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Dissecting Earth's Magnetosphere: 3D Energy Transport in a Simulation of a Real Storm Event

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Key Points:

- Simulation results are used to quantify the global energy dynamics of Earth's magnetosphere in terms of energy pathways.
- Externally during main phase 61 PJ of energy is lost from the closed region due to erosion while 92 PJ of energy enters the lobe region.
- Internally, 70PJ of energy is recirculated at the cusp from the closed to open field, then passed back to the closed region in the tail.

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Abstract

We present new analysis methods of 3D MHD output data from the Space Weather Modeling Framework during a simulated storm event. Earth’s magnetosphere is identified in the simulation domain and divided based on magnetic topology and the bounding magnetopause definition. Volume energy contents and surface energy fluxes are analyzed for each subregion to track the energy transport in the system as the driving solar wind conditions change. Two energy pathways are revealed, one external and one internal. The external pathway between the magnetosheath and magnetosphere has magnetic energy flux entering the lobes and escaping through the closed field region and is consistent with previous work and theory. The internal pathway, which has never been studied in this manner, reveals magnetically dominated energy recirculating between open and closed field lines. The energy enters the lobes across the dayside magnetospheric cusps and escapes the lobes through the nightside plasmashet boundary layer. This internal circulation directly controls the energy content in the lobes and the partitioning of the total energy between lobes and closed field line regions. Qualitative analysis of four-field junction neighborhoods indicate the internal circulation pathway is controlled via the reconnection X-line(s), and by extension, the IMF orientation. These results allow us to make clear and quantifiable arguments about the energy dynamics of Earth’s magnetosphere, and the role of the lobes as an expandable reservoir that cannot retain energy for long periods of time but can grow and shrink in energy content due to mismatch between incoming and outgoing energy flux.

Plain Language Summary

Results of computer simulation of near Earth space is looked at in a new way to understand how energy moves around the global system. It is found that in addition to a pathway of energy from the outside into the system and back again there is an internal loop which recirculates energy. These new methods will greatly improve our understanding how the whole magnetosphere system evolves and will help address evolution of processes that have space weather impacts.

1 Introduction

Energy that couples from the solar wind into Earth’s magnetosphere can have significant negative consequences on terrestrial life. Global dynamics of energy within Earth’s magnetosphere has long been a topic of interest since original works by Dungey (1961), who presented a clear combination of events involving dayside magnetic reconnection, advection of opened field lines and a re-closing of field lines at a tail reconnection site. Twenty years later, Akasofu (1981) presented a quantified picture of energy balance within the magnetosphere. In this work it was hypothesized and evidence was found for a system in which energy input from the solar wind was fully consumed by a combination of the enhancing ring current, Joule heating in the ionosphere, and precipitating auroral flux. Notably any plasma or magnetic energy contained in the open flux lobes was omitted, which would seem to suggest that the tail reconnection process would not significantly impact the energy balance, because that energy flows through the lobes without being stored there. We now have simulation tools to take a new look at this energy balance hypothesis and dig deeper into the energy transfer between sources and their specific timings.

In the following decade the International Solar-Terrestrial Physics program released the first Inter-Agency Consultative Group campaign with an objective to define “the structure and energy flow through the boundary layers of the Earth’s magnetosphere” (Mish et al., 1995). Many publications and valuable data sets resulted from this program, but as of yet there has not been a comprehensive quantitative resolution of this objective. This is because it is difficult to extrapolate observed pointwise boundary crossings to de-

63 termine the full surface geometry, and field values on the geometry to obtain integrated
 64 energy flux. It remains an open question how exactly energy circulates through the various
 65 boundaries in the magnetosphere system.

66 Global energy dynamics in the magnetosphere have been studied using simulation
 67 as far as the magnetopause boundary. Palmroth et al. (2003) and Pulkkinen (2007) showed
 68 the dependence of clock angle on the amount of energy and energy content through the
 69 magnetopause. Hoilijoki et al. (2014), Lu et al. (2021), H. Zhang et al. (2023) have also
 70 shown that the type of energy entering the system varies significantly with the radial com-
 71 ponent of the interplanetary magnetic field (IMF) and the dipole tilt. Brenner et al. (2021)
 72 took this a step further showing the energy flux through a full magnetopause surface in-
 73 cluding a bounding tail cutoff and a forward surface. By using the magnetic field rather
 74 than the flow field to construct the magnetopause surface, it was shown that the effect
 75 of magnetic reconnection on the dayside results in energy outflow in the form of hydro-
 76 dynamic flux at $X_{GSM} > 0$ and Poynting flux inflow at $X_{GSM} < 0$. These dynamics
 77 were also seen in a study by Ala-Lahti et al. (2022) using a 2D version of the Vlasiator
 78 code (Palmroth et al., 2018). This is in contrast with previous studies by Lu et al. and
 79 H. Zhang et al. who conclude that hydrodynamic flux (there referred to as mechanical
 80 energy flux) is entering the system near the magnetopause nose. The difference arises
 81 from their choice of the magnetopause boundary definition. We argue that the magne-
 82 topause definition outlined in this paper is the best choice when considering the energy
 83 circulation between the solar wind and the magnetosphere and within the magnetosphere
 84 – ionosphere system.

85 The internal workings of the magnetosphere, namely the energy transport within
 86 the system, has not been studied in detail using global simulation explicitly. However,
 87 there have been many important works which provide insight into how the system is ex-
 88 pected to behave. Many studies have shown that the IMF clock angle has direct con-
 89 trol of how the magnetosphere opens and allows solar wind plasma to enter the system.
 90 Specifically, studies using observations from the Cluster mission have shown how the mag-
 91 netic cusp responds to a change in the reconnection line position causing a reversal of
 92 the reconnection outflow relative to the open-closed field line boundary (Escoubet et al.,
 93 1989; Lavraud et al., 2005) (see also recent review of magnetospheric cusp findings from
 94 the Cluster mission by Pitout et al. (2021)). When the IMF is northward and high lat-
 95 itude reconnection occurs, the energy transport is not captured in the coupling functions
 96 such as the Newell et al. (2007) function, while it is thought to be one possible mech-
 97 anism for energy influx. Specifically this may result in energy influx when both north
 98 and south lobes reconnect simultaenously, known as dual lobe reconnection (Russell, 1972).
 99 Milan et al. (2020) summarizes the various possibilities of reconnection between the sheath
 100 and open-closed field lines, and shows evidence for dual lobe reconnection signatures in
 101 the ionosphere. Finally, Glocer et al. (2020) show simulation results on how the mag-
 102 netosphere may be largely populated by ions coming from polar wind outflow rather than
 103 from the solar wind, highlighting the significant role the inner boundary must also play
 104 in the energy transport. Although we do not employ a two-way coupled polar wind out-
 105 flow model in this study, the effective mass transport out of the system due to the fixed
 106 density inner boundary condition mimics real outflow effects (Welling & Liemohn, 2014).

107 In this work, we use results from a coupled global space environment simulation
 108 to address the following questions:

- 109 1. What is the energy balance in the magnetosphere during a real storm event? What
 110 determines the energy split between open and closed field line regions and what
 111 conditions internally and externally cause it to change?
- 112 2. What is the energy pathway between the magnetosphere and surrounding (shocked)
 113 solar wind plasma? In contrast, what are the energy pathways internal to the mag-

114 netosphere? How do each of these respond to variations in the external solar wind
 115 and IMF conditions and internal system state?

116 2 Space Weather Modeling Framework (SWMF)

117 In this work, we use the Space Weather Modeling Framework (SWMF) in the Geospace
 118 configuration (Toth et al., 2012). This configuration includes the BATS-R-US in ideal
 119 MHD mode for the Global Magnetosphere, Ridley Ionosphere Model (RIM) for Ionosphere
 120 Electrodynamics, and the Rice Convection Model for the Inner Magnetosphere. The MHD
 121 domain was configured with $1/2 R_E$ grid resolution inside a paraboloid aligned with the
 122 X_{gsm} direction with height of $52 R_E$ and a radius of $35 R_E$ at the base ranging from $+20$
 123 to $-32 R_E$ to capture the extent of the magnetopause. Additionally, within a box $-20 <$
 124 $X < 8$ and $-8 < Y, Z < 8$ and in X the resolution was increased to $1/4 R_E$. Finally
 125 in a spherical shell from the inner boundary of $2.5 R_E$ out to $8 R_E$ the resolution was
 126 increased again to $1/8 R_E$ (see Figure 1). The ionosphere model included the Conduc-
 127 tance Model for Extreme Events (CMEE) (Mukhopadhyay et al., 2020).

128 3 Observations

129 The event selected for this study is the well-known Starlink event in which 38 com-
 130 mercial satellites launched as part of the Starlink constellation were lost due to thermo-
 131 spheric upwelling (Zhang et al., 2022). It is a recent event, which allows us to take ad-
 132 vantage of the growing number of Earth-orbiting space missions. Figure 2 shows com-
 133 parisons of observed and simulated geomagnetic indices, demonstrating the suitability
 134 of the simulation for capturing the global scale physics.

