

# Sensitivity of Convection Permitting Simulations to Lateral Boundary Conditions in Idealised Experiments

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## Key Points:

- The nesting challenge of convection-permitting climate modelling (CPM) is investigated with idealised simulation experiments
- Nesting the CPM into host simulations with grid-spacing in the grey zone of convection is not better than into coarser simulations
- Fraction of the CPM domain is small suggesting a larger domain even at the expense of CPM grid-spacing coarser than usually accepted

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**Abstract**

Limited-area convection-permitting climate models (CPMs) with horizontal grid-spacing less than 4 km are being used more and more frequently. CPMs represent small-scale features such as deep convection more realistically than coarser regional climate models (RCMs), and thus do not apply deep convection parameterisations (CPs). Because of computational costs CPMs tend to use smaller horizontal domains than RCMs. As all limited-area models (LAMs), CPMs suffer issues with lateral boundary conditions (LBCs) and nesting. We investigated these issues using idealised so-called Big-Brother (BB) experiments with the LAM COSMO-CLM ( $\approx 2.4$  km). Deep convection was triggered by idealised hills with driving data from simulations with different spatial resolutions, with/without a deep CP, and with different nesting frequencies and LBC formulations. All our nested idealised 2.4 km Little-Brother (LB) experiments performed worse than a coarser CPM simulation (4.9 km) using a four times larger computational domain, but with only 50% computational cost. A boundary zone of  $> 100$  grid-points of the LB could not be interpreted meteorologically because of spin-up of convection and boundary inconsistencies. A host with grid-spacing in the so-called grey zone of convection (ca. 4 - 20 km) was not advantageous to the LB performance compared to an even coarser host. The LB performance was insensitive to the applied LBC formulation and updating (3-hourly or better). Therefore, our CPM experiments suggested opting for a larger domain instead of a higher resolution even if coarser than usual (i.e.,  $> 4$  km). Better preconditioning the convectivity at the CPM inflow boundaries might decrease the spin-up zone's depth.

**Plain Language Summary**

Recently, very high resolution (grid-spacing  $< 4$  km) so-called convection-permitting climate models (CPMs) were developed, which represent deep convection explicitly. CPMs, however, are computationally very expensive. They need information about the state of the atmosphere at their lateral boundaries from coarser models. This paper investigates the setting of the lateral boundary formulation. We used idealised experiments with grid-spacing of  $\approx 2.4$  km, where deep convection was triggered by small hills. We found that a CPM boundary zone  $> 100$  grid points can not be interpreted reliably. The boundary data should be given to the CPM every 3 hours or more often. The CPM simulations all performed not as well as a reference simulation on a larger domain with the same high or even two times lower resolution. We tested different resolutions of the driving data for the CPMs and found that driving data from a model in the "grey zone" of convection (about 4 to 20 km) is not advantageous for the CPM performance. We concluded that it often might be better to opt for a larger domain with an unusually coarse CPM resolution ( $\geq 4$  km) than for a smaller domain with grid-spacing  $< 4$  km.

**1 Introduction**

Regional climate models (RCMs) have been developed with the aim to represent regional scale climate processes better than global climate models (GCMs). With this downscaling of driving global climate projections, results can be applied in regional climate assessments (Giorgi, 2019). The added value of limited-area RCM downscaling is dependent on many factors (like the quality of the driving GCM simulation, consistency of RCM and GCM physics, RCM's domain size, resolution jump, formulation of lateral boundary conditions (LBCs)). The impact of the used nesting approach, i.e. the formulation of LBCs, numerical grid resolution jump from driving GCM to RCM, and the update frequency of driving data, is still under debate (Becker et al., 2015; T. Davies, 2014; Matte et al., 2016; Leps et al., 2019; Li et al., 2020).

The first month-long climate simulations used grid-spacing of 60 km (Giorgi & Bates, 1989). Since then, RCM simulations got more complex, multi-centennial, and used better grid resolutions. In CORDEX (Coordinated REgional Climate Downscaling Exper-

63 iment), for example, a default grid-spacing of about 50 km was suggested to be used in  
64 multiple domains covering all global continents (<https://cordex.org/>, Giorgi et al. (2009)),  
65 but finer grid-spacing was already suggested and later on used (e.g., 12 km in EURO-  
66 CORDEX, <https://www.euro-cordex.net>, or CORDEX-CORE, Sorland et al. (2021)).  
67 This, however, results in RCMs being used in the so-called grey zone of convection, i.e.,  
68 in a grid-spacing range of about 4 - 20 km. Here, the assumptions of the deep convec-  
69 tion parameterisations (CPs) used in climate models are not well fulfilled (Weisman et  
70 al., 1997).

71 Recently, limited-area convection-permitting climate models (CPMs) with grid-spacing  
72 below 4 km were developed and successfully applied (Kendon et al., 2012; Ban et al., 2014;  
73 Prein et al., 2015; Ban et al., 2021; Purr et al., 2021). These CPMs resolve much of deep  
74 convection processes and do not use any deep CP. Because of their spatiotemporal very  
75 high resolution, the CPMs are computationally very expensive and at present feasible  
76 only over smaller and/or shorter climate periods than RCMs (Ban et al., 2021).

77 In a convection-permitting simulation with grid-spacing of 2.8 km, Brisson et al.  
78 (2015) found an extended spatial spin-up zone at the lateral boundaries, especially at  
79 the primary inflow boundary, which the simulated convective systems need to fully de-  
80 velop. They investigated the nesting strategy, and concluded that an additional nest-  
81 ing step in the grey zone of convection with 7 km grid-spacing is not beneficial for the  
82 CPM simulation compared to a direct nesting into a driving simulation with grid-spacing  
83 of 25 km (i.e. with a resolution jump of about a factor of 10). The simulation experiments  
84 by Panosetti et al. (2019) have shown that convective processes are simulated climato-  
85 logically robust (the simulations achieved bulk convergence) in case of strong orographic  
86 forcing (in a domain over the European Alps) and less robust in hilly terrain over Cen-  
87 tral Germany. They concluded that a coarse-grid CPM with grid-spacing of 4.4 km might  
88 be sufficient in the mid-latitudes in cases with strong forcing. Typical grid-spacings in  
89 real-data applications, however, are 3 km and finer (as, e.g., in Ban et al. (2021) which  
90 evaluates several CPMs over the European Alps).

91 Figure 1 illustrates the CPM nesting challenge we want to investigate here. The  
92 simulated precipitation amounts shown are from RCM and CPM simulations discussed  
93 in Purr et al. (2019). The RCM was driven by the European Centre for Medium-Range  
94 Weather Forecast Interim Reanalysis (ERA-Interim) from 1979 to 2015 using a European-  
95 scale domain with horizontal grid spacing of  $0.22^\circ$  ( $\approx 25$  km). The CPM with a domain  
96 over Germany with grid-spacing of  $0.025^\circ$  ( $\approx 2.8$  km) was nested into the RCM simu-  
97 lation laterally nudged towards the driving data using Davies relaxation (H. C. Davies,  
98 1976) using hourly updates of the LBCs provided by the RCM. The CPM simulated about  
99 40% more precipitation at the 309 most convectively active days in the simulation pe-  
100 riod. Yet, the CPM simulates less precipitation in a spin-up zone along the primary in-  
101 flow boundary from the South-West.

102 This study investigates the challenge of nesting CPM into RCM simulations by us-  
103 ing idealised experiments. It explores the dependence of the added value of CPM sim-  
104 ulations nested in coarser simulations on resolution jumps (which implies decreasing qual-  
105 ity of the coarser driving simulation), LBC update frequencies, and LBC formulation.  
106 We aim to provide additional guidance in planning CPM climate simulations.

107 The following section introduces the idealised simulation experiments applied us-  
108 ing a modified Big-Brother experiment design (Leps et al., 2019) and the applied limited-  
109 area climate model and its set-up. Section 3 presents and discusses the idealised simu-  
110 lation results. Finally, we summarise and draw conclusions.

**Figure 1.** Mean daily precipitation of 309 convective days from climate simulations with an RCM (left) and nested CPM (right) in a domain over Germany in the period 1983–2015.

## 111 2 Method, Model and Experiments

112 In this study, we used the modified Big-Brother-Experiment protocol as introduced  
 113 in Leps et al. (2019). First, an idealised simulation was performed using a large domain  
 114 with a high, convection-permitting resolution, called the Big-Brother (BB) simulation.  
 115 This simulation drove, i.e. provided lateral boundary and initialisation conditions for,  
 116 a simulation on a smaller domain but otherwise the same set-up as the BB set-up. The  
 117 small domain simulation is called the Little-Brother (LB) simulation and is chosen to  
 118 have a typical domain size as in studies with realistic simulations (e.g., in Brisson et al.  
 119 (2021); Purr et al. (2021)). So-called Coarse-Brother (CB) simulations were performed  
 120 on the BB domain with a coarser resolution to represent input data from a coarser model.  
 121 CB simulations also drove LB simulations, and the BB simulation was used as the refer-  
 122 ence for the LB and CB simulations. With this protocol, it was possible to show the  
 123 impact of nesting, the update frequency,  $U$ , of LBCs, and the resolution jump,  $J$ , from  
 124 CB to LB set-ups. The following sub-sections give the details.

### 125 2.1 Model and reference Big-Brother set-up

126 The non-hydrostatic LAM COSMO-CLM (e.g., Rockel et al. (2008)) in version COSMO5.0-  
 127 CLM7 was applied in idealised test configurations. COSMO-CLM has been used suc-  
 128 cessfully in many climate studies with typical grid-spacings from  $\sim 50$  km to convection-  
 129 permitting scales with grid-spacing of  $\mathcal{O}(1)$  km (Sorland et al., 2021; Purr et al., 2021).  
 130 Necessary initial and lateral boundary data were compiled with the pre-processor INT2LM2.0-  
 131 CLM4.

132 The reference set-up which was used to perform the reference simulation for later  
 133 sensitivity experiments is called Big-Brother (BB) set-up. We used a one-moment mi-  
 134 crophysics scheme and shallow convection is parameterized using the convection scheme  
 135 after Tiedtke (1989). In the reference simulation no deep CP was used. The used radi-  
 136 ation scheme follows Ritter and Geleyn (1992), and the lower boundary condition were  
 137 provided by the sub-model TERRA (with homogeneous land cover: short grass, rough-  
 138 ness length 0.01 m) and turbulence scheme as documented in Doms et al. (2018). The  
 139 Coriolis force term was switched off in all simulations.

140 The BB set-up used a horizontal grid-spacing of  $0.022^\circ$  ( $\approx 2.4$  km), 50 vertical lev-  
 141 els, numerical time steps of 20 s, and a cartesian simulation domain of  $1006 \times 452$  grid  
 142 points (domain area:  $\approx 2430 \times 1100$  km<sup>2</sup>). This domain size is large enough to host two  
 143 non-overlapping domains with an order of size typical in CPM studies (e.g., Brisson et  
 144 al. (2015) or Panosetti et al. (2019)). The BB simulation was run for 24 hours with pe-  
 145 riodic LBCs (with 6 grid point wide overlapping boundary zones). The simulation orog-  
 146 raphy is mainly flat with twelve Gaussian hills (height = 450 m, half-width = 25 km)  
 147 in the western part of the domain. These hills are planted into the domain to trigger deep  
 148 convection in the simulation, but are rather smooth aiming not to provide too strong forc-  
 149 ing. They resemble hilly terrain in central Germany and not alpine terrain. Panosetti  
 150 et al. (2019) have shown that simulations with km-scale grid-spacing are more robust  
 151 with strong orographic forcing from the European Alps than with weaker central Ger-  
 152 man orographic forcing. The BB domain with the locations of the hills is sketched in Fig. 2.

153 The simulation was initialised with a Weisman and Klemp (1982)–wind shear pro-  
 154 file as implemented by Blahak (2015) with a mean zonal wind speed of 20 m/s above 6 km,  
 155 potential temperatures/relative humidities of 300 K/1 and 343 K/0.25 at the profile base  
 156 at 0 m and the tropopause in 12 km, respectively. The zonal speed implies a parcel ad-  
 157 vection time of  $\approx 34$  h from the inflow to the outflow boundary.

**Figure 2.** Domain of the reference simulation BB (blue) and two nested LB domains (orange). Black dots indicate the locations of the Gaussian hills. The left LB domain is used for the "orographic" and the right one for the "inflow" experiments.

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## 2.2 Coarse-Brother set-up

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Five different Coarse-Brother (CB) 24-h simulations were performed with COSMO-CLM, covering the BB domain. Due to the overlapping zone for the periodic boundary conditions, the CB domains are slightly larger than the BB domain (interior domains are identical). Three grid spacings frequently used in RCMs, i.e.  $0.11$ ,  $0.22$ , and  $0.44^\circ$ , and additionally  $0.044^\circ$  were used. Thus, the CB simulations are 2, 5, 10, and 20 times coarser than the reference BB simulation. Table 1 summarizes the domain set-ups. The idealised hills were smoothed (yielding lower heights and larger half-widths, but keeping the same volume as in the BB set-up) as is usually the case with coarser model grids.

