-8 are no longer necessary. The 2m air and dewpoint temperature, surface pressure, 10m wind speed and surface downward and upwelling solar and thermal radiation on a 0.25°×0.25° grid are used to calculate WBGT at an hourly frequency.

The cosine zenith angle ( $\cos\theta$ ) is needed to project direct solar radiation from a flux through a horizontal plane (as stored in ERA5 reanalysis archive) to a flux through a plane perpendicular to the incoming solar radiation (as required by energy budget analysis) (as denoted by  $\cos\theta$  term in the denominator within eq. 4-5). Since model radiation components are stored as accumulated-over-time quantities (over each hourly interval in the case of ERA5 reanalysis data), the time average of  $\cos\theta$  during each interval is needed. However, when the accumulation intervals encompass sunset or sunrise, the inclusion of zeros (when the sun is below the horizon) may make the time average of  $\cos\theta$  too small. Being in the denominator, this too small  $\cos\theta$  would lead to an over-estimation of the projected direct solar radiation and consequently too high WBGT values. A simple approximate solution to this problem is taking the average  $\cos\theta$  during only the sunlit part of each interval (please refer to Hogan and Hirahara (2016) or Di Napoli et al. (2020) for the calculation procedure). In Fig. S1, we provide an example of erroneously peaks of WBGT values around sunrise or sunset introduced by using  $\cos\theta$  averaged over the whole hourly interval, and also show that the peaks can be removed by averaging  $\cos\theta$  only during the sunlit period.

## 2.4 Labor productivity calculation

Several different labor productivity functions have been applied to assessing heat stress-induced labor reduction (Dunne et al., 2013; Bröde et al., 2018; Kjellstrom et al.,

196 2018; Foster et al., 2021), and here we choose the method adopted by ISO7243 standard  
 197 for illustrative purposes.

198 The ISO7243 standard provided WBGT limit reference values ( $WBGT_{lim}$ ) corre-  
 199 sponding to the upper limit of the prescriptive zone for different levels of metabolic heat  
 200 production rates ( $M$  in Watts) (ISO, 2017):

$$201 \quad WBGT_{lim} = 56.7 - 11.5 \log_{10}(M) + 273.15 \quad (9)$$

For WBGT exceeding the limit value, only a fraction of each hour is allowed for  
 working in order to ensure that the physiological strain during each hour cycle can be  
 recuperated after the rest. This fraction can be used as an estimate of labor productiv-  
 ity (for example, a value of 0.5 indicates a 30min working and 30min rest cycle, and con-  
 sequently a 50% labor productivity) and calculated as follows (Malchaire, 1979; Bröde  
 et al., 2018):

$$\text{labor productivity} = \max\{0; \min[1; \frac{WBGT_{lim,rest} - WBGT}{WBGT_{lim,rest} - WBGT_{lim}}]\} \quad (10)$$

## 202 **2.5 Gridded population dataset**

203 Gridded world population data (GPWv4.11) (Center for International Earth Sci-  
 204 ence Information Network - CIESIN - Columbia University, 2018) with a spatial reso-  
 205 lution of  $0.25^\circ \times 0.25^\circ$  for year 2020 after adjusting to match the country total of United  
 206 Nations World Population Prospects are employed to calculate global population-weighted  
 207 labor productivity.

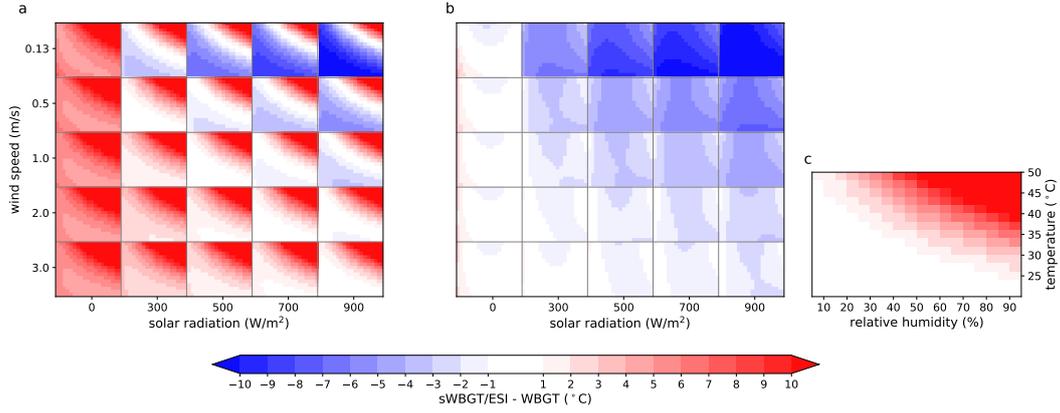
## 208 **3 Bias quantification**

### 209 **3.1 Idealized setting**

210 In order to understand bias structure and its dependencies on ambient conditions,  
 211 we calculate sWBGT/ESI biases (sWBGT/ESI - WBGT) across artificially selected ranges  
 212 of air temperature, relative humidity, wind speed and solar radiation (Fig. 1). In the case  
 213 of sWBGT, positive biases (sWBGT > WBGT) appear to be dominant, especially dur-  
 214 ing nighttime (zero solar radiation), with bias magnitudes up to more than +10 °C. Nev-  
 215 ertheless, negative biases (sWBGT < WBGT) may occur under strong solar radiation and  
 216 light wind condition. Given any fixed level of solar radiation and wind speed, there tends  
 217 to be larger positive biases under hotter and more humid condition which is a direct re-  
 218 sult of sWBGT placing all weights on temperature and humidity.

219 ESI, in comparison, is mainly subject to negative biases. Wind speed and solar ra-  
 220 diation appear to be the dominant factors controlling bias magnitudes with larger neg-  
 221 ative biases under strong solar radiation and light wind (up to -10 °C under  $900w \cdot m^{-2}$   
 222 solar radiation and 0.13 m/s wind speed). Under dry condition with relative humidity  
 223 <10%, ESI exhibits smaller negative biases and even positive ones during nighttime when  
 224 the bias magnitudes are overall smaller as well.

225 Although some combinations of the four meteorological inputs shown in figure 1  
 226 are physically less plausible (such as large humidity and strong solar radiation), it pro-  
 227 vides an overall picture of sWBGT/ESI biases across the 4-D climatic space which can  
 228 serve as a guidance for further detailed bias assessment or practical applications. For ex-  
 229 ample, we expect larger over-estimations by sWBGT during nighttime (or indoor) or un-  
 230 der hot-humid climate such as in the tropics, and larger under-estimation by ESI under  
 231 sunny, calm days. Next, we explore bias structure under the more realistic setting of ERA5  
 232 reanalysis data with frequent reference to and comparison with the pattern obtained here.  
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**Figure 1.** Bias distribution of sWBGT (a) and ESI (b) across an artificial 4-D climatic space of air temperature, relative humidity, 2m wind speed and surface downward solar radiation. Each small box in (a) and (b) depicts bias distribution across a range of temperature (20-50°C) and relative humidity (5-95%) as shown in (c) under fixed levels of solar radiation and wind speed.