135 The ground-based observations can be used for comparison with the simulation re-
 136 sults. The third panel of Figure 2 shows the Sym-H index constructed from a series of
 137 mid to low latitude magnetometer station recordings, typically responding to the vari-
 138 ations in the ring current encircling the Earth within the inner magnetosphere. While
 139 the magnitude is somewhat off especially during the recovery phase of the storm, the over-
 140 all temporal evolution is well captured by the simulation. We define the storm main phase
 141 as the rapidly decreasing Sym-H period, ending at the peak value of the observed Sym-
 142 H.

143 The Supermag SML index (Gjerloev, 2012) (bottom panel of Figure 2) is constructed
 144 using high-latitude magnetometer records responding mostly to ionospheric currents and
 145 auroral activity. To make a 1-1 comparison to the SML index, we seed virtual magne-
 146 tometers for each point in the Supermag network in the simulation domain and compute
 147 the northward component of dB . The minimum dB_n value from the high latitude sub-
 148 set of stations is taken as the simulated SML index value. Consistent with recent work
 149 by Shidi et al. (2022), who showed that SWMF has a lower average Heidke Skill Score
 150 for high latitude magnetic disturbance predictions, the simulation does not capture the
 151 very high auroral currents that were observed during the main phase of the storm.

152 We use the Cluster-1, Magnetospheric Multiscale (MMS) 1, and Time History of
 153 Events and Macroscale Interactions during Substorms (THEMIS) A, D, and E space-
 154 craft to compare in-situ plasma and magnetic field measurements with the simulation
 155 results. The orbits are shown in Figure 3 with contours of the virtual status variable which
 156 represents the topological region of the magnetosphere within which the virtual satel-
 157 lite was in at that time. As evident in the plots, the orbits include magnetopause bound-
 158 ary crossings as well as crossings between open and closed field lines, which allow us to
 159 compare the observed crossings with the simulation boundary locations.

160 Figure 4a shows the comparison of the z component of the magnetic field at the
 161 locations of the THEMIS, Cluster, and MMS spacecraft. In the magnetosphere, the B_z

162 component is a good proxy for the magnetic energy density in the system, while also cap-
 163 turing the sign change associated with leaving the magnetosphere during southward IMF.
 164 On the same plot, on the right vertical axis, we plot the magnitude of the local Poynt-
 165 ing flux $|\mathbf{S}|$. This derived quantity is constructed from the local magnetic field strength
 166 and bulk velocity, as discussed in more detail below (see Equation 2). While the B_z is
 167 a useful proxy, the Poynting flux is a direct measure of the electromagnetic energy trans-
 168 port, and therefore a key quantity for the purpose of this paper. Similarly, Figure 4b shows
 169 the observed and simulated total pressure P on the left axis and the local magnitude of
 170 hydrodynamic flux $|\mathbf{H}|$ on the right axis (see Equation 1 and discussion below).

171 Overall the differences in the magnitude of the state variables (B_z, P) as well as the
 172 derived flux magnitudes ($|\mathbf{S}|, |\mathbf{H}|$) are similar. The data – model comparison results are
 173 discussed further in Section 5.4.

174 4 Methods

175 4.1 Region Identification

176 In order to analyze the energy transport within the 3D MHD output domain, the
 177 energy density must be integrated over a volume and energy flux through a surface. While
 178 the choice of the volume(s) and surface(s) can be arbitrary, we select definitions that dis-
 179 tinguish physically significant boundaries that separate plasmas with different proper-
 180 ties, while keeping the analysis concise with objects that are clearly defined and limited
 181 in number.

182 Building on previous work by Brenner et al. (2021) we first define the magnetopause,
 183 which sets the boundaries of the magnetosphere. The magnetopause definition uses a
 184 combination of the field line tracing status variable for closed field lines with the mod-
 185 ified plasma-beta $\beta^* = 2\mu_0(P_{th} + P_{dyn})/B^2$, which was first introduced in a study of
 186 the Martian magnetosphere (Xu et al., 2016). The β^* limit chosen was 0.7, but the sharp
 187 gradients in this variable result in a very forgiving choice in the limit value close to unity.
 188 To account for cases when the solar wind β^* value dips below the limit value, we add
 189 the condition that solar wind field lines are explicitly omitted. (Note that this also omits
 190 plasma tailward of the distant X line, if it reaches within the X_{gsm} cutoff. This plasma
 191 tends to be high β^* and traveling away from the Earth.) The X_{gsm} cutoff is set at $X =$
 192 $-20R_e$, and the inner boundary (of the analysis, not the simulation domain) is set at
 193 $r = 4R_e$, close to where the MHD model is coupled to the ionospheric electrodynamic-
 194 ics model ($3R_e$). Below this altitude, there may be numerical boundary effects which make
 195 the analysis results less accurate and meaningful. This definition captures the spatial re-
 196 gion where the plasma is dominated by the planet’s magnetic field, and thus forms a strong
 197 definition for the magnetosphere.

198 Once the magnetosphere system volume is identified, further subclassification is done
 199 in order to track energy within the system. To keep the analysis limited and the bound-
 200 aries well defined, we make only two splits: The first is the open-closed field line bound-
 201 ary. This separates the open flux lobes from the closed field line region of the magne-
 202 tosphere. The plasma in the closed field line region experiences different physics than
 203 the open field line plasma: In the inner magnetosphere, the particle drifts separate ion
 204 and electron motions, which in the simulation is captured by coupling the MHD code
 205 with a drift kinetic code, the Rice Convection Model. The open closed boundary is eas-
 206 ily determined using the status variable, and, as discussed above, separates distinct plasma
 207 populations.

208 The second split is done based on day-night magnetic field mapping. Since, by def-
 209 inition, the entire magnetosphere system is magnetically connected to the inner bound-
 210 ary ionosphere, we can divide the volume to regions mapping to the dayside and night-
 211 side (with respect to the magnetic terminator plane), respectively, without loss of vol-

212 ume or creation of additional unclassified volumes. This division is simply implemented
 213 by assigning the magnetically mapped north and south footpoint coordinates to each point
 214 in the 3D GM domain. Using the x coordinate of the footpoint, we can separate the day-
 215 side magnetospheric cusp boundary from the nightside plasmashet boundary layer, that
 216 may exhibit different energy transport phenomena.

217 The two core quantities we examine are the energy density integrated over a vol-
 218 ume and the energy flux integrated over a surface. The volumes of interest are limited
 219 to the lobes and closed regions, as well as their sum, which makes up the total magne-
 220 tosphere. The surface flux analysis, however, is detailed to cover the integrated flux across
 221 each interface of the magnetospheric system. With these definitions, there are six dis-
 222 tinct regions that any point in the domain can belong to: I. outside magnetosphere, II.
 223 dayside lobes, III. nightside lobes, IV. dayside closed, V. nightside closed, VI. inside in-
 224 ner boundary (see Figure 5a). The interfaces between each of these 6 regions results in
 225 a number of integrated flux values, the most relevant of which are explored in this pa-
 226 per (see arrows and numbered boundaries in Figure 5a).

227 4.2 Energy Transport Integration

In discussing both the volumetric energy contents and surface energy fluxes, we eval-
 228 uate the hydrodynamic energy (and its flux) and the magnetic energy (and the Poynt-
 229 ing flux) separately; together they make up the total energy and flux quantities. The hy-
 230 drodynamic energy flux \mathbf{H} and Poynting flux \mathbf{S} can be written in the form

$$\mathbf{H} = \left(\frac{1}{2} \rho u^2 + \frac{\gamma}{\gamma - 1} P_{th} \right) \mathbf{u} \quad (1)$$

$$\mathbf{S} = \frac{B^2}{\mu_0} \mathbf{u} - \frac{\mathbf{B} \cdot \mathbf{u}}{\mu_0} \mathbf{B} \quad (2)$$

228 where ρ is mass density, \mathbf{u} is the MHD bulk velocity, P_{th} is plasma thermal pressure, \mathbf{B}
 229 is the magnetic field, and γ is the ratio of specific heats. Together, these sum to the to-
 230 tal energy flux $\mathbf{K} = \mathbf{H} + \mathbf{S}$.

Similarly, the total energy density U is split into hydrodynamic (U_{P0}) and mag-
 231 netic (U_B) components, which allows us to write the total energy flux and energy con-
 232 tent equations as

$$\mathbf{K} = \mathbf{H} + \mathbf{S} = \left(\frac{1}{2} \rho u^2 + \frac{\gamma}{\gamma - 1} P_{th} + \frac{B^2}{\mu_0} \right) \mathbf{u} - \frac{\mathbf{B} \cdot \mathbf{u}}{\mu_0} \mathbf{B} \quad (3)$$

$$U = U_{P0} + U_B = \left(\frac{1}{2} \rho u^2 + \frac{P_{th}}{\gamma - 1} \right) + \frac{B^2}{2\mu_0} \quad (4)$$

231 This split into hydrodynamic and magnetic energy components is included to allow in-
 232 vestigation of the physical mechanisms that may drive energy transport at the various
 233 boundaries. The goal of this methodology is to keep the analysis comprehensive while
 234 also clear and limited in scope.