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Following, for example Weisman et al. (1997); Brisson et al. (2017), these CB simulations resolve deep convection partly at best and therefore deep convection processes are usually parameterised here using the Tiedtke (1989) scheme in addition to the shallow convection processes. Later we show results with deep convection switched on and switched off to explore the behaviour of the simulations in the grey zone of convective parameterisations. In addition, we show some results with CP triggering by CAPE threshold instead of low-level moisture convergence threshold which is the default in COSMO-CLM. LBCs and initialization was done as in the BB set-up.

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Table 1 gives approximate values of the relative computational processing times for the different CB simulations. The 12-km CB simulation needs only about 1% computing time compared to the BB reference simulation. Additionally, the CB simulations are also much cheaper in terms of necessary memory resources. The difference in cost of switching on or off the deep CP is negligible.

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## 2.3 Little-Brother set-up

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The Little-Brother (LB) simulations were driven by BB and CB simulations in order to quantify the impact of typical scale jumps  $J$  between driving and driven simulations (see Tab. 1) and of the update frequency (i.e. the frequency of availability of driving data per day)  $U$ . The set-up of numerics and physics of the LB simulations were the same as in the BB simulations, but using different domain size and replacing the periodic LBCs and initialization with driving data provided by the BB and CB simulations.

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The LB simulations covered domains of  $400 \times 300$  grid points (about  $980 \times 730 \text{ km}^2$ ). Two different LB domain locations within the BB domain were chosen (Fig. 2). The western LB domain includes the hills and thus represents a region, where orographic triggering of deep convection occurs. The eastern domain in contrast represents a region, where convective cells are advected into the domain through its lateral boundaries.

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We chose typical driving frequencies  $U \in \{96, 24, 8, 4\}/\text{day}$  (every 15 minutes, hourly, 3- and 6-hourly). The available driving data were interpolated linearly in between to provide the necessary LBCs for the LB simulation for every numerical time-step. COSMO-CLM uses the Davies relaxation approach H. C. Davies (1976). Here, all driven variables are prescribed at all lateral boundaries, which means the problem is over-specified (too much information is given at the lateral boundaries). A sponge zone is introduced to buffer any spurious noise developing at the lateral boundary, where the internal model solution is relaxed toward the driving data. Leps et al. (2019) implemented another approach based on Mesinger (1977) which prescribes less information at the outflow boundaries. We call this approach Mesinger approach. More details on the formulation of the LBCs are given in Leps et al. (2019).

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As Tab. 1 shows each of the LB simulations costs about 26% of the reference BB simulation and about twice as much as the 4.9-km CB simulation in terms of processing time.

**Table 1.** Properties of domains and simulations.

Set-up	grid-spacing	grid points	time step	jump $J$	processing time
BB	$0.022^\circ \approx 2.4$ km	$1006 \times 452$	20 s	1	100 %
CB	$0.044^\circ \approx 4.9$ km	$506 \times 232$	45 s	2	13 %
	$0.11^\circ \approx 12$ km	$206 \times 100$	90 s	5	1 %
	$0.22^\circ \approx 24$ km	$106 \times 56$	180 s	10	0.3 %
	$0.44^\circ \approx 49$ km	$56 \times 34$	300 s	20	0.09 %
LB	$0.022^\circ \approx 2.4$ km	$400 \times 300$	20 s	1	26 %

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## 2.4 Statistics

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The simulations of BB, CBs, and LBs were compared using simple statistics of simulated 15-min precipitation: (i) total sum, and (ii) the spatial mean of the grid-point time series' standard deviation. The latter is called transient-eddy standard deviation in Matte et al. (2017) (used for evaluation of spatial spin-up on limited-area simulations). The ratios of the respective statistics, called *sumr* and *tsdr*, were taken as one-value statistics in the comparisons (as in Ahrens et al. (1998)) with the BB reference values as denominators. Thus, simulations yielding *sumr*, *tsdr* values of one match the reference perfectly well measured by these statistics. If not mentioned otherwise, the comparisons were done for each of the LB domains separately reduced by 15 LB grid-points along the boundaries to avoid direct nesting effects in the boundary zones.

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## 3 Results and Discussion

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We show and discuss the reference BB and coarse driving CB simulations first, and then the LB simulations nested into the driving simulations BB and CB with different scale jumps  $J$  and of lateral boundary conditions (LBCs) update frequency  $U$ .

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### 3.1 Driving Simulations BB, CB

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Figure 3 shows the precipitation sum of one simulation day for the reference BB and different coarser CB simulations. The reference BB simulation shows precipitation largely orographically triggered by the Gaussian hills. The impact of the periodic boundary conditions in meridional direction can be seen too. Precipitating systems were not advected to or triggered near the outflow boundary within the simulated 24 h. The Fig. shows two CB simulations with the deep CP switched off. With twice as coarse grid-spacing ( $J = 2$ , CP = off) the pattern looks similar to the reference yet rougher (with intensified precipitation tracks). As Tab. 2 and Fig. 4 show, this CB simulation reduced the precipitation sum and temporal variability by about 15 % in the orographic domain and by less than 5 % in the inflow domain. The five times coarser CB simulation ( $J = 5$ , CP = off) shows delayed precipitation triggering and further reduced precipitation amounts and variability, especially in the orographic domain (Tab. 2). For  $J = 5$ , i.e. with grid-spacing of  $\approx 12$  km, the mountain drag of the hills with a half-width of 25 km is already largely underestimated by the numerical scheme following L. Davies and Brown (2001). It should be noted that with using COSMO-CLM's sub-gridscale orography parameterisation the degradation of simulation quality with increased grid-spacing would be smaller (Obermann-Hellhund & Ahrens, 2018).

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The coarse CB simulations with CP switched on, using low-level moisture convergence triggering produced only up to 56 % ( $J = 2$ , CP = on) and as little as 22 % ( $J = 20$ , CP = on) precipitation and even less variability (Figs. 3, 4, and Tab. 2). Thus, the

**Table 2.** Relative precipitation sums (*sumr*) and relative transient-eddy standard deviations (*tsdr*) of the CB simulations compared to the reference BB simulation in the two evaluation areas in the orographic and inflow LB domains (cf. Fig. 2).

set-up		orographic		inflow	
<b>J</b>	<b>param.</b>	<b>sumr</b>	<b>tsdr</b>	<b>sumr</b>	<b>tsdr</b>
2	off	84 %	84 %	97 %	96 %
2	on	56 %	38 %	32 %	22 %
2	on(CAPE)	81 %	66 %	47 %	47 %
5	off	43 %	42 %	95 %	89 %
5	on	43 %	25 %	37 %	28 %
5	on(CAPE)	72 %	66 %	52 %	56 %
10	on	45 %	25 %	29 %	17 %
20	on	28 %	17 %	22 %	12 %

simulation with grid-spacing  $J = 2$ , i.e.  $\approx 4.9$  km, with CP = on performed much worse than with CP = off. Obviously, the CP reduced instability too much and suppressed grid-scale convective precipitation. The simulation with the grey zone grid-spacings of  $\approx 12$  and the one with  $\approx 24$  km were similar with further degradation of simulation quality when increasing grid-spacing to  $\approx 49$  km. The CB quality was slightly better with orographic forcing than in the inflow evaluation domain without the orographic forcing. Interestingly, simulations with CAPE triggering of convection were better in terms of amount and variability than with moisture convergence triggering in our test set-up, but still convective activity was strongly suppressed as the underestimation of amount and variability by more than 50% in the inflow domain shows in case of  $J = 2$  and CP = on. Additionally, the characteristic precipitation tracks as simulated in the CP = off simulation are not visibly in the CAPE simulations (not shown). Overall, there was a decrease of simulation quality with increasing grid-spacing, and without internal forcing by hills. Here, the limitations of the Tiedtke-like CP will not be further discussed, but its weakness shows less with strong forcing.

The results show that the CB simulations are useful idealised coarse-grid host simulation for the nested LB simulations to be discussed in the following.

### 3.2 Driven Simulations LB

Next to the quality of the driving simulations, Fig. 4 shows the quality, as measured with *sumr* and *tsdr*, of LB simulations driven by BB and CB simulations, with different LBC update frequencies  $U$ . The quality of the output of LB simulations driven by the reference BB (with identical grid in the LB domain) was substantially degraded in comparison to the BB data. The precipitation sum was underestimated by about 30% and more in both the orographic and the inflow LB domain depending on update frequency  $U$ . The transient-eddy variability was underestimated by about 10% in the orographic domain and up to about 30% in the inflow domain by the LB simulations with LBC update only every six or three hours ( $U = 4/\text{day}$  or  $8/\text{day}$ , respectively), and much better represented with hourly or 15-min updates ( $U = 24/\text{day}$  or  $96/\text{day}$ , respectively). The LB results were less sensitive on update frequency in the orographic than in the inflow domain, with orographic precipitation triggered by the hills in the orographic domain and not well inherited from the BB simulation at the inflow boundary.

Figure 5 shows the precipitation sums as simulated in the two LB domains with hourly LBC update ( $U = 24/\text{day}$ ). The LB driven by BB simulation in the orographic

**Figure 3.** Simulated precipitation sum by the reference, BB (top panel), and coarser, CB, simulations. The grid-spacing increases from  $0.022^\circ$  to  $0.44^\circ$  from top to bottom row. The left column shows results with deep convection parameterisation switched off, the right column with deep convection parameterisation switched on. The blue and orange boxes show BB and LB domains, respectively, as in Fig. 2.

**Figure 4.** Scatter diagram of the BB, CB, and LB simulations' relative precipitation sums (*sumr*) vs. relative transient-eddy standard deviations (*tsdr*) in the two evaluation areas in the orographic (left) and inflow (right) LB evaluation domains (cf. Fig. 2).

275 domain underestimates the impact of the hills in or near the western, inflow boundary  
 276 zone. This generates a substantial spin-up zone of about 80-100 grid-points depth. This  
 277 deep spin-up zone can be seen for all  $U$  and is largest for 6-hourly updates (Fig. 6). There  
 278 is a large overestimation of precipitation by the LB in the western inflow boundary zone.  
 279 In this zone, inconsistency between the interpolated driving and driven simulations gener-  
 280 ate disturbances and subsequently rainfall, but here, because of small absolute values,  
 281 the small absolute errors generated large relative errors. The inflow domain simulation  
 282 shows the deep spin-up zone too and too much precipitation close to the eastern, out-  
 283 flow boundary (Fig. 5 and 6). This backwatering of inconsistencies and subsequent pre-  
 284 cipitation near the outflow boundary was observed in real-data regional climate mod-  
 285 elling experiments too (see (T. Davies, 2014)). But, again, the BB simulation produced  
 286 only small precipitation amounts in this region yielding large relative errors. Still, the  
 287 Figs. indicate that, using perfect driving data even with 15-min LBC update, only ap-  
 288 proximately the inner 50% of the domain in zonal direction provided good simulation  
 289 results.

290 Nesting in the  $0.044^\circ$ , i.e.  $J = 2$ , CB simulation with deep CP switched off pro-  
 291 vided quality comparable to nesting into the reference simulation (Figs. 4, 5 and 6) in  
 292 the orographic domain. In the inflow domain, there was stronger precipitation overes-  
 293 timation in a deeper zone at the outflow boundary (Fig. 6). Nesting the LB into  $J =$   
 294 2 with deep CP switched on gave the worst results of all nesting experiments (Fig. 4).  
 295 The LBs precipitation processes were strongly suppressed (Figs. 5 and 6). Sensitivity to  
 296 the update frequency is again small in the orographic domain compared to the inflow  
 297 domain. All the nested LB simulations performed worse averaged over the evaluation  
 298 domains than the  $0.044^\circ$  CB simulation with deep DP switched off. Additionally, the  
 299 CB simulation with  $J = 2$  spent only 13% of the computing time while a LB simula-  
 300 tion needed 26% compared to a BB simulation.

301 Interestingly, LB simulations nested into the CB domain with  $\approx 12$  km grid-spacing  
 302 ( $0.11^\circ$ , scale jump  $J = 5$ , and deep CP switched on) did not improve the average re-  
 303 sults in the orographic domain (Fig. 4). As Fig. 6 shows, the LB simulations suffered dam-  
 304 aging spin-up at the inflow boundary of more than 150 grid-points (about 40% of the  
 305 zonal domain extent). The results in the inflow domain are slightly better, with enough  
 306 disturbances provided at the inflow boundary to generate precipitation. Beyond the spin-  
 307 up region the precipitation amounts are comparably well to nesting into the BB simu-  
 308 lation.

309 The results with CB  $J = 10$  are better on average. The domain average results  
 310 are even comparable to the results by nesting into the BB simulation. But, as Fig. 6 shows  
 311 the underestimation of precipitation in a somewhat smaller spin-up zone than in case  
 312  $J = 5$  is compensated by an overestimation deeper into the domain. For the inflow do-  
 313 main with  $U = 24/\text{day}$  and  $96/\text{day}$ , precipitation is overestimated substantially (up to  
 314 100%) in a zone of more than 100 grid points at the zonal outflow boundary (Fig. 6).