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## 3.2 Realistic setting

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### 3.2.1 Biases at climatological mean level

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ERA5 reanalysis data are applied to identifying the spatial distribution of biases within a realistic context. First, we assess biases of both metrics in terms of the climatological monthly average (1990-2019) of daily mean, maximum and minimum values (Fig. 2). Since we focus on heat stress, only the hottest calendar month (determined by climatological monthly mean of WBGT) is included. A consistent overestimation by sWBGT is detected across the globe with larger biases for daily minimum (by  $> 4^{\circ}\text{C}$ ) and smaller biases for daily maximum (Fig. 2e,f). Areas with hot-humid summer, such as the tropics, south Asia, eastern China and southeastern U.S., exhibit larger positive biases ( $> 2^{\circ}\text{C}$  for daily maximum,  $> 5^{\circ}\text{C}$  for daily minimum and  $> 4^{\circ}\text{C}$  for daily mean) (Fig. 2d-f) which is consistent with the bias structure revealed within idealized context (Fig. 1a). Subtropical dry regions show smaller biases in comparison. Additionally, a topography effect is evident with smaller positive or even negative biases for daily maximum over mountainous areas like the Himalayas, Andes, and Rocky Mountains (Fig. 2e), although the WBGT values over these regions are generally small (Fig. 2b).

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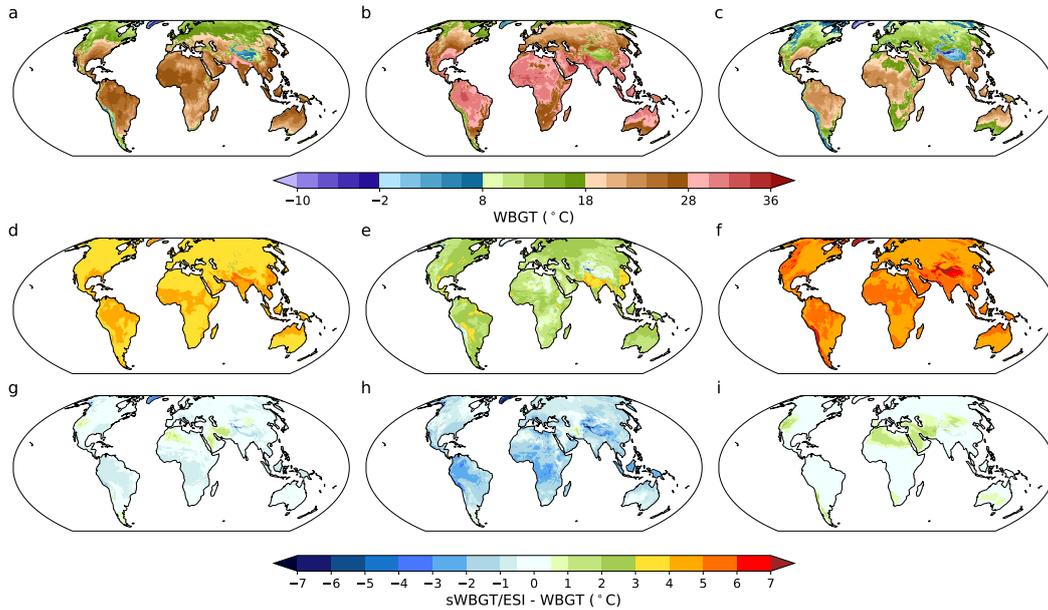
ESI has smaller overall biases compared with sWBGT. Positive and negative biases within  $\pm 1^{\circ}\text{C}$  occur for daily mean in subtropical dry regions and the tropics respectively (Fig. 2g). Negative biases dominate daily maximum values particularly in the tropics (Fig. 2h). In that region, the bias magnitude is -2 to  $-3^{\circ}\text{C}$  due to relatively strong solar radiation and low wind speed over tropical areas as indicated in the idealized results (Fig. 1b). Subtropical dry regions, despite even stronger solar radiation, show smaller negative and even positive biases for daily maximum as a result of low humidity and probably relatively higher wind speed. In the case of daily minimum, the differences between ESI and WBGT are generally small (within  $\pm 0.5^{\circ}\text{C}$ ) except over-estimations by  $1\text{-}2^{\circ}\text{C}$  over North Africa and Middle East (MENA) dry regions (Fig. 2i). This agrees with the positive biases under dry nighttime conditions revealed within the idealized setting (Fig. 1b).

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Compared with sWBGT, ESI appears to be a better approximation particularly for nighttime and daily mean situation. However, the larger negative biases for daily max-

264 inum (Fig. 2h) imply that ESI may substantially underestimate daily peak heat stress  
 265 especially when we turn from climatological mean to individual days or hours.



**Figure 2.** Climatological monthly average (CMA) of daily mean (a), maximum (b) and minimum (c) WBGT for the period 1990-2019. Biases of sWBGT (d-f) and ESI (g-i) with respect to CMA of daily mean (d, g), maximum (e, h) and minimum values (f, i). Only the hottest month (determined by CMA WBGT) being included.

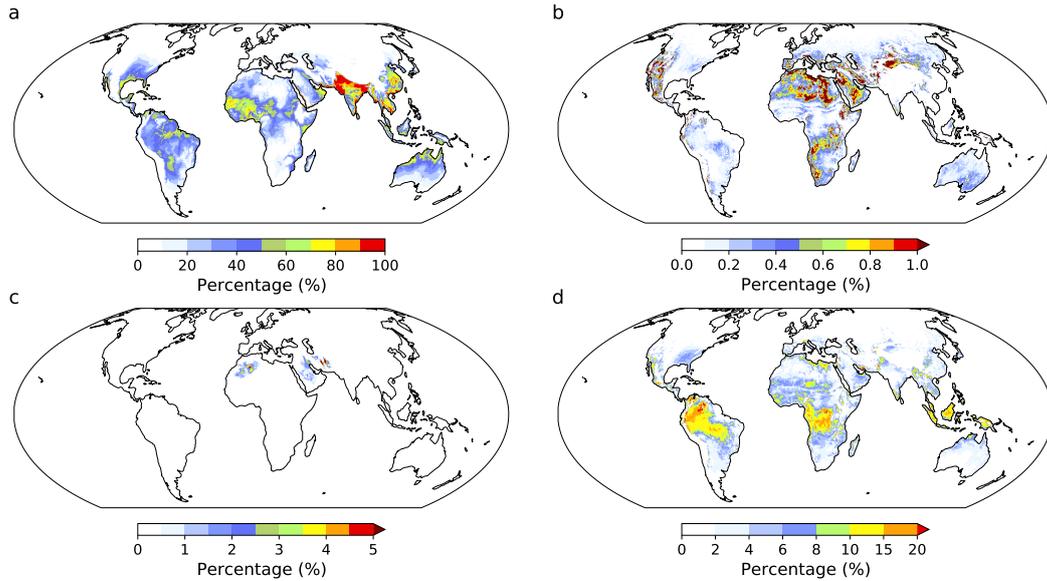
### 266 3.2.2 Frequencies of relatively large biases

267 It bears mentioning that bias quantification in Fig. 2 is based on 30-year clima-  
 268 tological means, whereas bias magnitudes can be much larger over certain individual days  
 269 and/or hours. Here we count the frequencies of relatively large positive and negative bi-  
 270 ases (beyond  $\pm 2^\circ\text{C}$ ) based on original hourly time series during 1990-2019 (Fig. 3), with  
 271 an additional requirement of WBGT exceeding  $25^\circ\text{C}$ , the  $WBGT_{lim}$  value for very heavy  
 272 work (a metabolic rate of 520W) according to ISO7243 standard.