Finally, it is important to track both the static and motional contributions of flux
 through a surface that can move between two timesteps. As defined in Brenner et al. (2021),
 we include the motional component of all energy flux values by tracking the volumes traded
 between the 6 regions between each pair of consecutive time steps. This flux contribu-
 tion from the moving surface can be approximated by

$$\int_{\mathcal{S}(t)} U \mathbf{q} \cdot d\mathcal{S} = \int_{d\mathcal{V}/dt} U d\mathcal{V} \approx \frac{1}{\delta t} \int_{\delta\mathcal{V}} U d\mathcal{V} \quad (5)$$

235 where \mathcal{S} indicates a 2D surface in 3D space moving with velocity \mathbf{q} , \mathcal{V} indicates the en-
 236 closed 3D volume and $\delta\mathcal{V}$ is the volume covered by the moving surface in time δt . For

237 example, if a small volume of the dayside magnetosphere was in the dayside closed re-
 238 gion at time t_0 and at time $t_1 = t_0 + \delta t$ is now outside the magnetosphere, the energy
 239 contained in that small volume is considered as an energy flux from the closed region to
 240 the magnetosheath over a time period of δt . This is illustrated in Figure 5b.

241 5 Results

242 5.1 Volumetric Energy

243 Figure 6 shows the total volume integrated energy in regions of the magnetosphere
 244 stacked so that the top line represents the full magnetosphere volume. The main phase
 245 of the storm shown in the grey shaded region clearly shows the total energy increase fol-
 246 lowed by a slower energy decay as the system recovers. Comparing this with the Sym-
 247 H index in Figure 2 shows how good a proxy it is for the total energy content in the mag-
 248 netosphere.

249 Figure 6 also shows how variable the energy partitioning is between the closed and
 250 open field regions: The volume energy rate of change indicated by the slope of the stack
 251 interface is much stronger than the rate of change of the total. In order to understand
 252 what's happening between the two regions we next examine the variation in the surface
 253 energy flux values.

254 5.2 Surface Flux

255 Figure 7 summarizes the energy flux across the external regional interfaces which
 256 includes both the instantaneous energy flux across the static interface as well as the en-
 257 ergy flux due to surface motion. The magnetopause surface is broken down into four sec-
 258 tions: interface 1 between the lobes and the magnetosheath, interface 5 between the closed
 259 region and sheath, interface 4 between the lobes and the exterior through the tail cut-
 260 off, and interface 6 between the closed region and the exterior through the tail cutoff.
 261 Likewise, the inner boundary is split into two sections: interface 3 toward the open field
 262 and interface 7 toward the closed field each at a fixed distance of $4R_e$ from the Earth's
 263 center (see surface definitions and reference vectors shown in Figure 5a).

264 The three panels of Figure 7 show the exchange of hydrodynamic energy, Poynt-
 265 ing flux, and total energy flux, respectively. The sign convention for the flux calculation
 266 is with the surface normal pointing away from the interior of the reference volume so that
 267 positive values indicate energy escaping the system. From the top panel we see that ki-
 268 netic and thermal energy is escaping via the closed region throughout main phase, fol-
 269 lowed by a shortlived reversal in the average that seems to follow the IMF B_z turning
 270 briefly northward then back southward.

271 The middle panel shows that Poynting flux through the lobe – sheath interface dom-
 272 inates the total, and that this energy is going into the magnetosphere. For the Poynt-
 273 ing flux, there are more contributors as well during the main phase as later during the
 274 recovery. Magnetic energy transport out from the inner boundary to the open flux tail
 275 lobes represents low density, cold plasma outflow from the strong dipole magnetic field.
 276 This energy inflow is countered by the magnetic energy transferred out from the system
 277 through the inner boundary surface toward the closed field region. These two flux con-
 278 tributions appear to be quite balanced, but the lobe inner boundary flux steadily increases
 279 then decreases, while the closed inner boundary flux seems to retain a constant rate through-
 280 out most of the main phase.

281 The bottom panel showing the total energy transfer depicts the sum of the above
 282 results with only the lobe magnetosheath number 1 interface changing sign between in-
 283 tegrated \mathbf{H} , \mathbf{S} , and \mathbf{K} . This can be explained by looking at the form of the equations
 284 and noting that in the motional case they cannot differ, and the static case all energy

285 is transported with the velocity except for the $(-\mathbf{B} \cdot \mathbf{u}) \mathbf{B} / \mu_0$ portion of the Poynting
 286 flux. This means that this transport along the magnetic field direction rather than the
 287 flow field direction is dominating the flux between the sheath and lobes.

288 Figure 8 summarizes the energy flux across the internal interfaces in the magne-
 289 tosphere system, the flux sign is now with respect to the closed region so that positive
 290 flux transfers energy from the closed regions to the open tail lobes. The top panel re-
 291 veals that there is very little hydrodynamic energy exchanged at the dayside cusp (in-
 292 tegrated H_{2a}) or tail plasmashet boundary layer (integrated H_{2b}) with a slight bias to
 293 energy moving through the cusp toward the lobes.

294 The middle panel shows very large integrated Poynting fluxes, especially during the
 295 main phase, with maximum magnitudes approaching double that of the external fluxes.
 296 The balance is also now reversed with the tail interface (integrated S_{2b}) dominating the
 297 sum at almost all times. The connection of the temporal evolution with the IMF clock
 298 angle is apparent as there is a clear drop in both internal integrated Poynting fluxes be-
 299 fore the end of the main phase. Especially, the cusp flux reverses sharply right at the end
 300 of main phase.

301 The total integrated energy flux for the internal interfaces is almost entirely in the
 302 form of Poynting flux, and is much larger in magnitude than the external energy fluxes.
 303 This indicates that magnetic energy is recirculating in the system via slow, cold, low den-
 304 sity plasma with high magnetic field strength embedded within it.

305 Table 1 compares the various spatially integrated surface flux values by integrat-
 306 ing the power contribution in time over the main phase interval to obtain a total energy
 307 exchange through each interface. The signs of the values are consistent with the spatially
 308 integrated flux timeseries plots. This tabular format highlights the large amount of en-
 309 ergy moving through the internal interfaces 2a (dayside closed field region to tail lobes)
 310 and 2b (night-side closed field region to tail lobes). To further demonstrate this inter-
 311 nal energy re-circulation, we add up the energy entering through 1 (tail lobes to magne-
 312 tosheath) and the energy returned through 2a (closed field region to the lobes) that
 313 amounts to 163 PJ, which is close to the energy transferred through boundary 2b from
 314 the lobes to the closed field region in the tail of 157 PJ. This suggests that a large por-
 315 tion of the energy acquired by the lobes from the magnetosheath is transmitted to the
 316 closed field region and sent right back to the lobes in a recirculating loop. Note that when
 317 performing integrations over both space and time for an 8 hour window such as this, even
 318 small biased errors in the surface flux can result in large changes in the total energy trans-
 319 ported. Care was taken to avoid spurious effects from the inner boundary, and relative
 320 magnitude values for the largest fluxes were unaffected by these changes.

321 5.3 Reconnection lines

322 Figure 9 examines the locations of potential reconnection sites in relation to the
 323 magnetopause field topology. The four field junction (Laitinen et al., 2007) represents
 324 the location where four magnetic topologies (closed-closed, open-closed, closed-open, open-
 325 open) are all adjacent to each other and indicates the possibility of magnetic reconec-
 326 tion. The figure shows the neighborhood of four field junction cells (green), in reference
 327 to the magnetopause color coded with the magnetic connectivity status variable from two
 328 different viewing angles.

329 The first panel shows the rapid evolution of the system starting from the moment
 330 of B_z reversal at the end of main phase and then progressing in 10-minute increments.
 331 The magnetospheric cusp is also indicated in this figure as the dayside mapped bound-
 332 ary between open and closed field. Considering that reconnection has to happen near
 333 the four field junction neighborhoods, the Figure demonstrates how the northward turn-
 334 ing IMF first splits the single dayside X line, then the split X-line advects and is replaced

335 by an additional split X-line that covers large sections of both the closed and open mag-
 336 netopause. From the color coding showing open and closed field it is clear that dual lobe
 337 reconnection is occurring, as the lighter color closed region quickly expands to cover most
 338 of the shown magnetopause surface. These snapshots are taken from an animated video
 339 (see supplementary material), which demonstrates the explosive nature of the changing
 340 reconnection pattern.

341 5.4 Data Model Comparison

342 The right axes of Figures 4a and 4b show the satellite trace comparison of the mag-
 343 nitude of Poynting and hydrodynamic energy flux $|\mathbf{S}|$ and $|\mathbf{H}|$. For the Cluster 4 satel-
 344 lite, the simulated and observed flux magnitudes match well, especially during the main
 345 phase. There is a noticeable discrepancy just after the main phase ends, when the ob-
 346 served hydrodynamic energy flux is much larger than the energy flux predicted by the
 347 simulation.