315 Surprisingly, in the orographic domain the LB nested into the coarsest CB simu-  
 316 lation with a scale jump of  $J = 20$  produced the best total precipitation amount (Fig. 4).  
 317 But, there is an extended spin-up zone underestimation which is later on compensated  
 318 by overestimation ( $> 50\%$  in the central region of the domain, Fig. 6). The mean qual-  
 319 ity in the inflow nesting experiment was comparable to the other experiments. They all  
 320 show the degraded quality at the outflow boundary. Still, Fig. 5 gives the impression that  
 321 the simulated precipitation pattern deviates strongest from the BB pattern. The pat-  
 322 tern is dominated by artefacts at the boundaries (compensated by an underestimation  
 323 in the domain centre, Fig. 5), which can clearly be seen in the  $J = 10$  simulation, though  
 324 to a weaker extent. Therefore, the error compensation ranks the LB results with a scale  
 325 jump from about 50 km to 2.4 km at the boundaries wrongly best on average.

**Figure 5.** Simulated precipitation sum by the LB simulations (orographic domain: left orange box, inflow domain: right orange box) using different driving simulations (indicated by precipitation sums surrounding the LB domains). The top row shows the results in the BB and in the CB with  $J = 2$  simulations (both with deep convection parameterisation switched off). The panels in the second and third row show LB results with increasing resolution jumps (deep convection parameterisation switched on). The LBC update frequency was hourly ( $U = 24/\text{day}$ ).

**Figure 6.** Meridional mean of the ratio of temporal sums of precipitation  $sumr$  as simulated with the LBs driven by BB and CB simulations using different  $Us$  (rows). The left columns shows the results in the orographic, the right column in the inflow domain. The grey zones were not used in calculation of the mean evaluation statistics (Tab. 2 and Fig. 4).

**Figure 7.** Meridional mean of the ratio of temporal sums of precipitation  $sumr$  as simulated with the LBs driven by the CB simulation with  $J = 10$  and using  $U = 8/\text{day}$ . The left column shows the results in the orographic, the right column in the inflow domain. Two different LBC specification approaches were used: Davies relaxation (solid lines), Mesinger (dashed lines).

326            Given the shown nesting challenge, we tested, as in Leps et al. (2019) at coarser  
 327 nesting grid-scales, the Mesinger approach as an alternative to the Davies relaxation ap-  
 328 proach for LBC specification. As illustrated in Fig. 7, the LB simulations with Mesinger  
 329 LBCs tended to show less deep spin-up zones in the orographic domain, which fits to a  
 330 smaller boundary zone and thus better representation of the western hills. But, total pre-  
 331 cipitation underestimation in the evaluation domain was increased by 5–10% compared  
 332 to simulation with the relaxation approach. In the inflow domain the total precipitation  
 333 amount was generally even more underestimated ( $\approx 15\%$ ). This might be an indica-  
 334 tion of smaller disturbances near the domain boundaries which later triggered convec-  
 335 tion. Near the outflow boundary, the effects of driving and driven simulation inconsis-  
 336 tencies were simulated in a narrower zone with the Mesinger than with the Davies re-  
 337 laxation approach. Overall, the Mesinger approach performed comparable to the Davies  
 338 relaxation approach.

## 4 Summary and conclusions

This paper presented idealised CPM nesting experiments using a modified Big-Brother (BB) experiment design as used before for RCMs in Leps et al. (2019). The model applied, COSMO-CLM, was used in many real data simulations successfully at RCM and at CPM scales. The reference BB simulation used a convection-permitting grid-spacing of 2.4 km. Coarse-Brother (CB) simulations with reduced grid-spacing by factors  $J = 2$  to 20 showed the expected degradation of simulation quality in terms of precipitation sum and temporal variability in two sub-domains, the Little-Brother (LB) domains with and without idealised hills. The CB simulation with  $J = 2$  (i.e. grid-spacing 4.9 km) and with deep convection parameterisation switched off (CP = off) performed very well compared to the CB with  $J = 2$  and CP = on and compared to the coarser CB simulations. In the discussed idealised set-up, the  $J = 5$  simulation also performed better without deep CP.

The LB simulations nested into the BB and the  $J = 2$ , CP = off, simulations produced up to about 30 % less precipitation than the driving simulations with best results using hourly or 15-min update frequency of the LBCs. In the domain with hills, i.e. with orographic forcing, the LB nesting could not improve the driving CB simulations with  $J = 2$  or 5 and CP = on, but the driving simulations with  $J = 10$  and 20 and CP = on in domain average. All LB simulations showed a large spin-up zone with precipitation underestimation near the inflow boundaries. The hilly domain LB simulations driven by the coarsest CBs compensated spin-up underestimation by overestimation in the inner parts of the domain. The nested simulations in the flat domain, i.e. without internal orographic forcing, did not inherit convective disturbances from the driving CBs with  $J = 10$  and 20 at the inflow boundary. Their relatively good evaluation results were probably due to disturbances because of inconsistencies between driving and driven simulation at the inflow boundary.

These results lead to the conclusion that in our idealised set-up at best only the inner 50 % of the domain in main flow direction, i.e. the inner 200 grid points of 400 grid points in zonal direction, of the LB simulations provided useful information. In other words, a buffer zone of at least 100 grid-points depth along the lateral boundaries has to be accepted in CPM simulations. The results are slightly better for hourly or 15-min update frequencies than three-hourly. Six-hourly updates yielded the worst results systematically. Using the Davies relaxation or the Mesinger approach in preparing the LBCs had an only negligible impact on results.

In our set-up, the CB simulation with grid-spacing of 4.9 km, CP = off, performs better than all LB simulations. The forcing by the hilly terrain was seen well in the simulation and advected into the flat sub-domain. Following Panosetti et al. (2019) an even stronger forcing would further improve the relative performance. Additionally, this large-domain CB simulation is computationally about two times cheaper than the small domain LB simulations. Still, the LB simulations perform comparably better than here in real-world applications with stronger and/or additional forcings like surface heterogeneity and frontal systems (cf. Coppola et al. (2020)). But, it is recommended to use a driving model with grid-spacing scales not too deep in the grey zone of convection. Direct nesting into, for example, global ERA5 re-analysis data (Hersbach et al., 2020) and global HighResMIP (Haarsma et al., 2016) or regional CORDEX-CORE (Sorland et al., 2021) simulations with about 30 and 25 km grid-spacing, respectively, is sensible given the results shown here. Depending on the application, opting for a larger domain is better than for higher resolution of the CPM simulation. A 3-hourly or better lateral update frequency should be applied. Finally, better preconditioning of convective activity at the CPM domain's inflow boundary (like preconditioning of eddies in large-eddy simulations, Tabor and Baba-Ahmadi (2010)) might help to decrease the depth of the observed spin-up zone.

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COSMO-CLM is the community model of the regional climate modelling community, which is freely available for community members (<https://www.clm-community.eu>). Namelists for reproducing the simulations and the data used for evaluation is available online (<http://doi.org/10.5281/zenodo.4553188>).

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Figure 1.

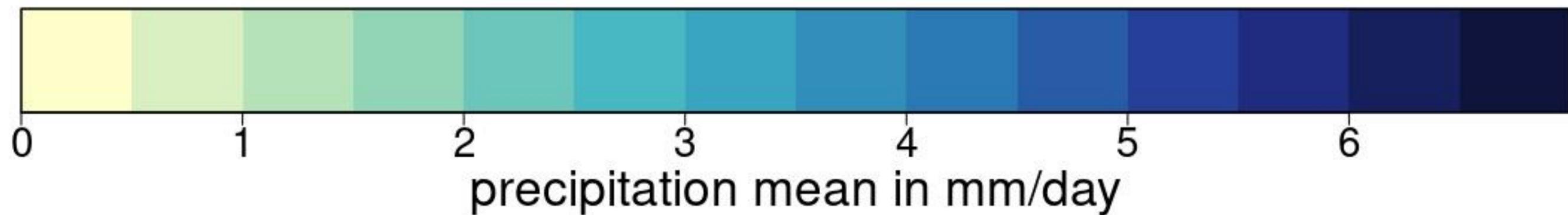
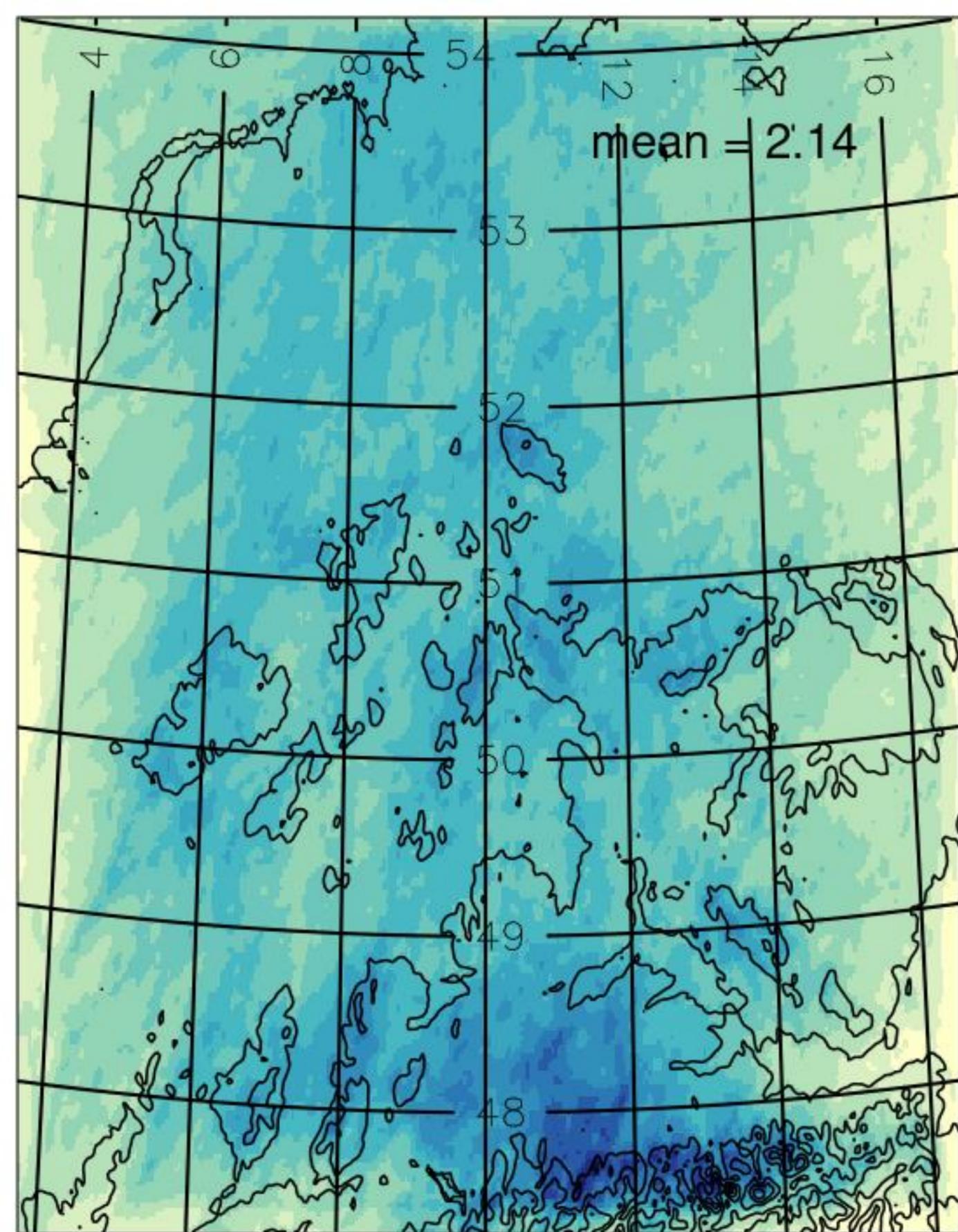
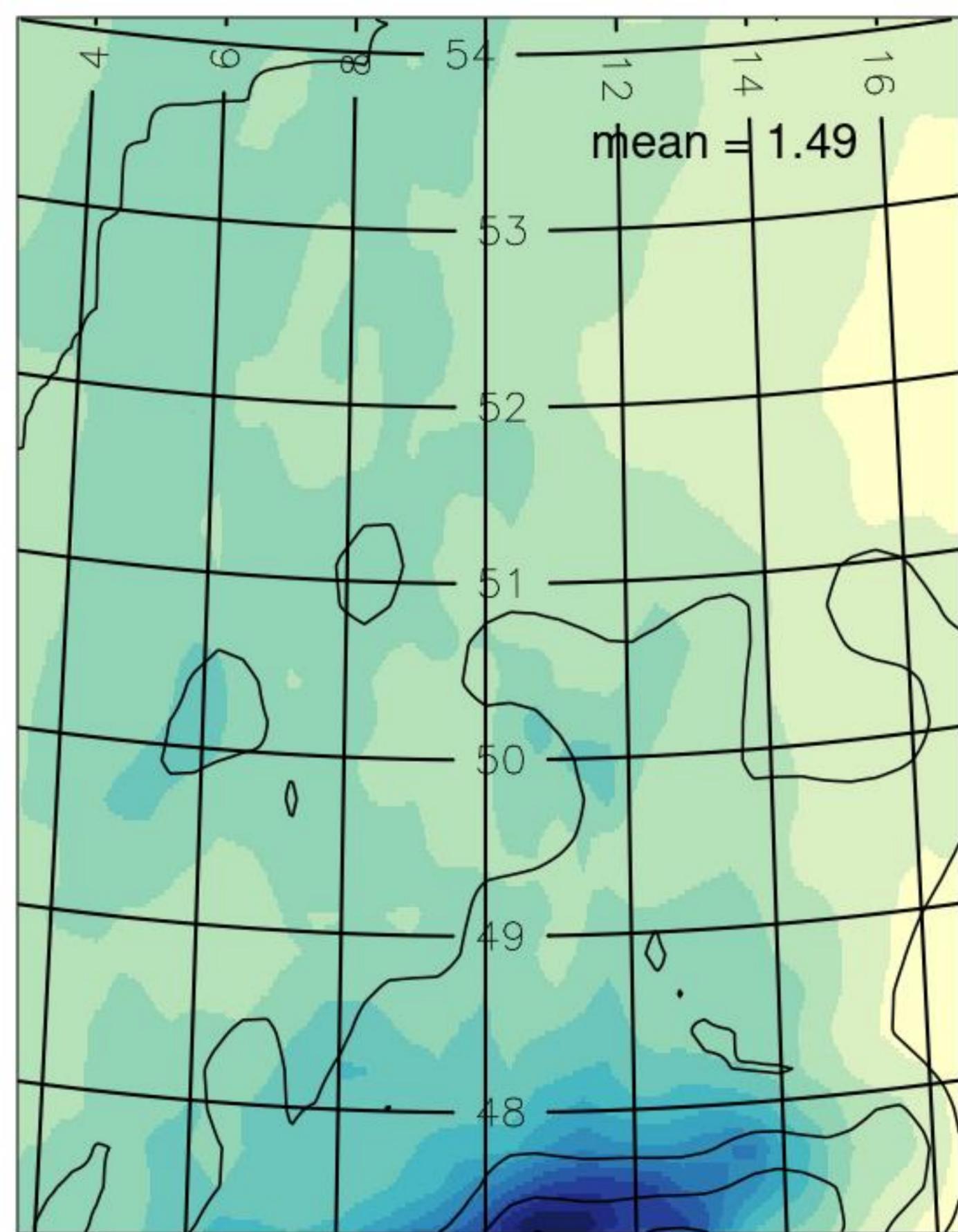