273 sWBGT overestimates WBGT by at least  $2^\circ\text{C}$  within more than 30% cases over  
 274 tropics and other hot-humid area and even more than 80% over the northern part of South  
 275 Asia (Fig. 3a). In the same region, there are still more than 50% cases even if biases mag-  
 276 nitudes are raised to  $>5^\circ\text{C}$  (Fig. S2). In contrast, underestimations by more than  $2^\circ\text{C}$   
 277 are rare ( $<1\%$ ) and concentrate in subtropical dry regions presumably under dry, sunny  
 278 and calm days (Fig. 1a). In the case of ESI, negative biases beyond  $-2^\circ\text{C}$  are detected  
 279 for over 10% cases in tropical areas (Fig. 3d); whereas positive biases in ESI by more  
 280 than  $2^\circ\text{C}$  are less frequent and concentrate over west Sahara and Middle East dry regions  
 281 ( $<5\%$ ) (Fig. 3c).

### 282 3.2.3 Biases conditional on WBGT values

283 It is useful to know whether biases are independent of WBGT values or not. A cor-  
 284 relation between them indicates biases of different magnitudes for heat stress of differ-  
 285 ent levels, amongst which the under- or over-estimation of more severe heat stress is of  
 286 particular concern. To explore it, we calculate and compare biases conditional on the 50th,



**Figure 3.** Occurrence percentage of positive (a, c) and negative biases (b, d) larger than  $\pm 2^\circ\text{C}$  for sWBGT (a, b) and ESI (c, d) during 1990-2019 with an additional requirement of WBGT exceeding  $25^\circ\text{C}$ . Only the hottest month (defined by climatological monthly average WBGT) is included.

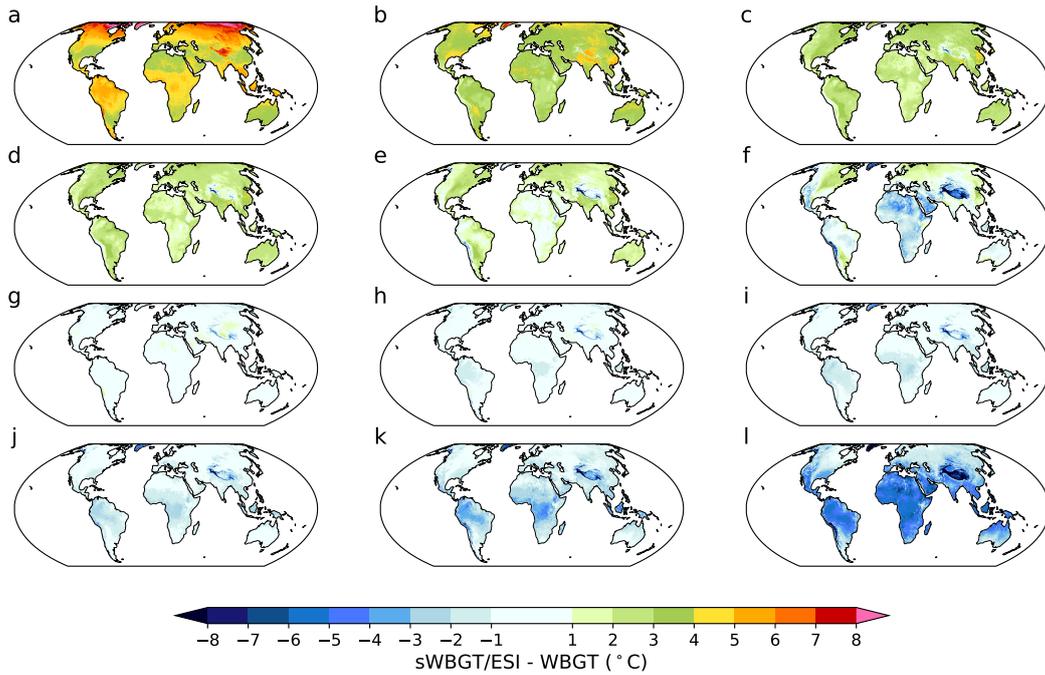
287 75th, 90th, 95th, 99th, and 99.9th percentile exceedance values of WBGT (Fig. 4), which  
 288 is done for each individual year first and then averaged across the period 1990-2019.

289 Both sWBGT and ESI show a clear tendency towards smaller positive or stronger  
 290 negative biases moving from lower to higher percentile exceedance values of WBGT, sug-  
 291 gesting a potential correlation between biases and WBGT which is not surprising since  
 292 both of them are controlled by the same set of meteorological variables (Fig. 1). sWBGT  
 293 conditional on 50th percentile of WBGT shows substantial positive biases ( $> 3^\circ\text{C}$  glob-  
 294 ally) which are reduced to  $< 2^\circ\text{C}$  in the majority of the world when conditional on 99th  
 295 percentile of WBGT. Negative biases even occur in many areas particularly over sub-  
 296 tropical dry regions ( $< -2^\circ\text{C}$ ) when we move to 99.9th percentile. ESI exhibits small  
 297 biases (within  $\pm 1^\circ\text{C}$ ) worldwide conditional on 50th percentile of WBGT which mono-  
 298 tonically shift to strong negative biases conditional on 99.9th percentile of WBGT ( $<$   
 299  $-1^\circ\text{C}$  globally and  $< -4^\circ\text{C}$  in the low latitudes).

300 The dependence of biases on WBGT may be explained by the fact that both higher  
 301 WBGT and stronger negative (or smaller positive) bias tend to be associated with strong  
 302 solar radiation and light wind (Fig. 1). Based on the results shown here, We expect sWBGT  
 303 to largely overestimate median-level heat stress but less (or even underestimate) for more  
 304 severe heat stress (such as the hottest week or 3 days of the year). ESI, in contrast, does  
 305 a better job in measuring heat stress of median level but tend to seriously underestimate  
 306 those of more severity.