348 Observations of all three THEMIS probes show two intervals when the satellite is
 349 crossing through a magnetospheric boundary. The first between -16:30 hours and -14:00
 350 hours when probes A and E initially reside in the open tail lobes as both the closed field
 351 region and the magnetosheath pass over several times. Probe D, just a small distance
 352 away, spends its time mostly in the closed field region during this time. All three probes
 353 have similar trends between the observed and simulated flux values, with the observed
 354 Poynting flux having more variations and a higher average value. Probe D within the
 355 closed field region also shows much lower hydrodynamic energy flux than those predicted
 356 by the simulation.

357 The next interval of crossings occurs during the main phase (between -8 hours and
 358 0 hours). Both the closed field region to lobe boundary and the tail lobe to magnetosheath
 359 boundary pass over each of the THEMIS satellites between -4:00 hours and -2:30 hours.
 360 For these crossings, the observed energy flux magnitude split does not agree with the sim-
 361 ulation results: The simulated values predict too much hydrodynamic energy flux and
 362 too little Poynting flux. Looking into the detailed components, specifically the simula-
 363 tion B_z magnitude drops where the observed field does not. This indicates reconnection
 364 transporting flux away from the magnetopause boundary in the simulation that is not
 365 happening to the same degree in the observations.

366 Finally, the MMS1 probe is compared with the simulation data (the inter-spacecraft
 367 spacing is too close to be resolved by the simulation grid size, so only one probe is used
 368 as a point comparison). Between -12:30 hours and -11:00 hours, MMS1 is near the mag-
 369 netopause. Comparison with the simulation values shows a much better agreement in
 370 the Poynting flux than in the hydrodynamic flux. The observed hydrodynamic flux mag-
 371 nitude peaks at much higher values, and after this point maintains a constant difference
 372 to the simulated values. During the main phase between -3:00 hours and -1:00 hours,
 373 there are enhancements in the observed B_z that are entirely missed by the simulation.
 374 These transients may be caused by smaller-scale structures in the magnetosheath, or tran-
 375 sient perturbations either at the bow shock or at the magnetopause.

376 5.5 Interpretation

377 Taking the individual results together, we see an emerging picture of two distinct
 378 energy pathways and an apparent mode shift. Energy exchange through the magnetosphere's
 379 external boundaries follows the classic Dungey cycle, but instead of focusing only on mag-
 380 netic flux (as the Dungey cycle does), we consider the total energy circulation. Energy
 381 is lost from the dayside closed field region as it opens through dayside reconnection; this
 382 is recorded as integrated hydrodynamic energy loss from the system through the H5 bound-
 383 ary (from dayside closed field line region to the magnetosheath) during main phase. Si-

384 multaneously, magnetic energy in the newly opened field is drawn back into the system
 385 through the lobes. This is what is recorded as the integrated Poynting flux injection through
 386 S1 boundary from the magnetosheath into the open lobes. The results clearly show that
 387 these two interfaces dominate the energy flux transport. As the latter is a source and
 388 the former is a sink, the result demonstrates how the magnetosphere simply captures a
 389 portion of energy coming from the solar wind: During the main phase, both the escape
 390 and injection increase, and it is only the imbalance that increases the system's total en-
 391 ergy.

392 Detailed examination of the energy distribution between the open and closed field
 393 line regions reveals a significant amount of recirculating Poynting flux, which comes into
 394 the closed region through the tail (boundary 2b from the tail lobe into the nightside plasma
 395 sheet) and returns almost as much through the cusp interface (boundary 2a from day-
 396 side closed field region to the open field region). This explains why the closed field line
 397 energy is decreasing during main phase, while the lobe energy content and total mag-
 398 netospheric energy content are increasing.

399 It would seem that the closed field region is not able to trap all the (electromag-
 400 netic) energy generated by the flux erosion on the dayside. While plasma cannot be con-
 401 fined in the open flux lobes, the results demonstrate how the open flux region can ac-
 402 cumulate and store energy by setting up this recirculation pattern. During the storm main
 403 phase, the volume and energy of the lobes grow, despite exchanging vast amounts of en-
 404 ergy at both ends.

405 To understand the dynamics at the end of main phase (time $T=0$ hours), we put
 406 several clues together. First, energy in the lobes is rapidly lost while the closed region
 407 energy rapidly increases. While the total energy does increase, the change mostly ap-
 408 pears as a transport of energy from the lobes to the closed region (see stack plot in Fig-
 409 ure 6). Qualitative results of the 3D magnetopause surface with the four field junction
 410 neighborhoods displayed (see Figure 9) show the potential reconnection locations wash
 411 over large regions of the open flux lobes, and later those sections changing topology to
 412 closed field. The only way for the open lobes to become closed in this way is for recon-
 413 nection to occur on both north and south lobes, i.e., dual lobe reconnection is taking place.

414 Examination of the internal energy flux results at that moment shows that the di-
 415 rection of flux reverses, as energy flows from the lobes to the dayside closed field just af-
 416 ter the main phase end. While the signs of dual lobe reconnection are clear in the sim-
 417 ulation results, unfortunately the satellites were not well positioned during the end of
 418 the main phase to record that phenomenon. However, THEMIS crossings earlier in the
 419 main phase suggest that the simulation overpredicts the rate of reconnection as evidenced
 420 by overabundance of thermal and kinetic energy and missing closed magnetic flux. This
 421 may mean that the amount of dual lobe reconnection seen in the simulation is overpre-
 422 dicted and warrants further investigation.

423 Finally, we discuss how the solar wind driving relates to the energy dynamics. Clearly
 424 both the external and internal energy pathways show a difference between the main phase
 425 and recovery phase as the IMF B_z component rotates away from due southward orien-
 426 tation. For the external energy flux values, the sharp decline does not occur until both
 427 the IMF B_z and B_y magnitudes drop, which confirms that it is the clock angle that
 428 is important to the solar wind – magnetosphere coupling rather than the IMF B_z alone.
 429 However, for the internal energy transport, the energy flux sharply decreases about 90
 430 minutes earlier, which does correspond to the decrease in IMF B_z . This would seem to
 431 indicate that the internal circulation loop is more strongly associated with B_z rather than
 432 the IMF clock angle. The different responses of the system highlight the complexity of
 433 the dynamics and hence the difficulty in devising universal coupling parameters targeted
 434 to predict the system state.

6 Discussion

Our results depict a different picture of energy storage in the magnetosphere system from that of Akasofu (1981). In particular, we note that energy is indeed stored in the tail lobes in electromagnetic form, by increasing the magnetic field strength in the lobes. This energy accumulation is realized as a recirculation pattern where the energy in the lobes is transferred from the dayside closed region to the nightside tail region, and as more energy is added to the system, the boundaries of the lobes expand and the field magnitude increases to accommodate the increased energy content.

Another way to illustrate the magnetic energy input and recirculation within the magnetosphere is using the language of basic circuit elements (see e.g. Mays et al. (2009), who have taken this approach to a fully fledged model). In this representation, the lobes act as a combination of inductors and capacitors which store and release magnetic energy via the magnetopause, tail, and Region 1 currents, which are all connected and driven by the solar wind electric potential. Because the energy transported through the lobes is almost entirely magnetic, this analogue provides a good illustration of how the energy dynamics work in that region.

Moving from the energy storage to the energy transport, the cusp plays a key role in determining the internal magnetospheric transport. In a previous study of the cusp using Cluster observations, Pitout et al. (2021) argue that motion of the reconnection line across the cusp should reverse the flux transport between open and closed field lines. Our results indicate that this trend indeed holds in that the energy transport between dayside lobes and closed region reverses, although the actual dynamics of the reconnection line appear to be much more complex than that represented by a two-dimensional cartoon.

Considering these global magnetosphere dynamics from the ionospheric perspective, our results are consistent with the Expanding Contracting Polar Cap (ECPC) theory (Lockwood et al., 1992). In this theory, the polar cap boundary is formed as an unsteady superposition of dayside flux expansion with the nightside flux contraction, and the rest of the polar cap boundary expands along the adiaroic (Siscoe & Huang, 1985) boundary. This simultaneous expansion and contraction of magnetic flux is exactly the same as re-circulation of magnetic energy through the system presented here (see Figure 10). Future work to merge the ionospheric results with the magnetospheric dynamics presented here can bridge the difference in terminology and solidly quantify magnetosphere-ionosphere coupling in terms of energy and magnetic flux transport.

The internal circulation pathway seen in our results can be directly linked to cold dense material from the plasmasphere being recirculated up and over the poles. This scenario presented by Freeman et al. (1977) demonstrates the same pathway that the magnetic energy would flow; $\mathbf{E} \times \mathbf{B}$ corresponds to both plasma drift motion and magnetic energy flux. In other words, the slow cold plasma with strong magnetic field frozen in moves across the poles and recirculates sunward in the closed field region. A more recent study by Christian-Andrew Bagby-Wright et al. (2023) using a coupled plasmasphere model demonstrates how this effect would also evolve throughout a storm. In this work, without the coupled multi-fluid model, the recirculation plasma should have much lower densities. Adding a plasmasphere model could change both the magnitude and timing of the recirculation energy.