Figure 2.

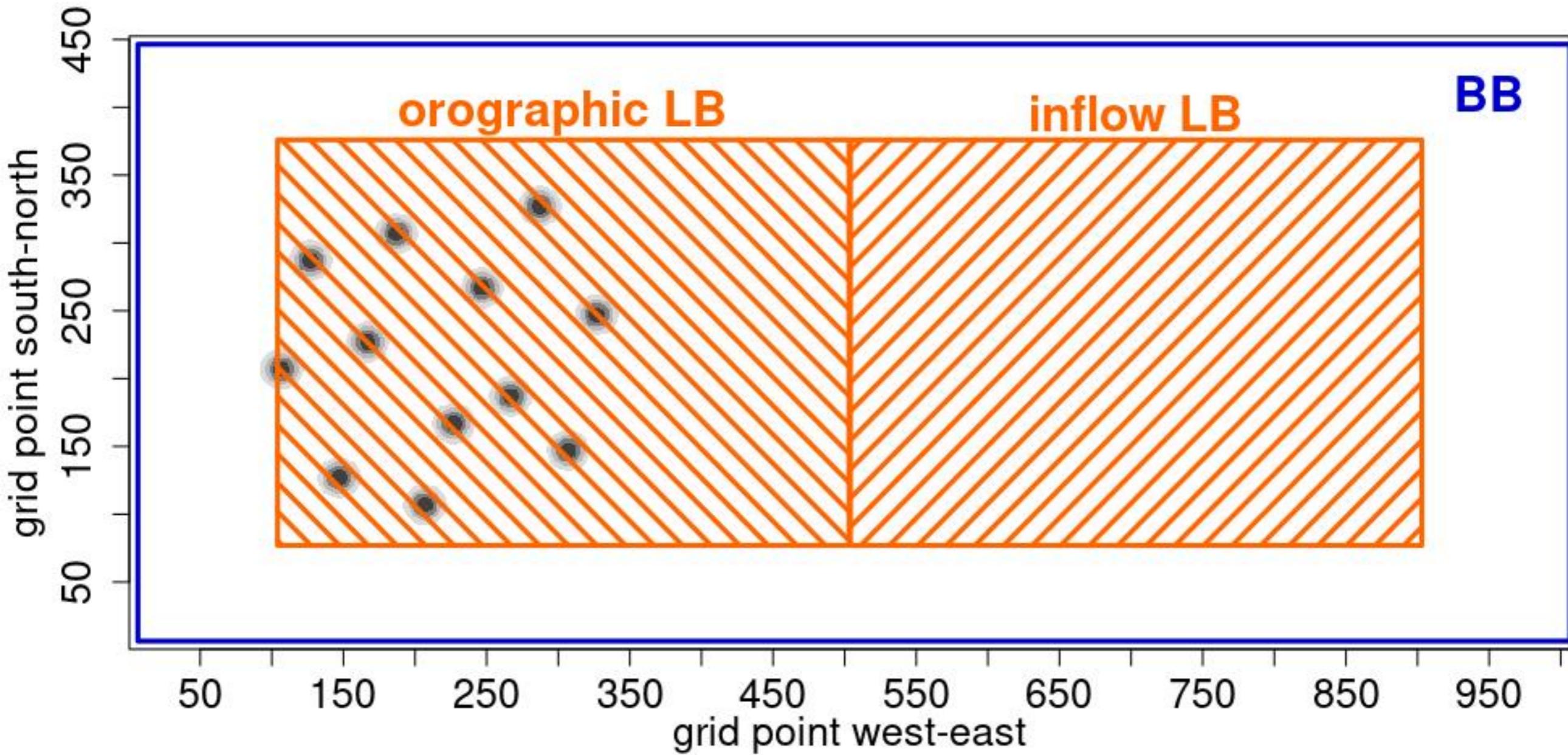
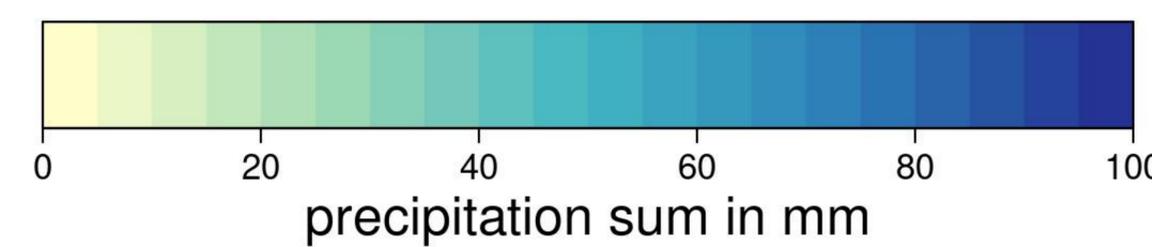
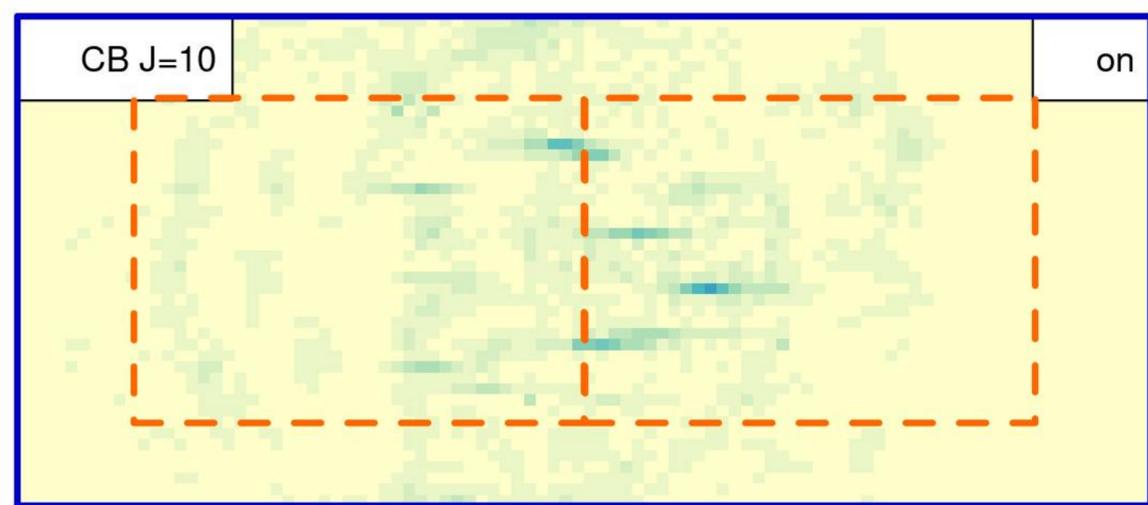
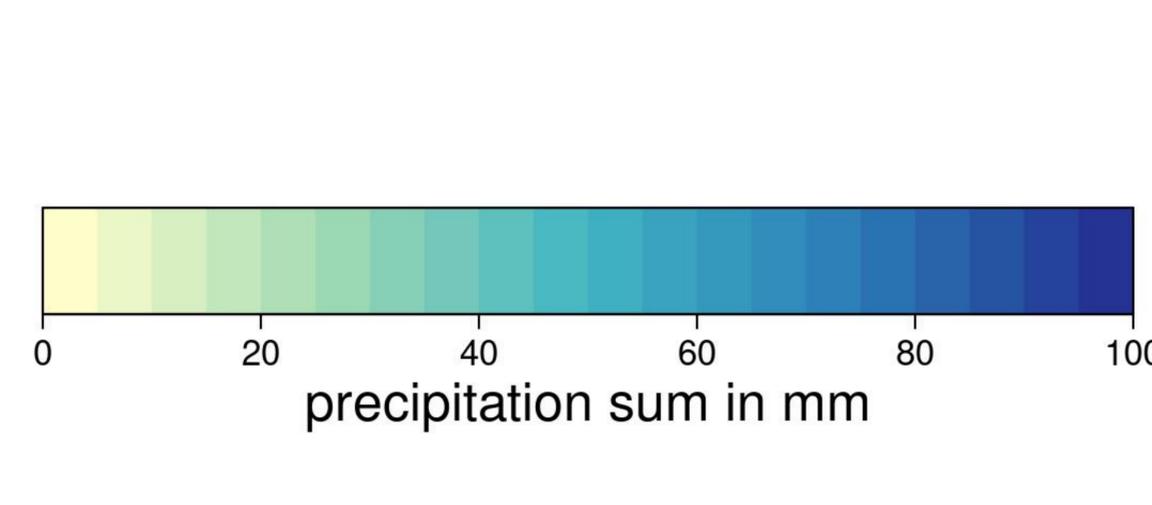
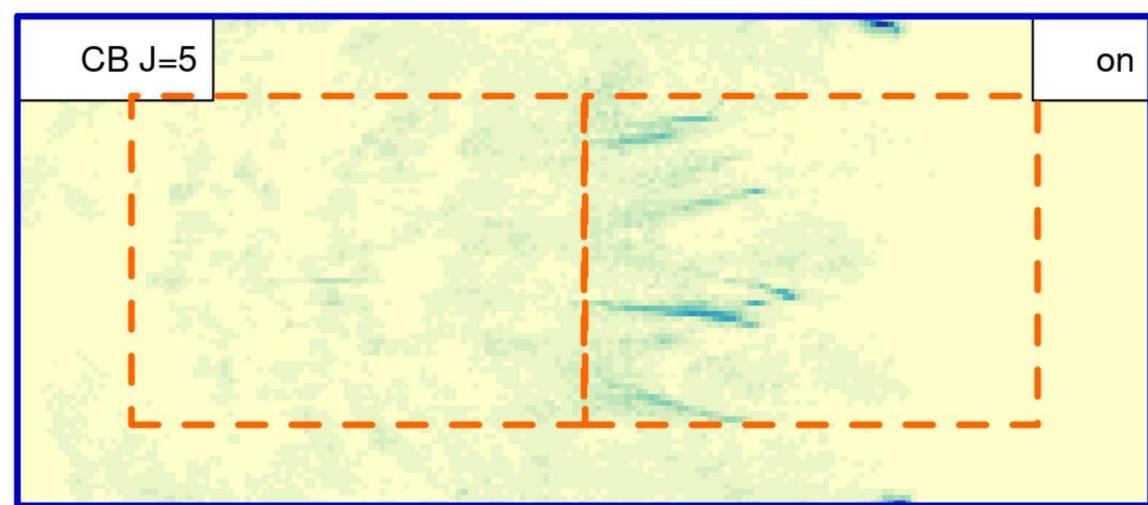
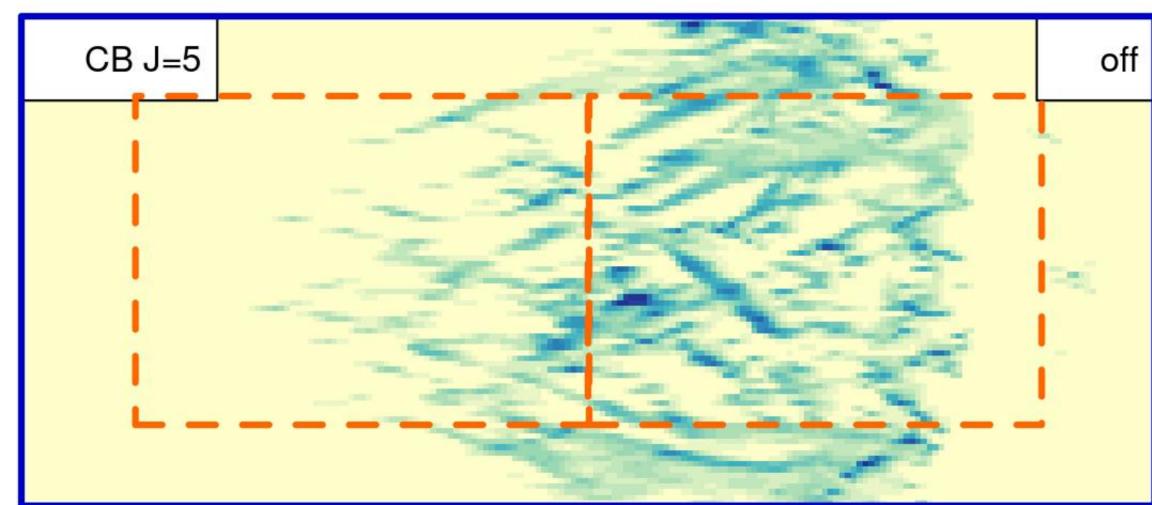
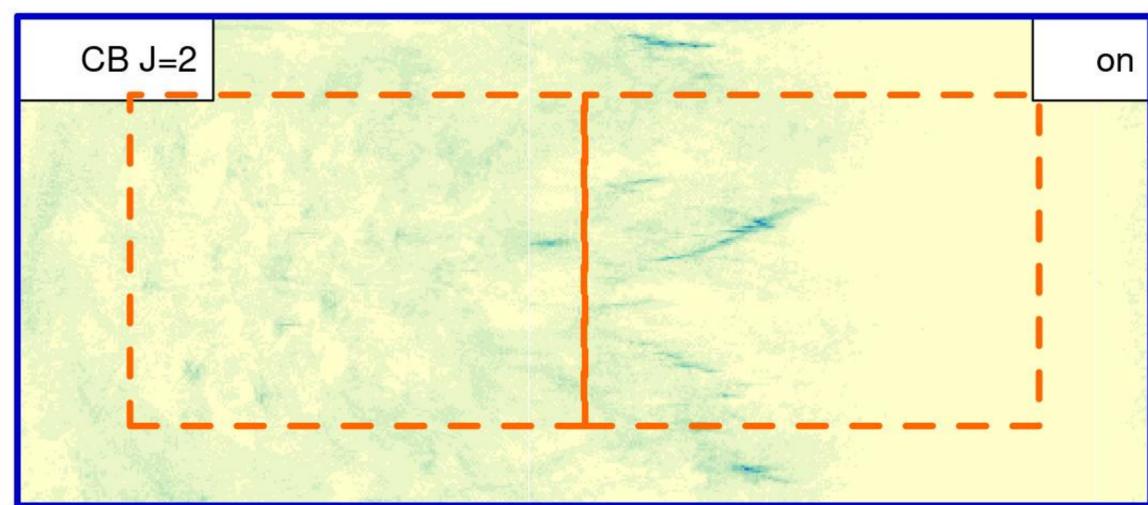
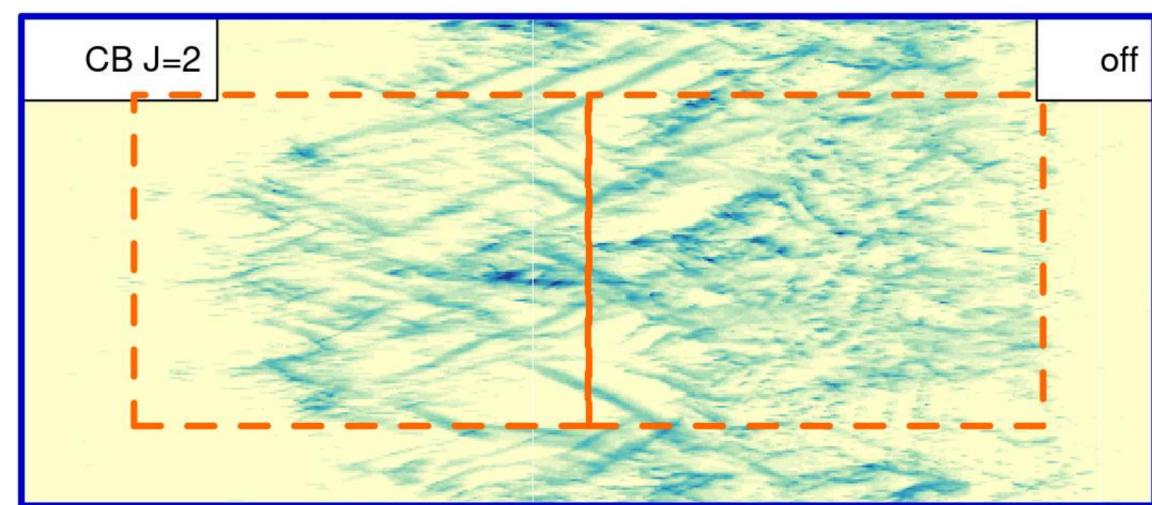
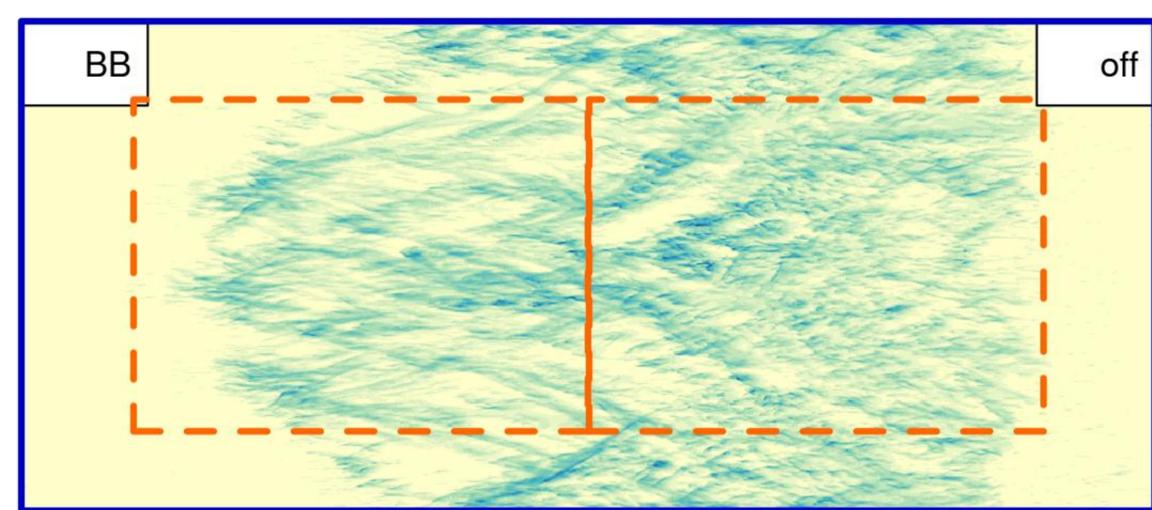
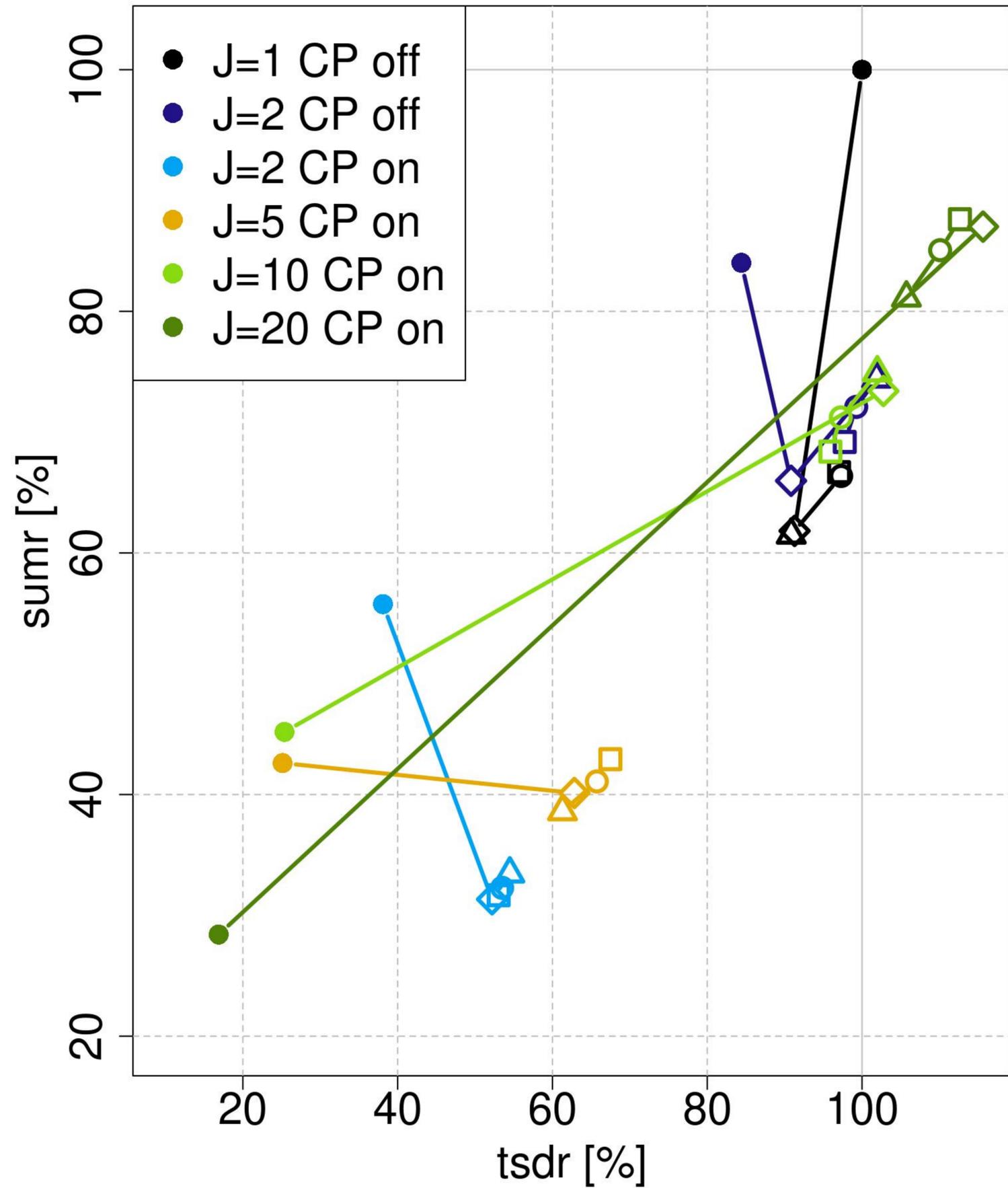


Figure 3.