### 307 3.2.4 Biases of extreme values

308 Extreme events are of special importance in the study of heat stress. For exam-  
 309 ple, some studies attempt to identify extremely rare, short-term events in  $T_w$  in the past  
 310 30 years and going into the future (Raymond et al., 2020). The stronger negative biases  
 311 of both metrics conditional on higher percentile exceedance values of WBGT (e.g. Fig.



**Figure 4.** Biases of sWBGT (a-f) and ESI (g-l) conditional on the 50th (a, g), 75th (b, h), 90th (c, i), 95th (d, j), 99th (e, k), and 99.9th (f, l) percentile exceedance values of WBGT during 1990-2019

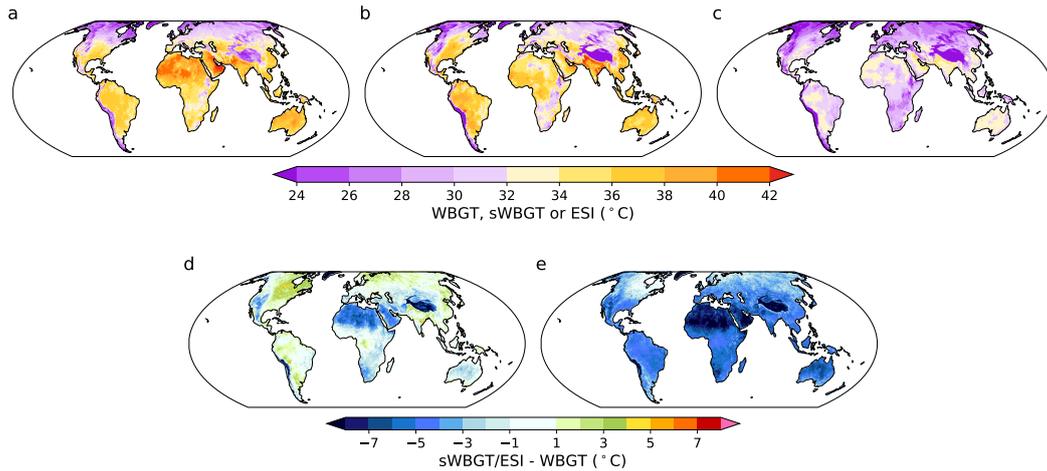
312 4f, l) raise a cautionary note that extreme heat stress at some places of the world may  
 313 be seriously underestimated. Here we implement a generalized extreme value (GEV) anal-  
 314 ysis to estimate and compare the extreme values of WBGT, sWBGT and ESI at each  
 315 grid cell. Specifically, a GEV model is fit to the annual maximum (calculated from hourly  
 316 frequency) of each metric during 1990-2019 using ERA5 reanalysis data. The metric val-  
 317 ues corresponding to a 1-in-30-year event are calculated and compared (Fig. 5).

318 Biases of extreme values share similar pattern with those conditional on 99.9 per-  
 319 centile exceedance values of WBGT yet with larger magnitudes. Even in extreme value  
 320 sWBGT produces overestimated values (by less than 3°C in tropics and other hot-humid  
 321 area and northern Eurasia, and by 3-5°C in the northeast of North America) in many  
 322 regions with the notable exception of subtropical dry regions. Large negative biases are  
 323 detected in MENA region (-4°C to -7°C) (Fig. 5d). ESI underestimates WBGT by more  
 324 than 3°C across most of the world (Fig. 5e). MENA regions stand out with strong neg-  
 325 ative biases between -6°C and -10°C.

326 The biases structure of extreme values shown here is not merely a simple exten-  
 327 sion of patterns observed at climatological mean levels. For example, relatively small bi-  
 328 ases of ESI at climatological mean level (Fig. 2g-i) suggest it is a potentially acceptable  
 329 approximation of WBGT for quantifying climatological mean heat stress or its tempo-  
 330 ral trends. Nevertheless, serious underestimations are expected when it comes to the most  
 331 extreme heat stress conditions.

### 332 **3.2.5 Local biases in specific hot-humid and hot-dry regions**

333 It is revealing to explore the bias structure in a more detailed way for two differ-  
 334 ent end-member regimes relevant to heat stress, corresponding to hot-humid and hot-



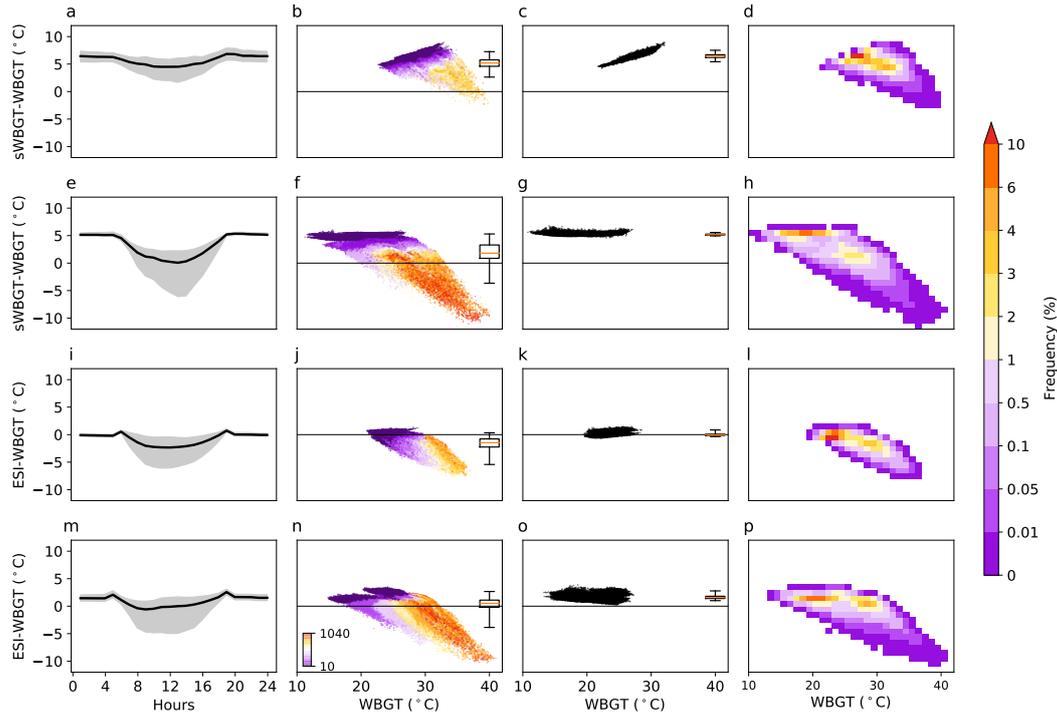
**Figure 5.** WBGT (a) and ESI (b) return levels corresponding to a 1-in-30-year event, and their differences (ESI-WBGT) (c)

335 dry climates (Buzan & Huber, 2020). Here Bangladesh and Sahara (Amazon and Ara-  
 336 bia) are selected for assessing the bias of sWBGT (ESI). Each region is characterized by  
 337 a  $2^\circ \times 2^\circ$  lat/lon box (Fig. 6).