A large part of the cusp energy dynamics seen here is connected to dual lobe reconnection happening in the simulation. Imber et al. (2007) have shown observational evidence of such phenomenon occurring when the IMF $B_z > 0$ and clock angle is close to zero (due northward IMF), which is what we observe at the end of the main phase of the Starlink storm studied here. However, based on the limited observations available for this event, it is likely that the simulation is overpredicting the scale and widespread

486 nature of reconnection, which leads to more dual lobe reconnection than occurred in re-
487 ality.

488 There are many ways available to adjust reconnection physics in the simulation.
489 First, in the ideal MHD framework, the reconnection rate is determined by the numer-
490 ical diffusion of the magnetic field, which is affected by the grid size as well as the choice
491 of numerical implementation including the scheme, limiter, speed of light adjustment fac-
492 tor, etc. (Ridley et al., 2010). Second, other physics can be included by changing the MHD
493 equations to include more terms (Hall or resistive MHD) or including a coupled parti-
494 cle in cell model (Chen et al., 2017) in limited regions of the simulation. Importantly,
495 this work demonstrates the capability to quantify the energy dynamics processes, which
496 will enable future studies using these tools to probe the connection between the kinetic
497 reconnection physics and the global energy transport.

498 7 Conclusion

499 In this study the Space Weather Modeling Framework (SWMF) was used in the
500 Geospace configuration to simulate Earth’s magnetosphere for a storm event on Febru-
501 ary 3, 2022 (the Starlink event). The energy transport was examined by identifying two
502 distinct volumetric regions and several surface interfaces. Consistent with previous work,
503 we found that kinetic and thermal energy escapes the dayside closed field region, and
504 magnetic energy is injected through the lobes during storm main phase. At the same time,
505 an internal recirculation pattern is set up that transfers magnetic flux from the lobes to
506 the closed field region in the nightside and back from the closed field to the open lobes
507 through the dayside cusp region.

508 At the end of the main phase, the simulated magnetosphere undergoes dual lobe
509 reconnection which rapidly depletes the magnetic energy flowing through the lobes while
510 adding net energy to the system. However, satellite observations and the Sym-H index
511 indicate differences between the simulation and observed values at that time, which may
512 indicate that the model is not capturing the true dynamics of the system. This may act
513 as evidence of the effects of kinetic scale physics on the global energy dynamics, high-
514 lighting the need to resolve the small scale physics in order to be able to quantify the
515 large scale effects.

516 Returning to the questions posed in the introduction, we conclude the following:

- 517 1. The open magnetotail lobes play a critical role in the energy balance in the mag-
518 netosphere during storm times. The total magnetospheric energy distribution be-
519 tween the lobes and the closed field region is determined by how much energy is
520 allowed to recirculate from the dayside closed region into the lobes under south-
521 ward IMF conditions. This energy transfer rate is controlled by the IMF B_z .
- 522 2. External energy exchange at the magnetopause is found to be consistent with pre-
523 vious studies, with plasma energy flowing out through the dayside magnetopause
524 and Poynting flux entering through the nightside magnetopause. The latter pro-
525 cess is controlled by the IMF clock angle $\theta = \tan^{-1}(B_y/B_z)$. Internal magnetic
526 energy transits from the lobes directly into the nightside closed region, and a por-
527 tion of that energy is circulated back into the lobes through the cusps on the day-
528 side. The cusp dynamics ultimately thereby determine the internal energy circula-
529 tion.

530 8 Open Research

- 531 • The simulation output data used for calculating magnetosphere energy transport
532 in this study are available at [Deep Blue Repository Setup in Progress] via [DOI
533 TBD] with [license, access conditions]

- 534 • Version 9.90 of the Space Weather Modeling Framework is used for simulating geospace.
 535 Access to the full SWMF requires user registration and signing the user license
 536 agreement. An open source version is preserved at [https://github.com/MSTEM-](https://github.com/MSTEM-QUADA/SWMF)
 537 [QUADA/SWMF](https://github.com/MSTEM-QUADA/SWMF). The open source version of the SWMF is the Michigan Sun-to-
 538 Earth Model with Quantified Uncertainty and Data Assimilation (MSTEM-QUADA
 539 distributed under a non-commercial license), for more information about the user
 540 license agreement and the open source version see <http://csem.engin.umich.edu/tools/swmf/>.

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Table 1: Time integrals over the storm main phase of the hydrodynamic energy flux, Poynting flux, and total energy flux.

	Energy [PJ]	$\int H dt$	$\int S dt$	$\int K dt$
1	Lobes→Sheath	+4.67	-97.28	-92.61
2a	Closed→Lobes (day)	+11.20	+58.82	+70.01
2b	Closed→Lobes (night)	-3.45	-153.12	-156.56
3	Lobes→Inner	-1.72	-15.34	-17.06
4	Lobes→TailCut	+7.01	+3.94	+10.96
5	Closed→Sheath	+46.62	+14.57	+61.19
6	Closed→TailCut	-10.57	-6.21	-16.79
7	Closed→Inner	+12.69	+40.48	+27.80

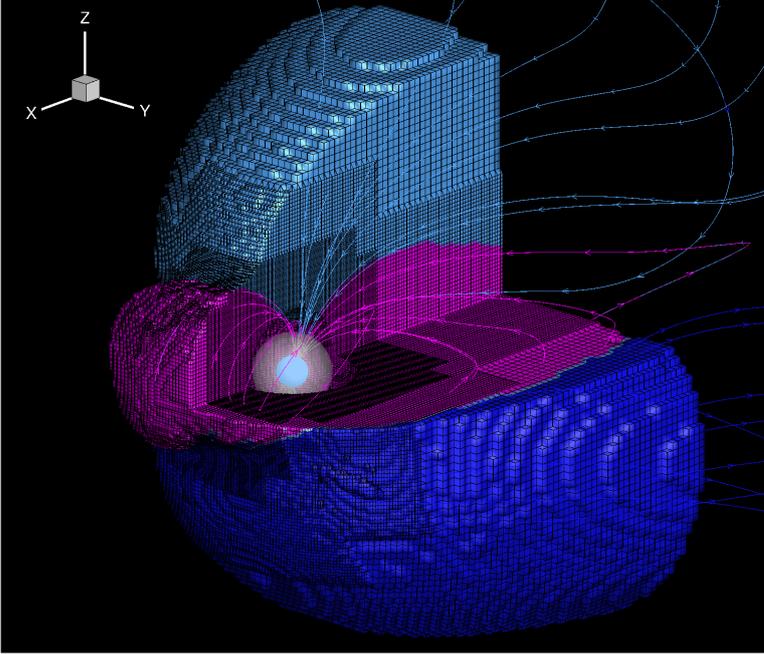


Figure 1: Cut-away of the 3D magnetosphere showing various regions and the grid resolution of the simulation. Magenta: Closed field line region, Blue: Lobes, Grey: Inner boundary surface.