**Figure 4.**

orographic LB domain



inflow LB domain

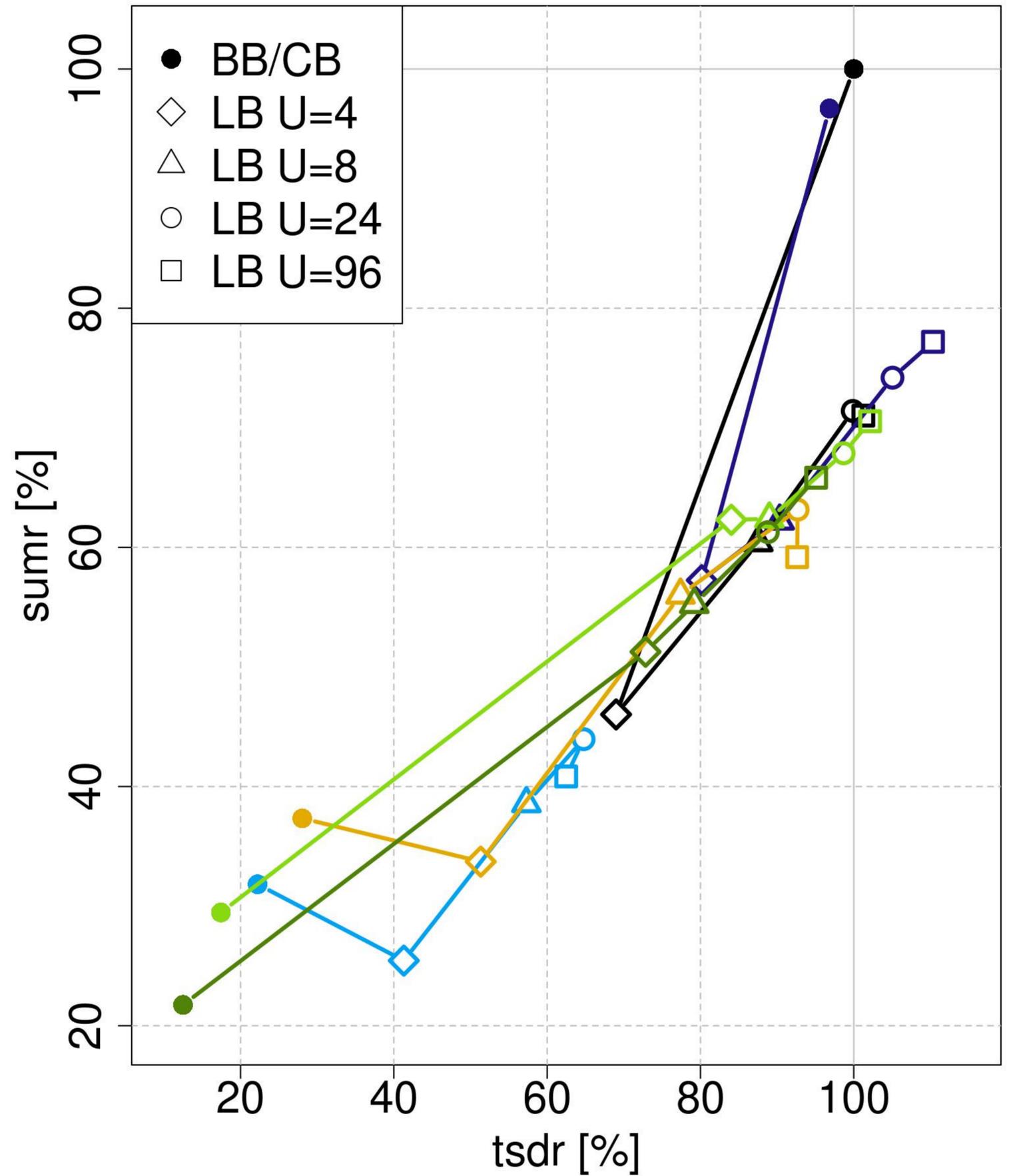


Figure 5.