338 Biases of sWBGT exhibit similar diurnal cycles at Bangladesh and Sahara with larger  
 339 positive biases during nighttime and smaller biases during mid-day (Fig. 6a,e) which is  
 340 consistent with previous studies (Grundstein & Cooper, 2018). sWBGT rarely under-  
 341 estimates WBGT in Bangladesh within hot-humid climate (Fig. 6a-d). Sahara, being  
 342 hot and dry, sees both positive and negative biases in daytime with the majority of cases  
 343 being positive biases (Fig. 6e-h). ESI also shows similar diurnal cycles of biases over Ama-  
 344 zon and Arabia with smaller biases in nighttime especially for Amazon (Fig. 6i,m). Dur-  
 345 ing nighttime in Arabia, ESI consistently overestimates WBGT by around  $2^\circ\text{C}$  poten-  
 346 tially as a result of low humidity (Fig. 6o).

347 Consistent with the dependence of biases on WBGT values revealed in Fig. 4, a  
 348 negative correlation between daytime biases and WBGT values is identified for both met-  
 349 rics (Fig. 6b,f,j,n). This negative correlation indicates a serious underestimation of ex-  
 350 treme heat stress by sWBGT at Sahara (up to  $-10^\circ\text{C}$  for WBGT values above  $38^\circ\text{C}$ ) and  
 351 by ESI at both Amazon (around  $-5^\circ\text{C}$  for WBGT values over  $35^\circ\text{C}$ ) and Arabia (up to  
 352  $-10^\circ\text{C}$  for WBGT values over  $38^\circ\text{C}$ ) (Fig. 6f,j,n). The underestimation of extreme heat  
 353 stress is especially severe at dry regions despite a positive bias at mean level for both met-  
 354 rics. Moreover, solar radiation appears to be negatively (positively) correlated with bi-  
 355 ases (WBGT) confirming its important role in contributing to the negative correlation  
 356 between biases and WBGT values. In addition, there is a positive correlation between  
 357 nighttime biases and WBGT values over Bangladesh (Fig. 6c) probably because both  
 358 biases and WBGT values are positively correlated with temperature and humidity. This  
 359 indicates that, when nighttime heat stress is exceptionally severe in hot-humid climate,  
 360 sWBGT tends to overestimate it even more.

361 Furthermore, Hot-dry regions have more dispersed bias distribution than hot-humid  
 362 regions. Bias spread is also much larger during daytime potentially as a result of the large  
 363 spatial and temporal variability in short-wave radiation.



**Figure 6.** Biases quantification for sWBGT over Bangladesh (23-25°N; 88-90°E) (a-d) and Sahara (22-24°N; 24-26°E) (e-h), and ESI over Amazon (1°S-1°N; 70-72°W) (i-l) and Arabia (25-27°N; 43-45°E) (m-p). The diurnal cycle of biases is plotted in the leftmost column, with the shading area corresponding to 1 to 99th percentiles. Bias scattergrams for daytime and nighttime are plotted in the middle two columns with daytime on the left and nighttime on the right. Boxplots placed within scattergram describe bias spread with box extending from the lower to upper quartile and whiskers representing 1th and 99th percentiles. Daytime scattergram is colored by surface downward solar radiation. Bias frequency heatmap for both daytime and nighttime is plotted in the rightmost column. Data used cover the period 1990-2019 with only the hottest calendar month (defined by climatological monthly average WBGT) included.

364

#### 4 Application to labor productivity estimation

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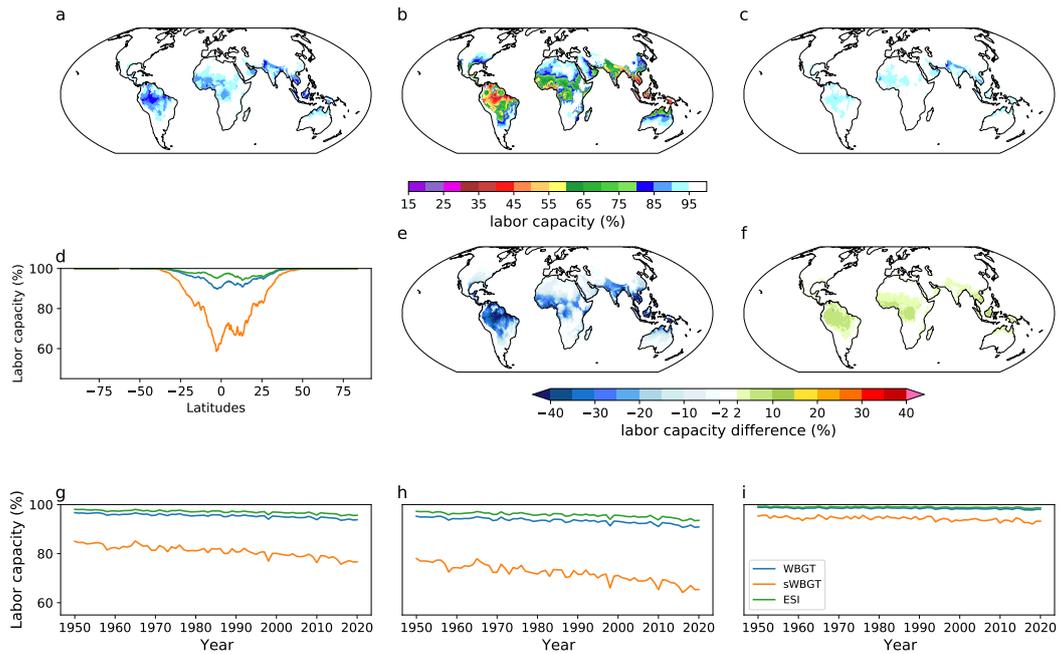
The sWBGT/ESI biases revealed above are expected to affect the downstream impact assessment of heat stress which might be assessed in many ways depending on the application. Here we take labor productivity estimation as an example to examine the impact of these biases. Labor productivity depends on working intensity measured by metabolic rate. Here we assume a metabolic rate of 415W which is classified as 'high metabolic rate' in ISO7243 standard (ISO, 2017) and representative for agriculture labor. Climatological mean annual labor productivity (1990-2019) is calculated using all three metrics from ERA5 reanalysis data (Fig. 7a-c). sWBGT vastly underestimates labor productivity (as a result of overestimating heat stress) in tropics and other hot-humid areas. The zonal average labor productivity shows large differences across equatorial area with values barely below 90% according to WBGT but as low as 60% as indicated by sWBGT. To put that in context, that bias (30%) is comparable to the labor loss in tropics predicted for a nearly 4.0 degree warming by Buzan and Huber (2020) (Fig. 10 in their paper), and the predicted global labor loss from the beginning to the end of this century under RCP8.5 scenario by Dunne et al. (2013) (Fig. 2 in their paper). ESI clearly

380 did a much better job with respect to deviation magnitudes. It overestimates annual labor  
 381 productivity by for example 5 percent in tropics (Fig. 7e,f).