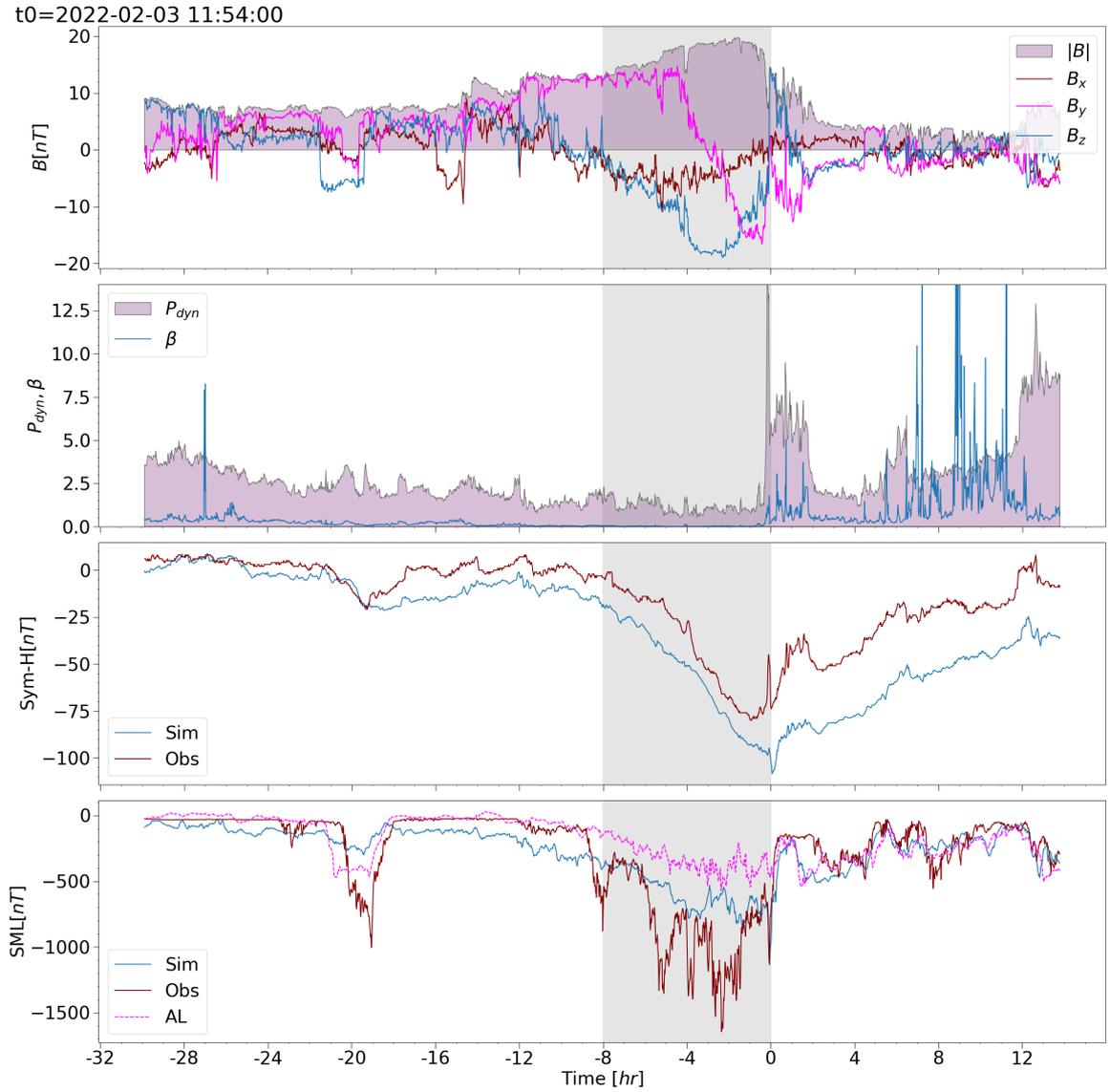


Figure 2: Panels from top to bottom: The IMF components and magnetic field magnitude; Solar wind dynamic pressure (shaded) and plasma β (blue); Observed (red) and simulation (blue) SYM-H index; and Observed (red) and simulation (blue) SML index. The simulation AL index (magenta) is shown for comparison.

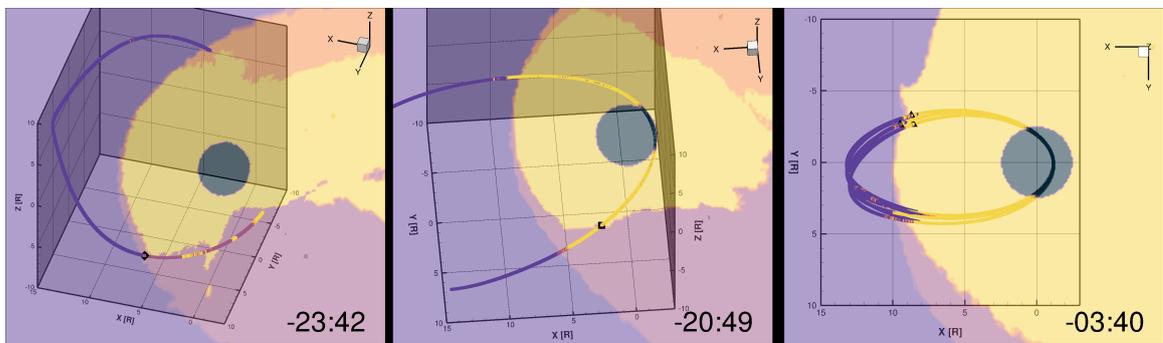
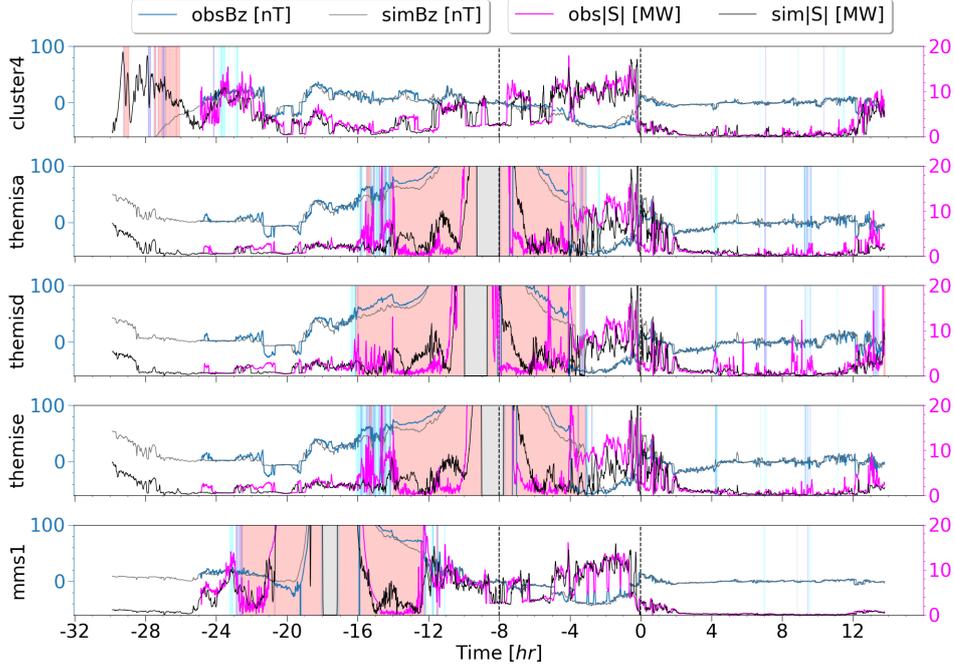


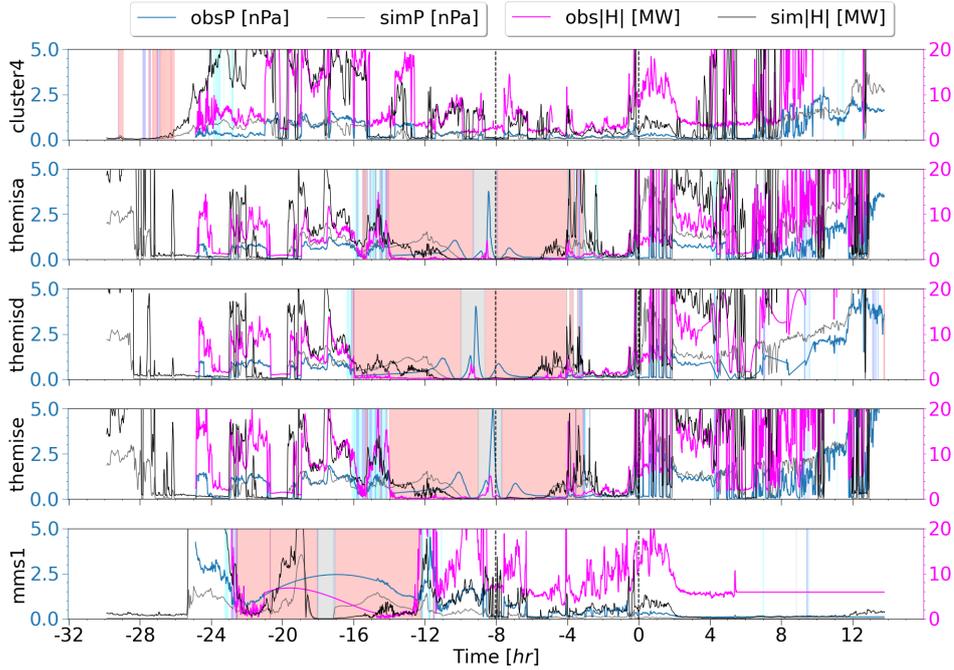
Figure 3: Orbit plane slices showing the trajectories within the simulation domain with contour of the virtual satellite status. Cluster4 (left), MMS (center), Themis (right). Color coding shows the status variables closed (yellow), Open-North (orange), Open-South (maroon), Open-Solar Wind (purple), Outside simulation domain (black).

t0=2022-02-03 11:54:00



(a)

t0=2022-02-03 11:54:00



(b)

Figure 4: (a) (Left vertical axis) Magnetic field B_Z time series from Cluster-4, Themis-A, Themis-D, Themis-E, and MMS-1 spacecraft (blue) and simulated B_Z at the satellite locations (gray). (Right vertical axis) The observed (magenta) and simulated (black) Poynting flux \mathbf{S} defined in equation 2. (b) (Left vertical axis) Plasma total pressure $P = P_{th} + P_{dyn}$ time series from Cluster-4, Themis-A, Themis-D, Themis-E, and MMS-1 spacecraft (blue) and simulated P at the satellite locations (gray). (Right vertical axis) The observed (magenta) and simulated (black) hydrodynamic energy flux \mathbf{H} defined in equation 1. Vertical shading indicates virtual satellite location status within the open (blue), closed (red), magnetosheath or solar wind (white).