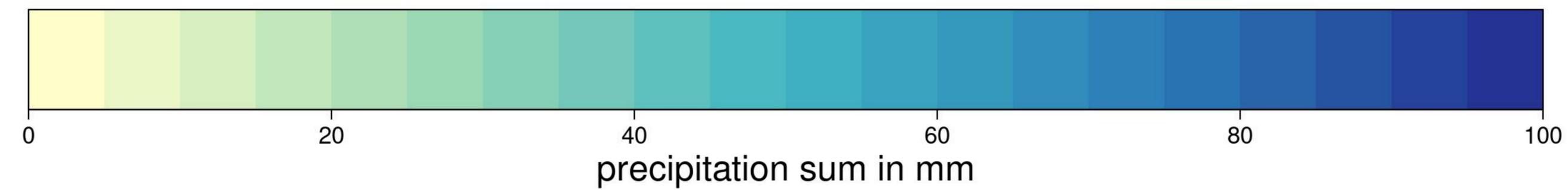
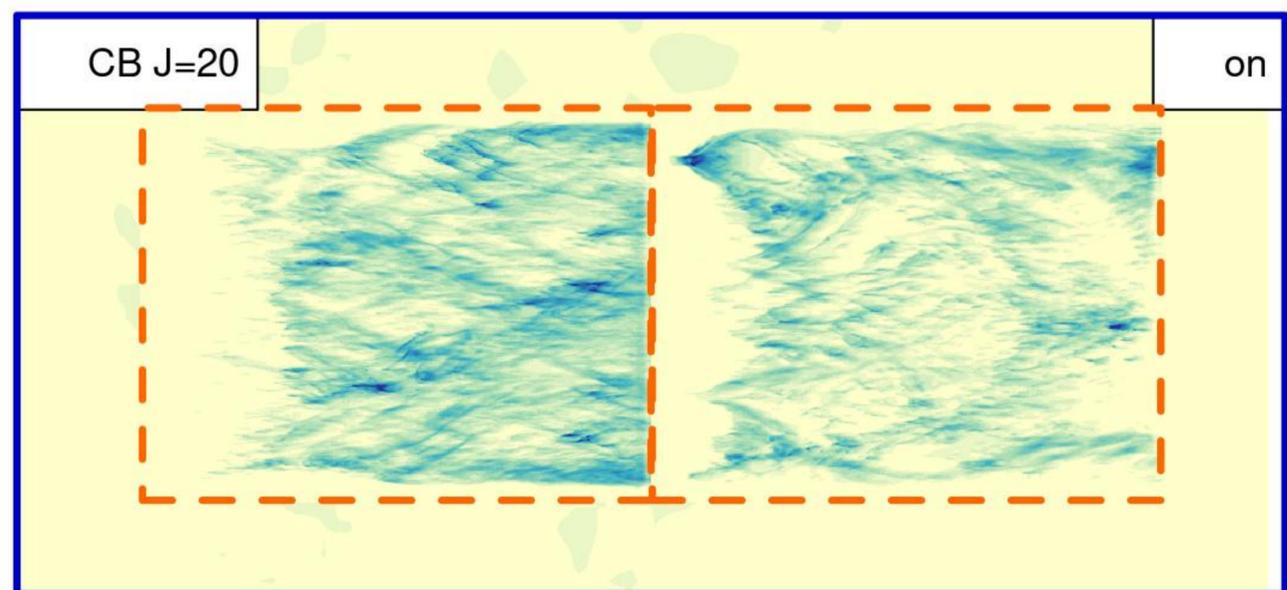
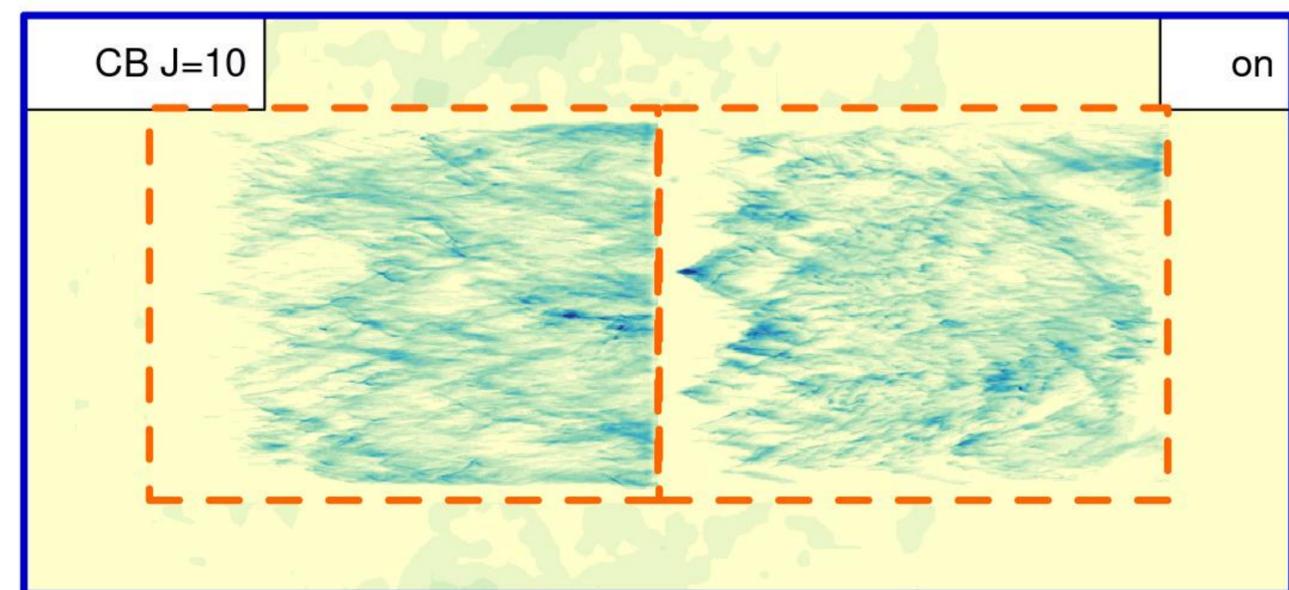
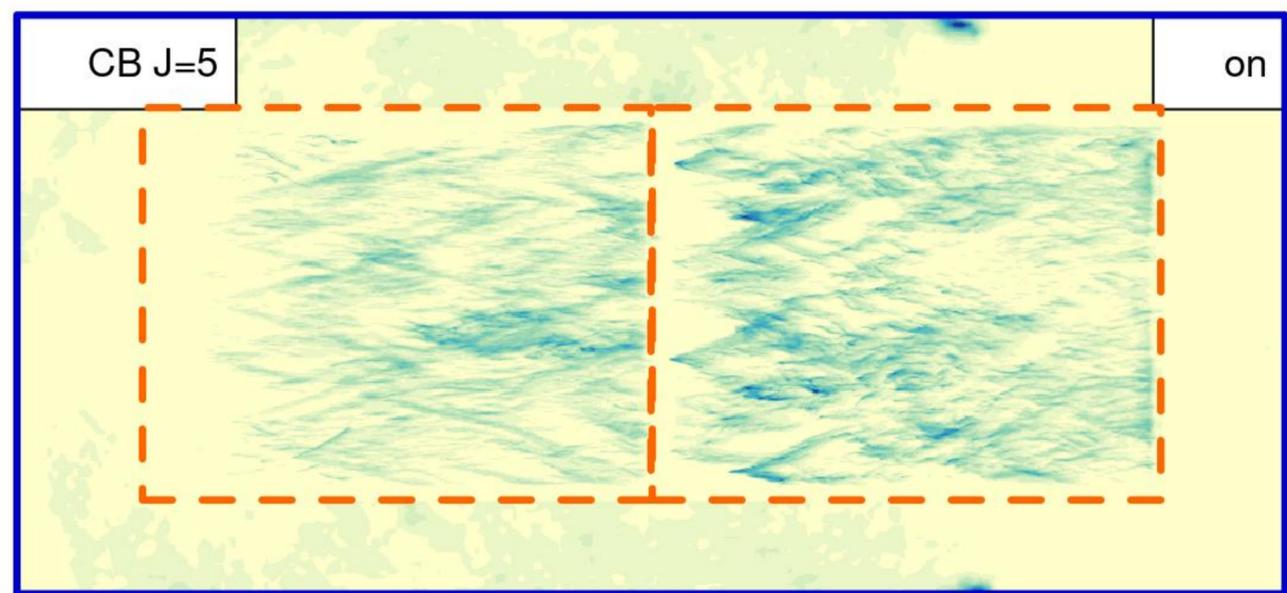
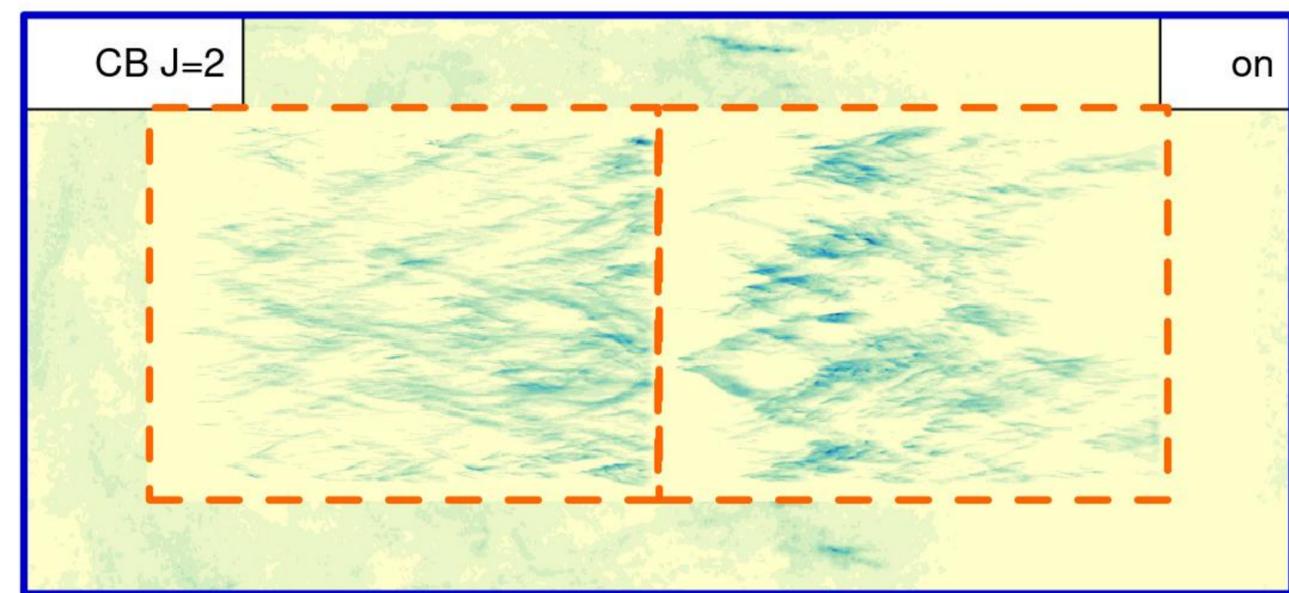