382 In order to take into account population distribution and human exposure, we further  
 383 calculate population-weighted average annual labor productivity for the globe, tropics  
 384 and high latitudes during 1950-2019 (Fig. 7g-i). The discrepancy between ESI and  
 385 WBGT is much smaller and relatively stable along with time leading to similar decreasing  
 386 trends (-0.26% and -0.33% per decade respectively for global average). However, under-  
 387 estimation of labor productivity by sWBGT became increasingly large resulting in  
 388 a substantially larger decreasing trends (-1.0% per decade for global average). Namely,  
 389 positive biases in sWBGT not only cause a serious underestimation of labor productivity  
 390 but also a substantial exaggeration of labor reduction tendency. This can be explained  
 391 by the larger positive bias of sWBGT in the hot-humid regime (Fig. 1a). Heat stress over-  
 392 estimation by sWBGT will be further amplified as the world warms with increasing air  
 393 temperature and only small changes in relative humidity (Byrne & O’Gorman, 2013; Byrne  
 394 & O’Gorman, 2018; Buzan & Huber, 2020). In contrast, solar radiation and wind speed,  
 395 the main controlling factors of ESI bias, have no clear, robust changes with warming over  
 396 land.

397 Labor productivity in Fig. 7 is derived by treating both daytime and nighttime hours  
 398 as potentially available working time. However, people within the majority of industries  
 399 tend to work in daytime. Some outdoor work (such as field preparation, sowing, and crop  
 400 harvesting) may rely on daylight making working during nighttime less feasible. Hence,  
 401 we repeat the labor productivity estimation with only daytime hours included (Fig. S3).  
 402 The absolute labor productivity is reduced (comparing Fig. S3a-c with Fig. 7a-c). sWBGT  
 403 still largely underestimate labor productivity (Fig. S3e) although we remove nighttime  
 404 hours when heat stress is consistently and seriously overestimated by sWBGT (Fig. 1a).  
 405 Labor productivity overestimation by ESI becomes stronger (Fig. S3f) which is consistent  
 406 with the tendency of heat stress underestimation by ESI in daytime (Fig. 1b).

407 Here we estimate annual labor productivity from hourly data which may be not  
 408 available in most archives such as CMIP and CORDEX. It is common to see studies using  
 409 sub-daily (de Lima et al., 2021; Buzan & Huber, 2020), daily (Liu, 2020; Altinsoy  
 410 & Yildirim, 2014; Zhu et al., 2021; Kjellstrom et al., 2018; Orlov et al., 2020) or even monthly  
 411 output (Dunne et al., 2013) for similar purpose. Although not the focus of this article,  
 412 it is useful to quantify the potential error introduced thereby. Therefore, the hourly ERA5  
 413 reanalysis data are re-sampled to 8 and 4 times daily scale (calculate temporal averages  
 414 of radiation flux and re-sample instantaneous values of other fields once each 3 and 6 hours  
 415 interval), and averaged to obtain the daily mean values. The estimation of annual labor  
 416 productivity (including both daytime and nighttime hours) is then repeated under  
 417 each temporal resolution (Fig. S4). We found that labor productivity derived from daily  
 418 average inputs is substantially overestimated especially in the tropics (by around 7 to  
 419 more than 13 percent) (Fig. S4f), which is not surprising since both WBGT formula-  
 420 tion and labor productivity function are nonlinear. Particularly, all existing labor pro-  
 421 ductivity functions involve a lower threshold of WBGT (e.g. 25°C for very heavy work  
 422 with a metabolic rate of 520W according to ISO7243 standard) below which there is no  
 423 labor loss. It is likely to have a daily average WBGT below this threshold but much higher  
 424 WBGT values during peaking daytime hours in which case the labor productivity esti-  
 425 mated from daily average WBGT is too optimistic. In terms of population-weighted  
 426 global and annual average labor productivity, the adoption of daily average inputs in-  
 427 troduce a consistent overestimation by around 2.2 percent during the period 1950-2019.  
 428 Nevertheless, the derived decreasing trend is similar between hourly (-0.33 percent per  
 429 decade) and daily average inputs (-0.29 percent per decade). In comparison, the 8 or 4  
 430 times daily inputs mainly face a sampling issue (despite the time average for radiation  
 431 fields) which nevertheless only small errors of within  $\pm 1$  percent in most of the world  
 432 (Fig. S4b,d).



**Figure 7.** Annual average labor productivity for the period 1990-2019 derived from WBGT (a), sWBGT (b), and ESI (c), with the zonal average value shown in (d). Labor productivity anomaly introduced by using sWBGT (e) and ESI (f). Population weighted annual average labor productivity from 1950 to 2019 across the globe (g), low latitudes ( $30^{\circ}\text{S}$  -  $30^{\circ}\text{N}$ ) (h) and high latitudes (outside of  $30^{\circ}\text{S}$  to  $30^{\circ}\text{N}$ ) (i). Labor productivity is quantified assuming a metabolic rate of 415W.

## 433 5 Discussion

434 sWBGT was soundly criticized for missing two ambient factors contributing to heat  
 435 stress (Budd, 2008). However, it is widely applied because of its simplicity (Smith et al.,  
 436 2018; Willett & Sherwood, 2010; Kakamu et al., 2017; Cooper et al., 2016; Lee & Min,  
 437 2018; Chen et al., 2020; Schwingshackl et al., 2021; Matthews et al., 2017). Particularly,  
 438 sWBGT has been frequently adopted for estimating heat stress-induced labor produc-  
 439 tivity reduction both globally (Kjellstrom et al., 2009; Chavaillaz et al., 2019; Knittel  
 440 et al., 2020) and regionally (Liu, 2020; Altinsoy & Yildirim, 2014; Zhu et al., 2021; Zhang  
 441 & Shindell, 2021). For instance, under RCP8.5 scenario labor productivity for heavy out-  
 442 door work was predicted to decrease by 38% in Southeast Asia and the Middle East by  
 443 2050 (Knittel et al., 2020), and more than 40% in South and East China by the end of  
 444 this century (Liu, 2020); in U.S., around 1.8 billion and 4.4 billion workforce hours were  
 445 predicted to be lost annually by the 2050s and 2100s under RCP8.5 scenario (Zhang &  
 446 Shindell, 2021). Such estimates have been applied to informing adaptation strategies (Zhu  
 447 et al., 2021), or feed into economic models for assessing the downstream socioeconomic  
 448 impact (Zhang & Shindell, 2021; Chavaillaz et al., 2019; DARA, 2012). However, as we  
 449 have demonstrated, the adoption of sWBGT may have introduced substantial overes-  
 450 timation of labor and economic loss which may bias the design of greenhouse gas emis-  
 451 sion policy and decisions of mitigation and/or adaptation investments.