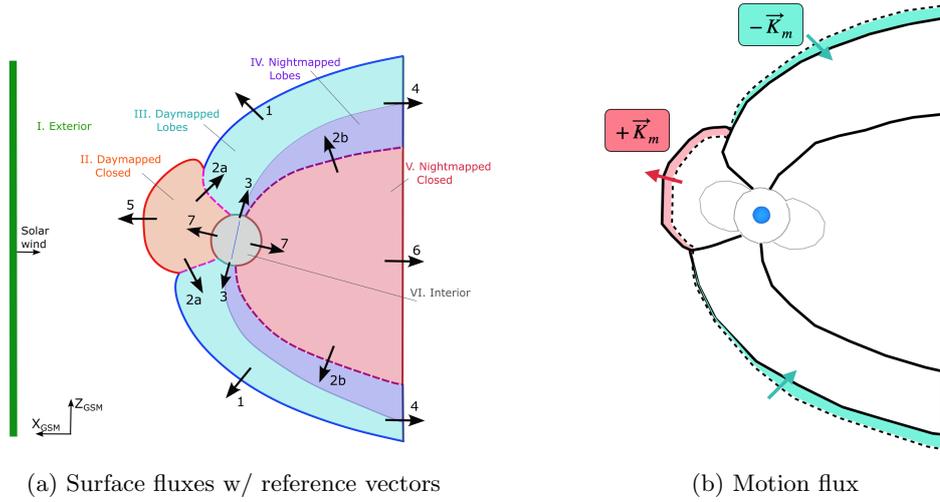


Figure 5: (a) Diagram of the magnetospheric cross section in GSM $X - Z$ plane showing reference vectors for energy fluxes between the sheath and lobes (1), lobes and closed (2a, 2b), closed and sheath (5) as well as magnetic flux transport at the inner boundary (3, 7), and through the tail cut off (4, 6). (b) Illustration of boundary motion contribution to surface flux. Between a time t_0 (solid lines) and t_1 (dashed lines), flux is transported to surface flux. Between a time t_0 (solid lines) and t_1 (dashed lines), flux is transported away from the dayside and towards the lobes as the volumes contract and expand.

$t_0=2022-02-03\ 11:54:00$

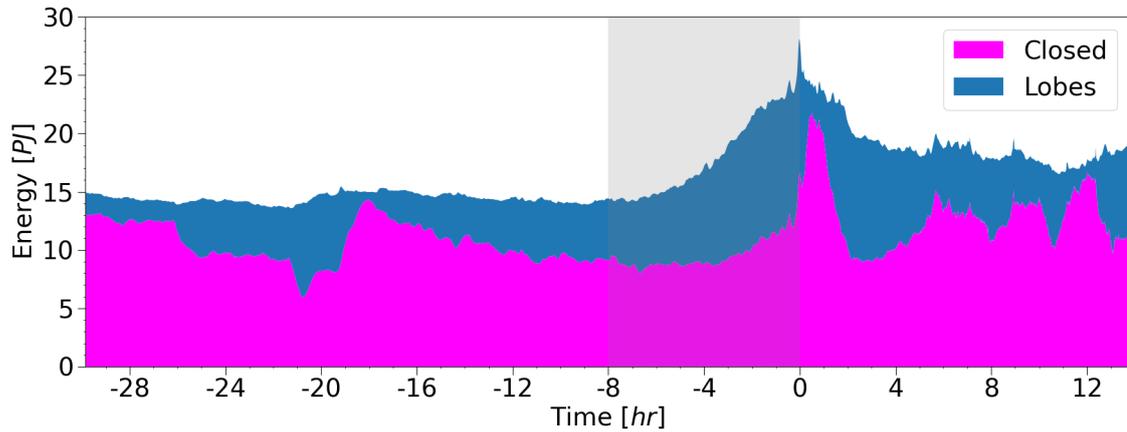


Figure 6: Time series of energy content in the open lobes (blue) and closed magnetosphere (magenta) regions in the magnetosphere in a stackplot format. The vertical shaded portion indicates the storm main phase.

t0=2022-02-03 11:54:00

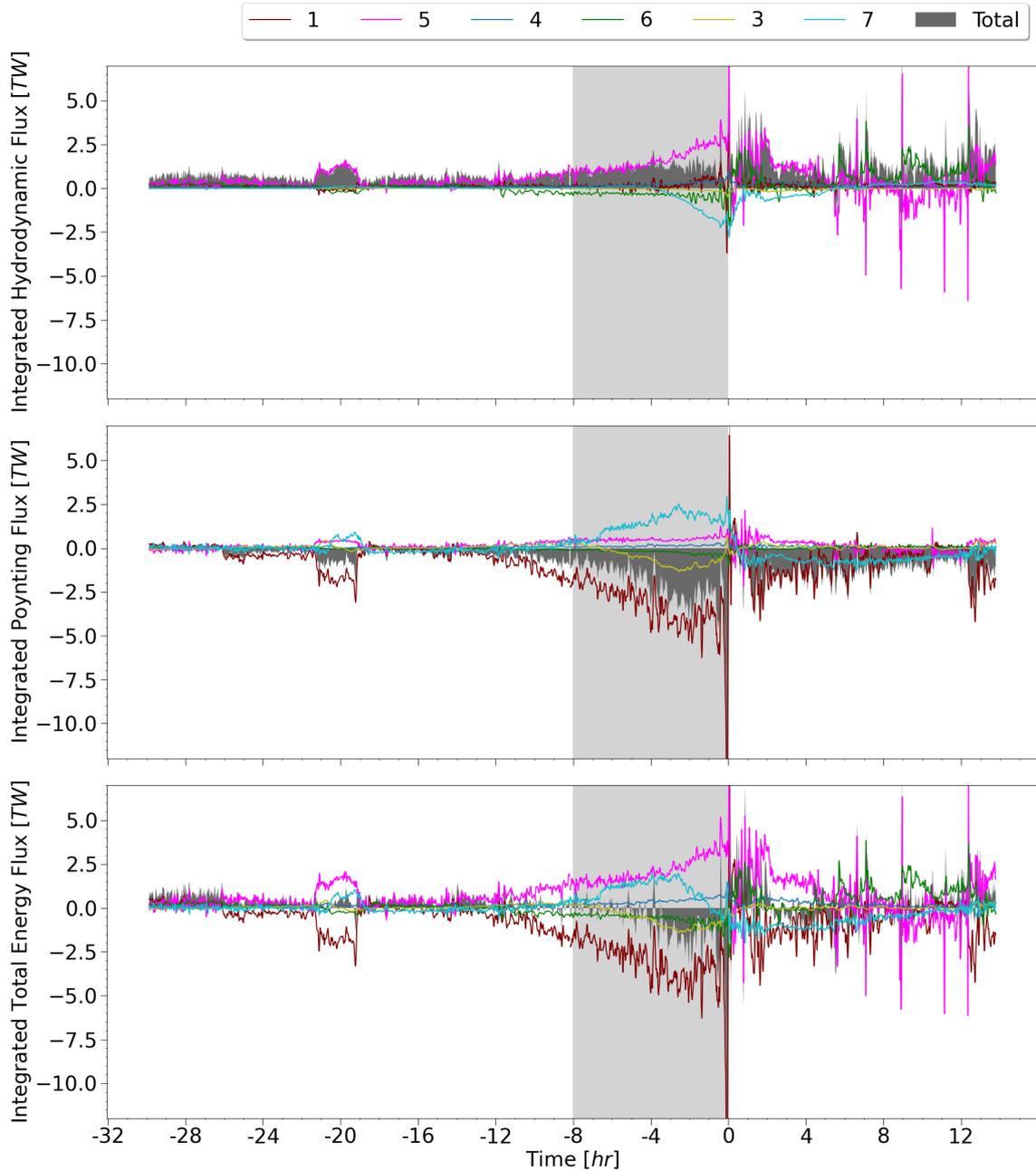


Figure 7: Time series of spatially integrated energy flux values over magnetospheric external interfaces: 1 open tail lobes – magnetosheath, 5 closed field region – magnetosheath, 4 open tail lobes – tail cutoff, 6 closed field region – tail cutoff, 3 open tail lobes – inner boundary (ionosphere), 4 closed field region – inner boundary (ionosphere). Top panel gives the hydrodynamic energy flux, middle panel gives the Poynting flux, and the bottom panel gives the total energy flux. Solid gray shading indicates the summed total of all individual contributions. Negative (positive) values indicate energy increase (decrease) in the magnetospheric volume between the inner boundary and the magnetopause.