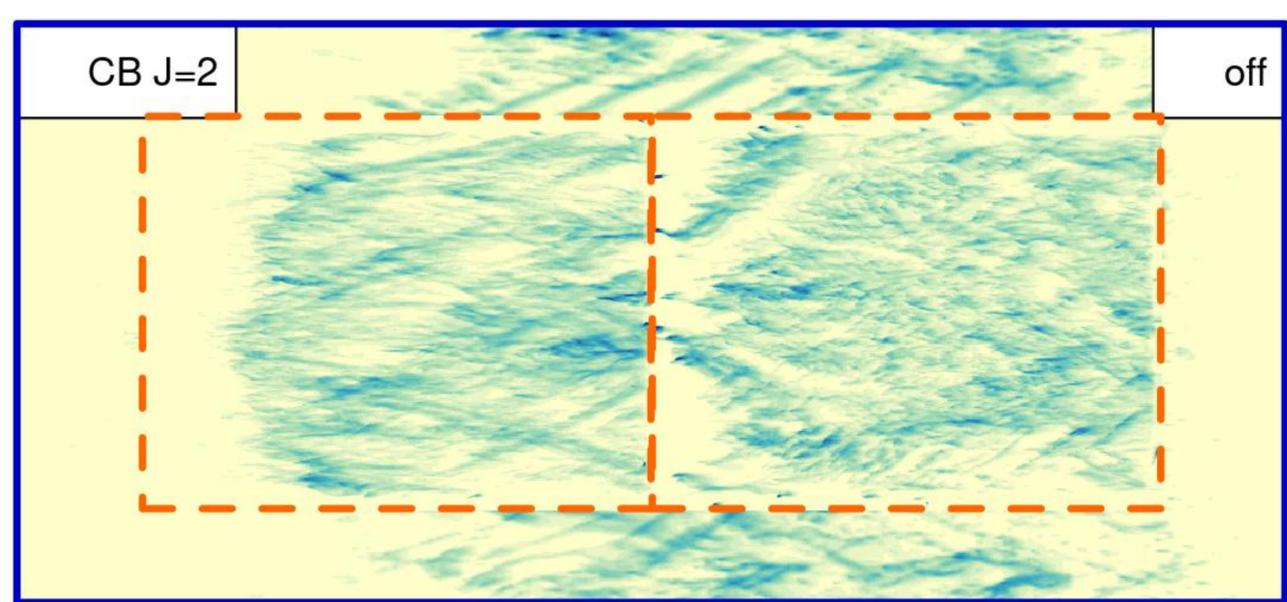
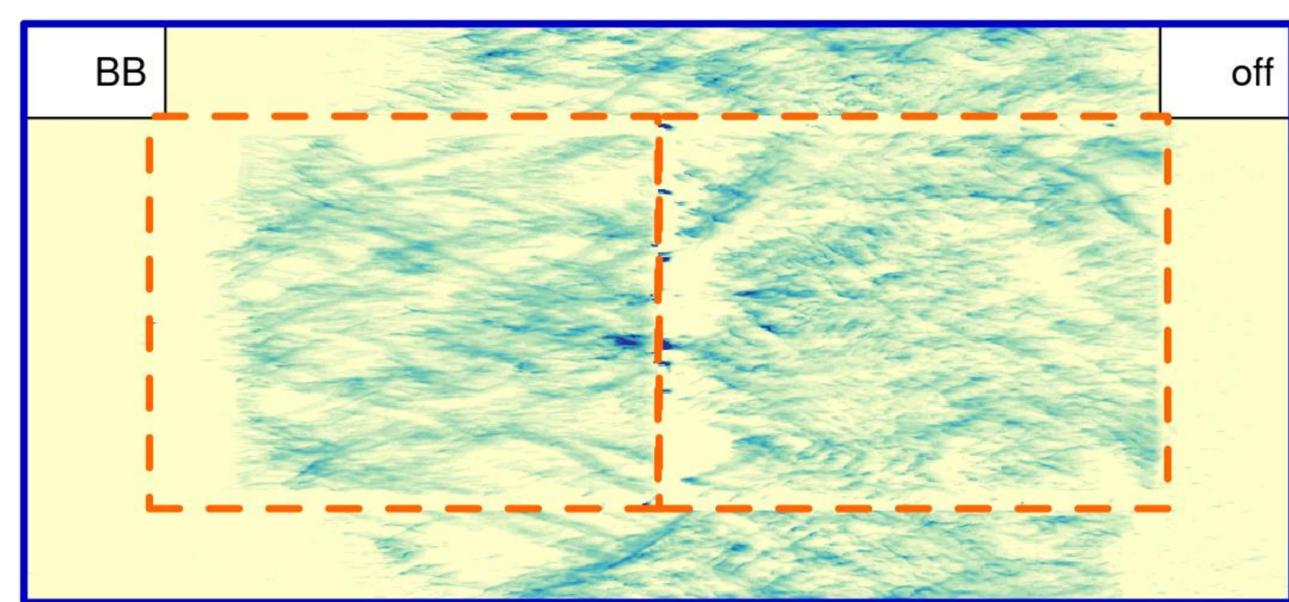
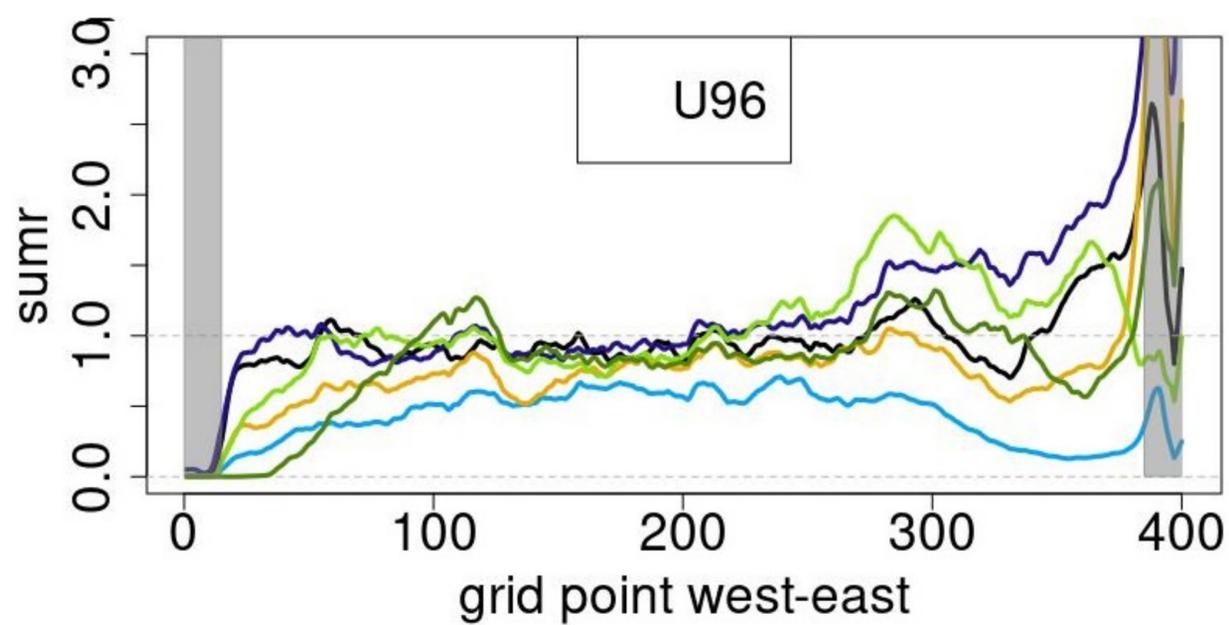
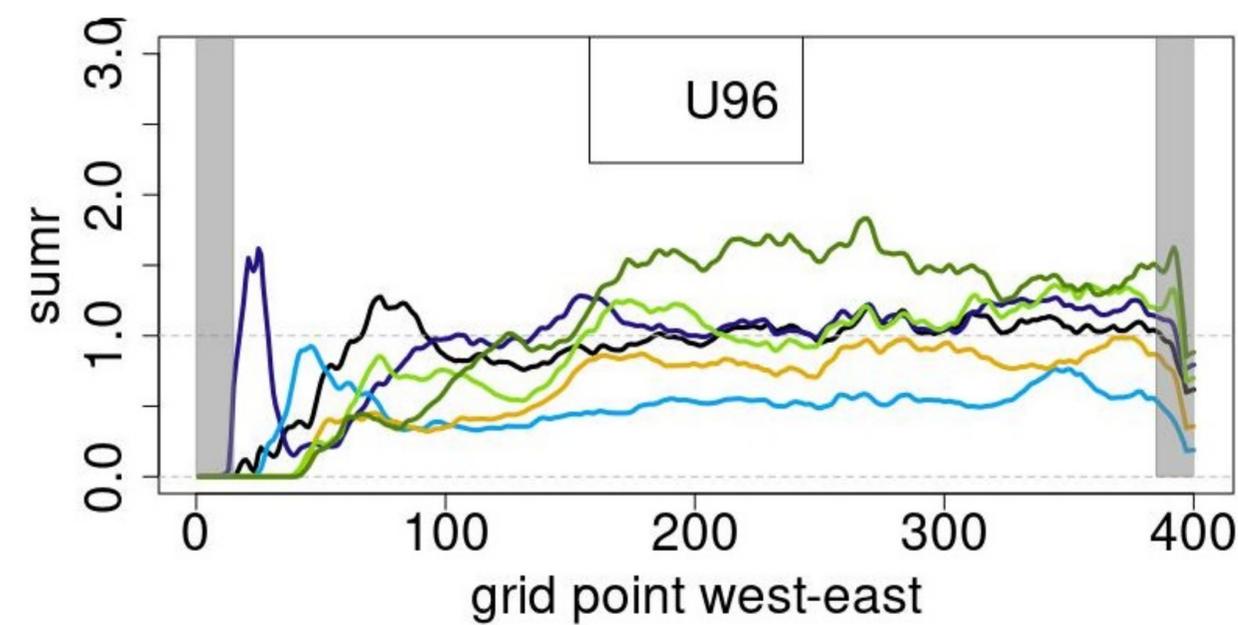
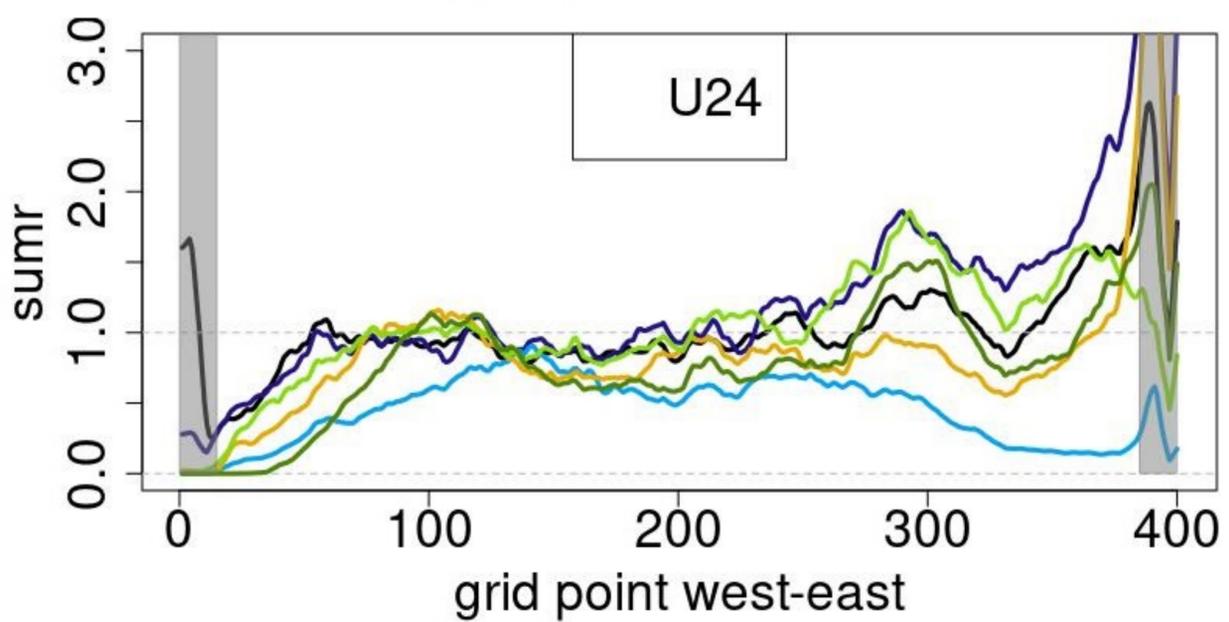