452 ESI has seen much less applications (de Lima et al., 2021). Its suitability depends  
 453 more on the application scenarios. The predictions of different heat stress outcomes in-  
 454 volve exposure duration of varying lengths and environmental data of different tempo-

455 ral resolutions (Vanos et al., 2020), and hence are affected by biases in varying degrees.  
 456 For instance, monitoring exertional heatstroke in bricklayers require sub-hourly environ-  
 457 ment data and will be heavily affected by the serious underestimation of extreme heat  
 458 stress by ESI during individual peaking hour with high WBGT values. The risk estima-  
 459 tion of classic heatstroke generally asks for heat stress information at daily timescale which  
 460 is then feed into epidemiological models (Vanos et al., 2020). It therefore concerns more  
 461 about biases at daily mean level. The estimates of labor productivity reduction and the  
 462 consequent economic impacts typically require heat stress information integrated over  
 463 a long period such as a year. In this case, ESI may be an acceptable approximation to  
 464 WBGT due to its relatively small biases under standard climatological conditions.

465 Many previous studies use daily (Chen et al., 2020; Schwingshackl et al., 2021) or  
 466 monthly (Newth & Gunasekera, 2018; C. Li et al., 2017; Knutson & Ploshay, 2016; C. Li  
 467 et al., 2020) average inputs to calculate one of the approximated forms of WBGT, ne-  
 468 glecting the fact that WBGT formulation is nonlinear involving nonlinear covariation  
 469 of temperature and moisture conditions. On one hand, it makes WBGT calculated from  
 470 temporally averaged inputs overestimated (Buzan et al., 2015); on the other hand, feed-  
 471 ing daily or monthly average WBGT into labor response function (Liu, 2020; Altinsoy  
 472 & Yildirim, 2014; Zhu et al., 2021; Knittel et al., 2020; Zhang & Shindell, 2021; Chavail-  
 473 laz et al., 2019; Orlov et al., 2020; Dunne et al., 2013) will result in substantial overes-  
 474 timation of labor productivity as we have shown above. For studies using daily average  
 475 sWBGT to estimate labor productivity (Liu, 2020; Altinsoy & Yildirim, 2014; Zhu et  
 476 al., 2021; Knittel et al., 2020; Zhang & Shindell, 2021; Chavallaz et al., 2019), errors in-  
 477 troduced by the metrics and the improper time scale may cancel each other to some ex-  
 478 tent. For the sake of accuracy, it is recommended to use high-temporal-resolution data  
 479 to calculate heat stress metrics involving the effects of multiple factors such as temper-  
 480 ature and humidity. In addition, a heat stress module called HumanIndexMod had been  
 481 incorporated into the Community Land Model (CLM), the land surface component of  
 482 the Community Earth System Model (CESM) since CLM4.5 (Buzan et al., 2015). It can  
 483 enable the calculation of several heat stress metrics (Liljegren’s WBGT formulation is  
 484 not included though) and thermodynamic quantities at each model time step capturing  
 485 the full nonlinearity of temperature-moisture covariation.

486 Except sWBGT and ESI, there are also several other approximations to WBGT  
 487 commonly used within heat stress literature. Orlov et al. (2020) performed a regression  
 488 analysis against WBGT calculated from Liljegren’s formulation and applied the resul-  
 489 tant 2nd order polynomial to subsequent calculations. Some studies use the psychromet-  
 490 ric wet bulb temperature ( $T_{pwb}$ ) and air temperature to replace natural wet bulb tem-  
 491 perature and black globe temperature leading to the following formula:  $WBGT = 0.7 * T_{pwb} + 0.3 * T_a$  (Dunne et al., 2013; Newth & Gunasekera, 2018; C. Li et al., 2017; Knut-  
 492 son & Ploshay, 2016; C. Li et al., 2020; Schwingshackl et al., 2021; D. Li et al., 2020).  
 493 This simplified form neglects the effects of solar radiation making it only apply to in-  
 494 door or well-shaded thermal conditions. We find that although the power of Liljegren’s  
 495 formulation has been well recognized 10 years ago (Lemke & Kjellstrom, 2012), it only  
 496 saw very limited applications (Takakura et al., 2017, 2018; Casanueva et al., 2020; Ja-  
 497 cobs et al., 2019; Orlov et al., 2019). One potential reason is that Liljegren’s approach  
 498 is computationally intensive since it requires iterative calculations and careful treatment  
 499 of latitude, date, and the time of day to get solar radiation correct (Orlov et al., 2020).  
 500 Moreover, Liljegren’s original code was written in C and Fortran language which may  
 501 be not familiar to most end-users. To tackle this problem, we rewrote the code in Cython  
 502 which is fast, easy to use in Python and scales well for large dataset. Leveraging on par-  
 503 allel computing enabled by Dask, it takes around half a minute to calculate one-year WBGT  
 504 at 3-hourly frequency for a GCM with a spatial resolution of  $1.5^\circ \times 1.5^\circ$  using one node  
 505 (24 cores) of Brown cluster at Purdue University. We include Liljegren’s original formu-  
 506 lation as well as the modified version to take advantage of the full set of radiation com-  
 507

508 ponents in climate model output. Please find the details of code availability in the Ac-  
 509 knowledgement section.

## 510 6 Summary and conclusions

511 We explicitly calculated Liljegren's formulation for WBGT and assessed the per-  
 512 formance of two previously used, simple approximations WBGT-sWBGT and ESI-against  
 513 it. The bias structure across the 4-D climatic (atmospheric temperature, shortwave ra-  
 514 diation, specific humidity, wind speed) space of this bias was explored within an ideal-  
 515 ized context. Within this idealized framework, sWBGT is expected to overestimate WBGT  
 516 during nighttime and under hot-humid days. Both approximate metrics tend to under-  
 517 estimate WBGT within sunny, calm days. An overestimation by ESI may occur under  
 518 dry nighttime conditions. We also explored the bias distribution driven by ERA5 reanal-  
 519 ysis data computed at hourly resolution (from 1990-2019) and find results which are con-  
 520 sistent with the structure revealed under idealized context. Under standard climatolog-  
 521 ical conditions, we identify a substantial overestimation by sWBGT across the world and  
 522 considerably smaller biases for ESI. Nevertheless, biases tend to be negatively correlated  
 523 with WBGT values suggesting a potentially serious underestimation of most extreme heat  
 524 stress values by both metrics especially in subtropical dry regions.

525 Given the large biases of sWBGT, we can not recommend it as a suitable approx-  
 526 imation to WBGT, which raises serious questions about prior work, since this is the most  
 527 commonly used approximation in previous studies. Studies using sWBGT to approxi-  
 528 mate WBGT need to be reevaluated as likely systematically overestimate heat stress and  
 529 its impacts over most of the Earth, most of the time, while underestimating the sever-  
 530 ity of the most extreme (>99.9 percentile exceedance). ESI is more suitable for many  
 531 applications and it's appropriateness depends more on the application purposes. It may  
 532 be acceptable for evaluating heat stress at climatological mean level or the integrative  
 533 downstream impact over a long period (such as annual labor productivity). However,  
 534 the expected serious underestimation of most extreme heat stress makes it less suitable  
 535 for epidemiological studies (i.e. on morbidity and mortality), extreme heat stress anal-  
 536 ysis, or as an operational index for heat warning, heatwave forecasting or guiding activ-  
 537 ity modification at workplace.