t0=2022-02-03 11:54:00

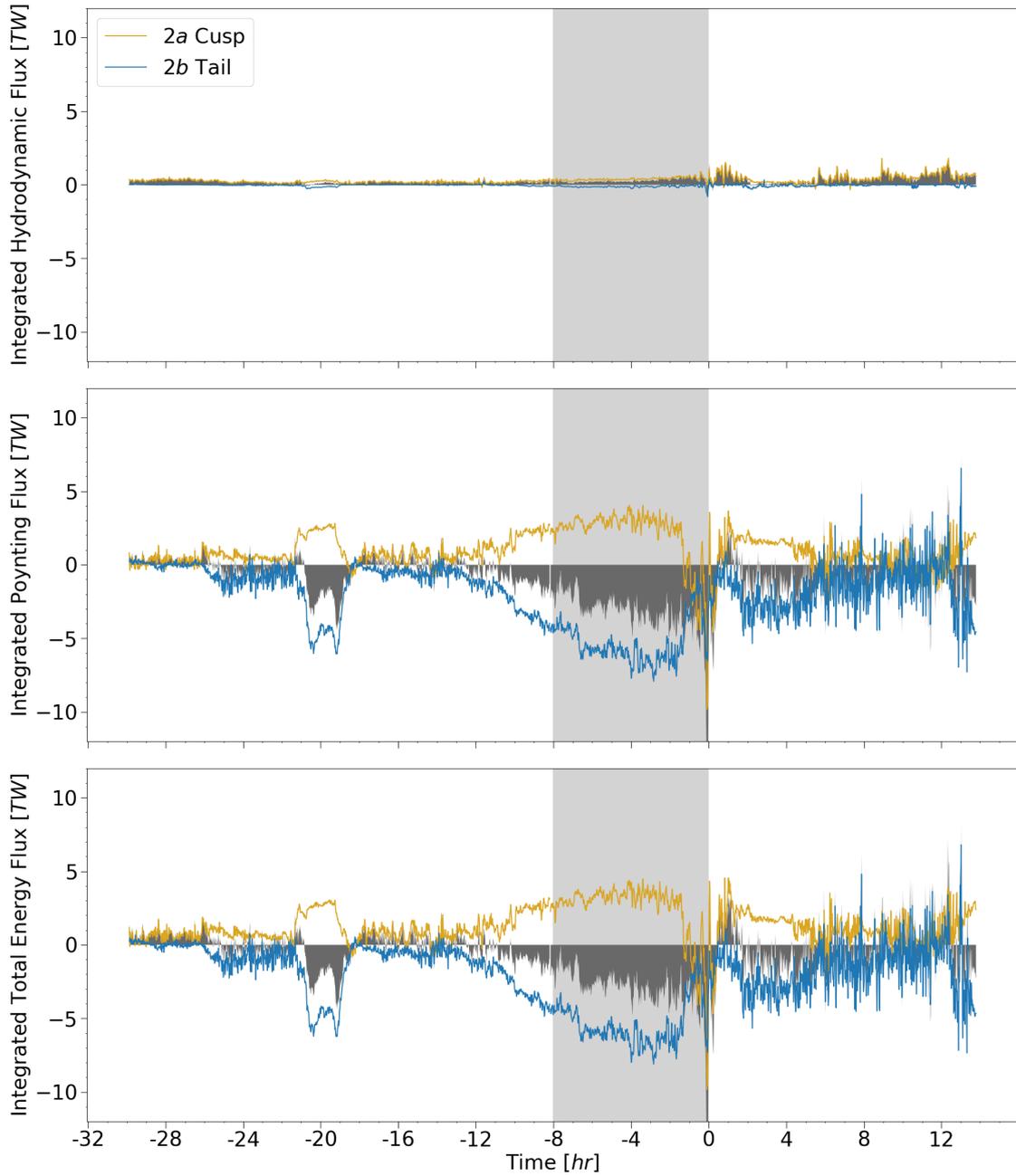


Figure 8: Time series of spatially integrated flux values over magnetospheric internal interfaces: 2a dayside closed field region – open tail lobes (cusp), 2b nightside closed field region – open tail lobes (tail). Top panel gives the hydrodynamic flux, middle panel gives the Poynting flux, and the bottom panel gives the total energy flux. Solid gray shading indicates the summed total of all individual contributions. Negative (positive) values indicate energy increase (decrease) in the closed field region, the opposite is true for the lobes.

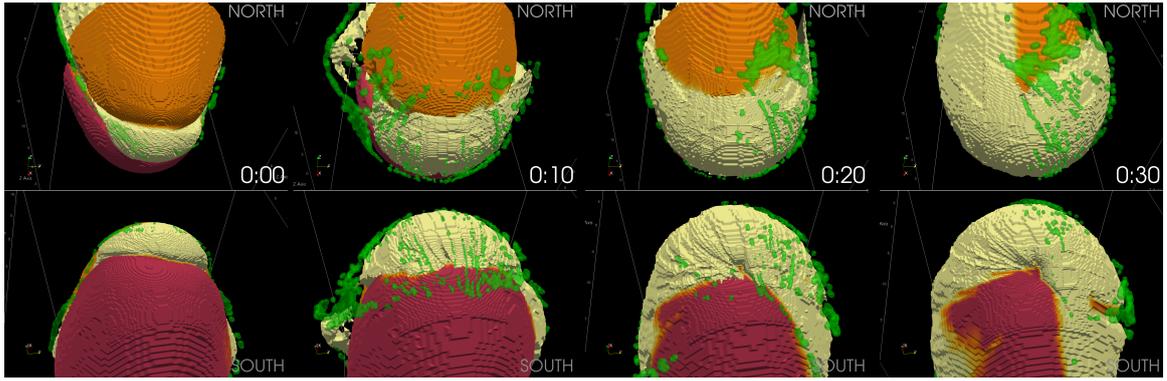


Figure 9: Snapshots of simulated magnetopause surface colored by Status (Yellow - closed, Orange - open north, Red - open south). Two views show the northern and southern cusp regions. The green iso-surfaces indicate neighborhoods around four field junctions (cells with status open-open, open-closed, closed-open, and closed-closed all adjacent), which indicate possible magnetic reconnection locations. Snapshot at $T=0$ is taken just after IMF northward turning and at three consecutive times 10-min apart, showing a single dayside X-line morphing and dual lobe reconnection occurring.

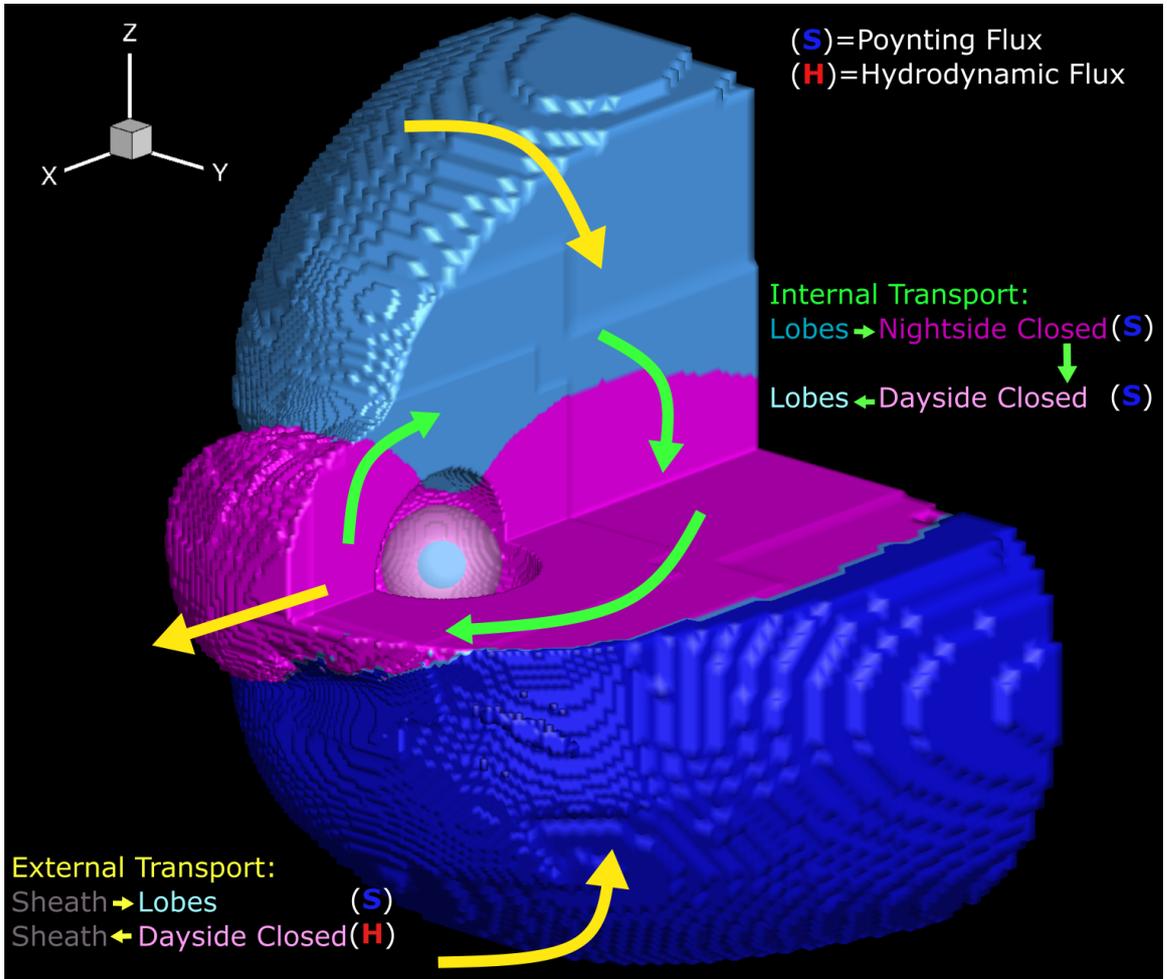


Figure 10: Summary of energy transport pathways. During most of main phase both an internal and external energy pathway were found following the corresponding arrows.