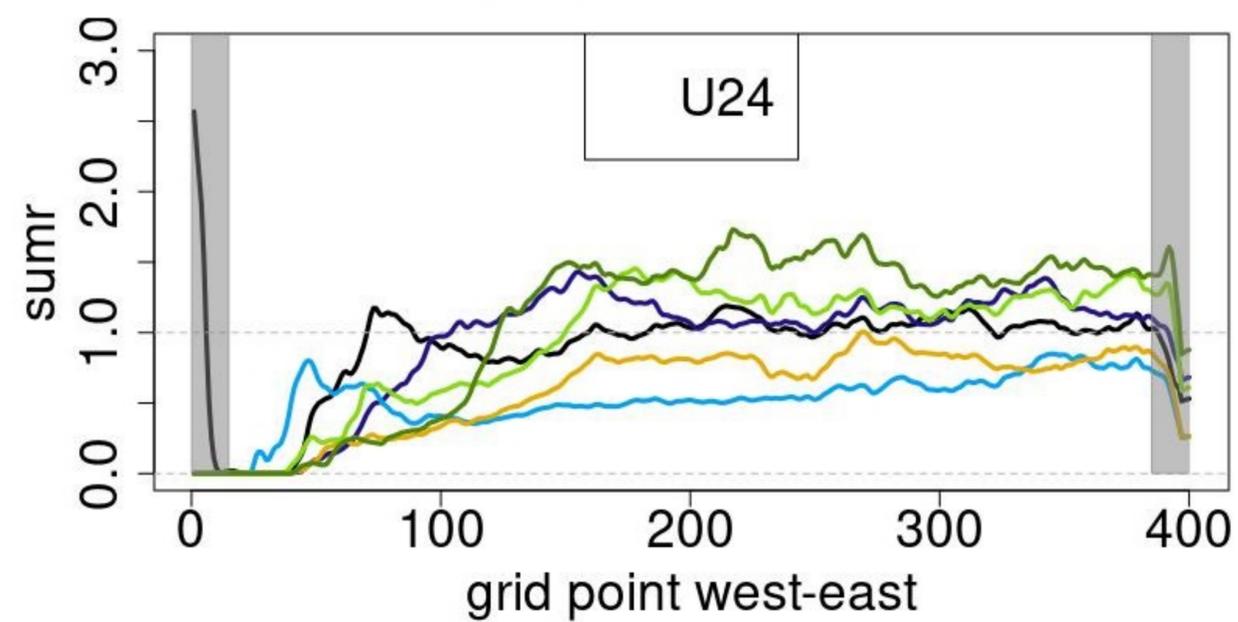
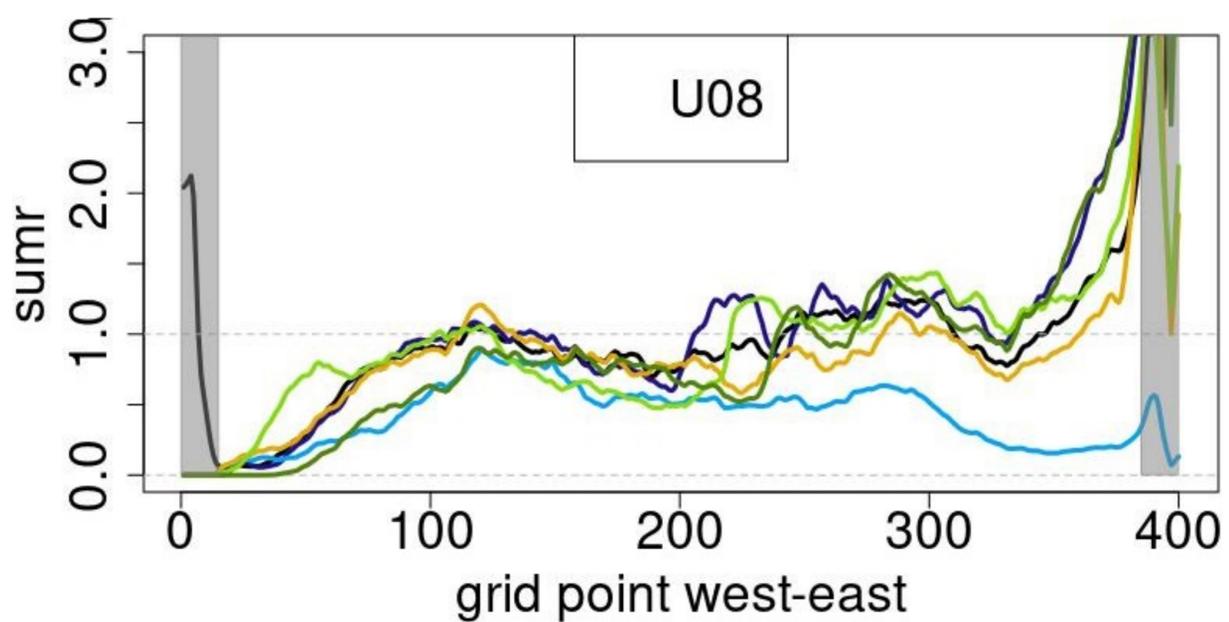
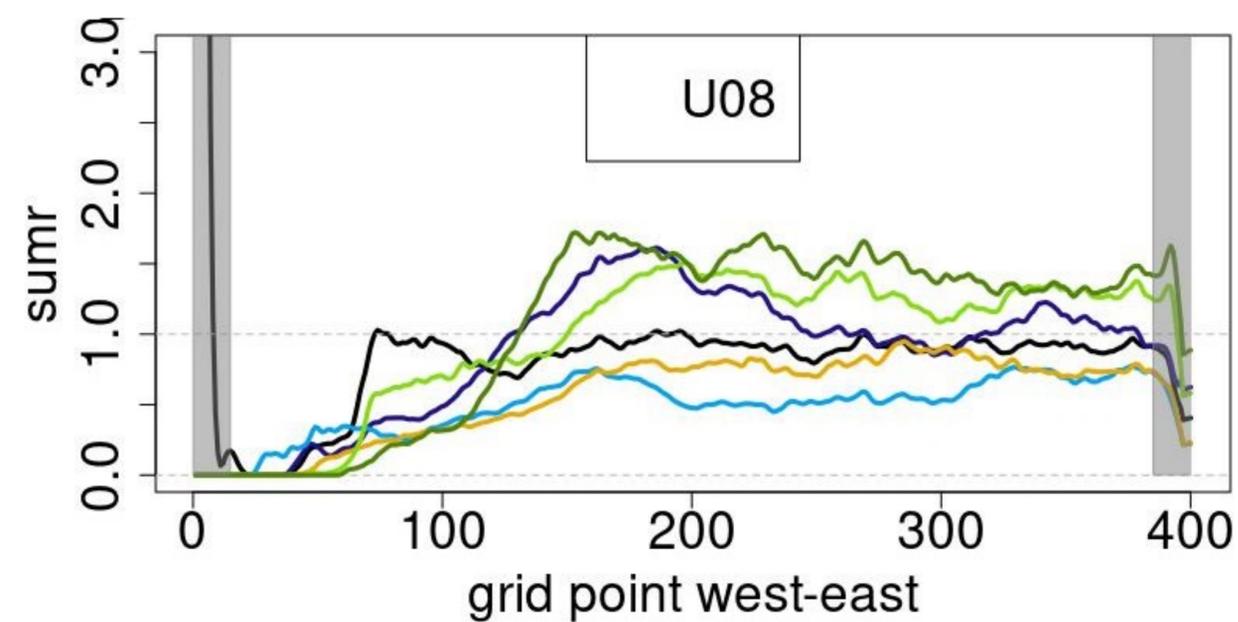
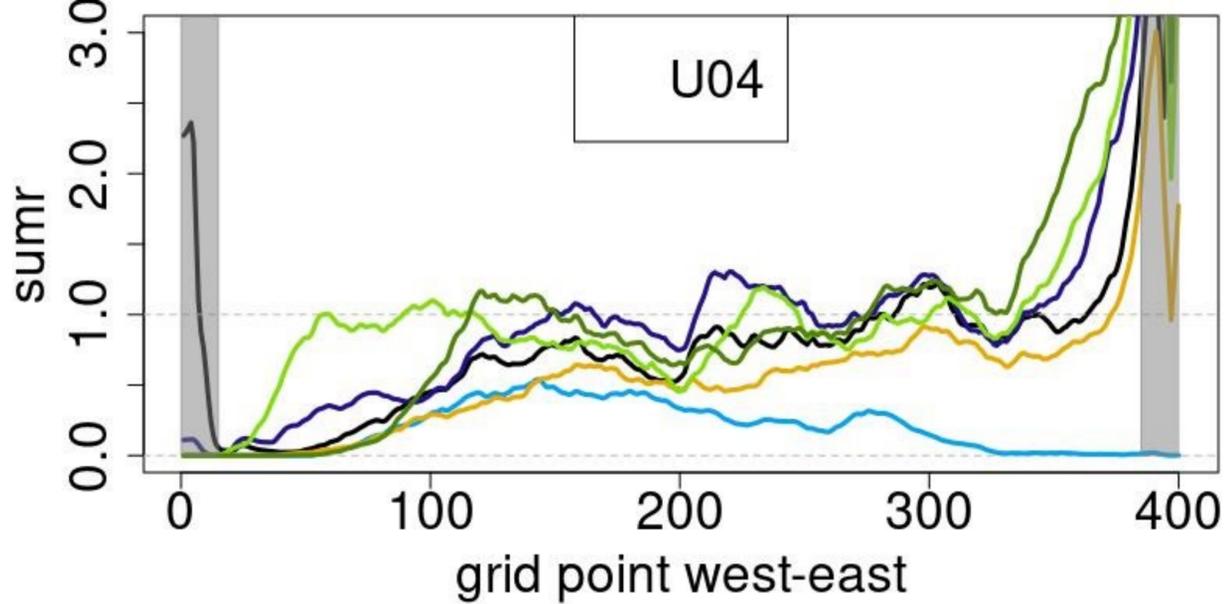
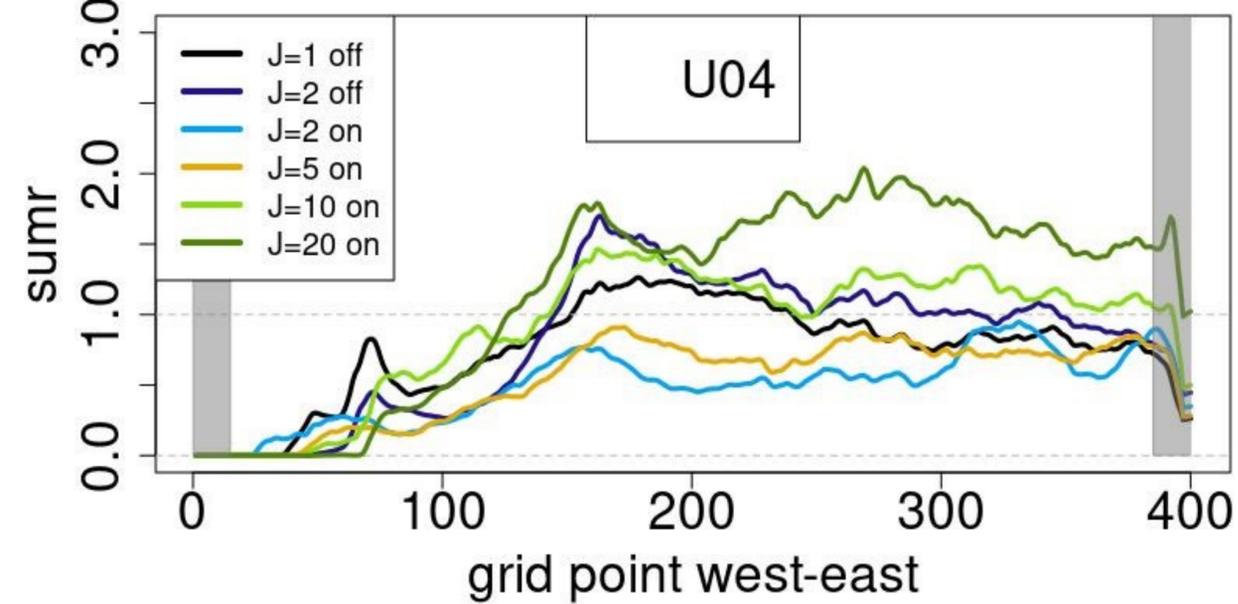


Figure 6.



**Figure 7.**