538 Nevertheless, Liljegren's explicit formulation of WBGT should be preferred over  
 539 these ad hoc approximations. Our code is straightforward to use and well suited for cal-  
 540 culating WBGT from large-size climate model output and reanalysis data.

## 541 Notation

542  $c_p$  specific heat of dry air at constant pressure ( $J \cdot kg^{-1} \cdot K^{-1}$ )

543  $D$  diameter of wick (m)

544  $e_a$  ambient vapor pressure (hPa)

545  $e_w$  vapor pressure at the surface of the wick (hPa)

546 **ESI** environmental stress index ( $^{\circ}C$ )

547  $f_{dir}$  fraction of the total horizontal solar irradiance due to the direct beam of the sun

548  $h$  convective heat transfer coefficient for the wick or black globe ( $W \cdot m^{-2} \cdot K^{-1}$ )

549  $L$  length of wick (m)

550  $L_{down}$  Surface downward long-wave radiation ( $W \cdot m^{-2}$ )

551  $L_{up}$  Surface upwelling long-wave radiation ( $W \cdot m^{-2}$ )

552  $M$  metabolic heat production rate (W)

553  $M_{Air}$  molecular weight of dry air (kg)

554  $M_{H_2O}$  molecular weight of water vapor (kg)

555 **RH** Relative humidity (%)

556	<b><math>Sc</math></b> Schmidt number
557	<b>sWBGT</b> simplified wet bulb globe temperature ( $^{\circ}\text{C}$ )
558	<b><math>S_{down}</math></b> Surface downward solar radiation ( $\text{W} \cdot \text{m}^{-2}$ )
559	<b><math>S_{up}</math></b> Surface upwelling solar radiation ( $\text{W} \cdot \text{m}^{-2}$ )
560	<b><math>T_a</math></b> ambient air temperature (K)
561	<b><math>T_g</math></b> Black globe temperature (K)
562	<b><math>T_{sfc}</math></b> surface temperature (K)
563	<b><math>T_w</math></b> natural wet bulb temperature (K)
564	<b><math>P</math></b> surface pressure (hPa)
565	<b><math>Pr</math></b> Prandtl number
566	<b>WBGT</b> wet bulb globe temperature (K)
567	<b><math>WBGT_{lim}</math></b> WBGT limit reference value (K)
568	<b><math>WBGT_{lim,rest}</math></b> WBGT limit reference value under resting metabolic rate (117 W) (K)
569	<b><math>\alpha_g</math></b> albedo of the globe
570	<b><math>\alpha_{sfc}</math></b> surface albedo
571	<b><math>\alpha_w</math></b> albedo of the wick
572	<b><math>\sigma</math></b> Stefan-Boltzmann constant ( $\text{W} \cdot \text{m}^{-2} \cdot \text{K}^{-4}$ )
573	<b><math>\epsilon_a</math></b> emissivity of the atmosphere
574	<b><math>\epsilon_g</math></b> globe emissivity
575	<b><math>\epsilon_{sfc}</math></b> surface emissivity
576	<b><math>\theta</math></b> Solar zenith angle (radian)
577	<b><math>\Delta F_{net}</math></b> net radiative gain by the wick from the environment (W)

## 578 Acknowledgments

579 Hersbach, H. et al., (2018) was downloaded from the Copernicus Climate Change Ser-  
580 vice (C3S) Climate Data Store (<https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-single-levels?tab=overview>). Bell, B. et al., (2020)  
581 was downloaded from the Copernicus Climate Change Service (C3S) Climate Data Store  
582 (<https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-single-levels-preliminary-back-extension?tab=overview>). The results contain modi-  
583 fied Copernicus Climate Change Service information 2020. Neither the European Com-  
584 mission nor ECMWF is responsible for any use that may be made of the Copernicus in-  
585 formation or data it contains. Center for International Earth Science Information Net-  
586 work - CIESIN - Columbia University (2018) was downloaded from [https://sedac.ciesin](https://sedac.ciesin.columbia.edu/data/set/gpw-v4-population-count-adjusted-to-2015-unwpp-country-totals-rev11)  
587 [.columbia.edu/data/set/gpw-v4-population-count-adjusted-to-2015-unwpp](https://sedac.ciesin.columbia.edu/data/set/gpw-v4-population-count-adjusted-to-2015-unwpp-country-totals-rev11)  
588 [-country-totals-rev11](https://sedac.ciesin.columbia.edu/data/set/gpw-v4-population-count-adjusted-to-2015-unwpp-country-totals-rev11). Liljegren's WBGT code in C language is accessible at [https://](https://github.com/mdljts/wbgt/blob/master/src/wbgt.c)  
589 [github.com/mdljts/wbgt/blob/master/src/wbgt.c](https://github.com/mdljts/wbgt/blob/master/src/wbgt.c). Our WBGT code along with  
590 a Jupyter notebook introducing its usage are stored within a private repository at Github  
591 and will be published and deposited at Zenodo upon the acceptance of this paper. For  
592 review purpose, the repository can be temporarily viewed at [https://gitfront.io/r/](https://gitfront.io/r/user-1452352/bf213c1f4de06259246d8974f7f16f5be77afc1e/PyWBGT/)  
593 [user-1452352/bf213c1f4de06259246d8974f7f16f5be77afc1e/PyWBGT/](https://gitfront.io/r/user-1452352/bf213c1f4de06259246d8974f7f16f5be77afc1e/PyWBGT/). Hosted in  
594 the same repository are several other Jupyter notebooks and processed dataset that can  
595 be used to reproduce all figures in this paper. A Binder project will be created for this  
596 repository once it is published which will enable readers run Jupyter notebooks with-  
597 out installing any packages. Data analyses were performed on Purdue University's high-  
598 performance computing cluster using Python (Van Rossum & Drake, 2009) and CDO  
599 (Schulzweida, 2019). The following Python packages were utilised: Numpy (Harris et al.,  
600 2020), Scipy (Virtanen et al., 2020), Xarray (Hoyer & Hamman, 2017), Dask (Dask De-  
601 velopment Team, 2016), Matplotlib (J. D. Hunter, 2007), Cartopy (Met Office, 2010 -  
602 2015), and pyMannKendall (Hussain & Mahmud, 2019). The authors declare no com-  
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604  
605

606 Nexus of Food, Energy, and Water Systems (INFEWS: U.S.-China): A multi-scale in-  
 607 tegrated modeling approach to managing the transition to sustainability and NSF 1829764-  
 608 OAC CyberTraining: CIU:Cross-disciplinary Training for Findable, Accessible, Interop-  
 609 erable, and Reusable (FAIR) science

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