

1 **Statistics on omega band properties and related geomagnetic variations**

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10

11 **Key Points:**

- 12 • Super-epoch analysis confirmed the typical ground magnetic variations for omega
13 structure - bipolar pulse in B_y and short B_z decrease
- 14 • Omega structures produce 50-100% higher than averaged dB/dt during low and
15 moderate geomagnetic activity
- 16 • Statistically confirmed that ground dB/dt value depends on omegas velocity and size.

17 **Abstract**

18 Using the list of the omega structures based on the The Magnetometers - Ionospheric Radars-
19 Allsky Cameras Large Experiment (MIRACLE) network (Partamies et al. 2017), we obtained a
20 number of important statistical characteristics describing the surface magnetic field. Based on
21 438 events, typical magnetic variation associated with the passage of the single omega were
22 obtained. The typical variation, obtained using superposed epoch analysis, is associated with a
23 local bending of the western electrojet and statistically confirms the distribution of equivalent
24 ionospheric currents obtained in earlier observations of single omegas. It was found that during
25 low and moderate geomagnetic activity, appearance of the omega structures in the dark morning
26 MLT sector results in twice higher than average dB/dt on the ground surface. Also, the velocity,
27 direction of movement, and area of omega structures were calculated. It is shown that faster and
28 bigger omegas produce larger time derivatives of the ground magnetic field. Furthermore, we
29 demonstrate that in the 03-08 MLT sector, superposed magnetic variations for the arbitrary
30 events of very high time derivatives $|dB/dt| > 10\text{nT/s}$, reveal magnetic signatures similar to
31 omegas. Our findings, together with the results described in Apatenkov et al., 2020, emphasize
32 the important role of omega structures in the formation of large geomagnetically induced
33 currents.

34

35 **1 Introduction**

36 Auroral omega bands are specific auroral forms emerging as a set of quasi-periodic long-
37 living undulations in the poleward side of diffuse auroral arc, which have typical scale size from
38 several hundred to several thousand kilometers, life time up to 100 min and drift eastward with
39 the speed of 0.4-2 km/s (Akasofu and Kimball, 1964; Henderson et al., 2001; Sergeev et al.,
40 2003).

41 Based on the MIRACLE all-sky camera data from five identical Lapland stations,
42 Partamies et al. (2017) have performed the largest statistical study of some omega band
43 properties. Using semi-automated search methods, they detected 438 individual auroral omega
44 structures in 1996-2007. Such representative statistics led to the following solid conclusions,
45 complementing previous works. (1) Omega bands are typically observed in the morning sector
46 towards the end of substorm expansion phase or during recovery phase (Akasofu 1974;
47 Opgenoorth et al., 1994). It is worth to note, the omega bands tend to appear during higher than
48 average substorm activity, characterized by averaged local electrojet index $IL = -250\text{ nT}$, which is
49 almost twice as intense as the average IL level for all substorms detected in this region
50 (Partamies et al., 2015). (2) An average altitude of peak emission within omega structures is 118
51 km. This gives an estimate of a few keV for the characteristic energy of precipitating electrons,
52 which agrees with previous estimates (Amm et al., 2005; Wild et al., 2011). (3) Each individual
53 omega was found to match with two-vortex equivalent Hall current structure associated with the
54 pair of field-aligned currents where upward current corresponds to the bright part of omega
55 undulation (Amm et al., 2005; Weygant et al., 2015).

56 The same set of omega structures from Partamies et al. (2017) was used by Andreeva et
57 al. (2021) to statistically investigate the omegas' source location. The authors projected the
58 omegas from the ionosphere to the magnetospheric equatorial plane, using the fresh empirical
59 magnetic field model (Tsyganenko and Andreeva, 2016). Ionosphere-to-magnetosphere
60 projection show that the omegas' source is located relatively close to Earth at radial distances of
61 6-13 R_E , supporting previous case study results (Liu et al., 2018; Wild et al., 2011; Weygand et
62 al., 2015). Velocity estimates for omega projections revealed the radial earthward propagation of
63 the omegas' source region at a typical speed of several tens of km/s, in addition to expected
64 eastward propagation observed in the ionosphere (Opgenoorth et al., 1983; Sergeev et al., 2003).

65 In the present study, we will further extend the set of characteristic omega band
66 properties using the same list of omegas from Partamies et al. (2017). Here, we will focus on the
67 ground magnetic field perturbations, particularly dB/dt amplitudes, and their link to the
68 kinematic characteristics such as size and drift velocity of omegas. The ground magnetic
69 perturbations are of special interest for space weather applications since they cause
70 geomagnetically induced currents (GIC) in long conducting systems – power grids, pipelines,
71 railway grids (Pulkkinen et al., 2017).

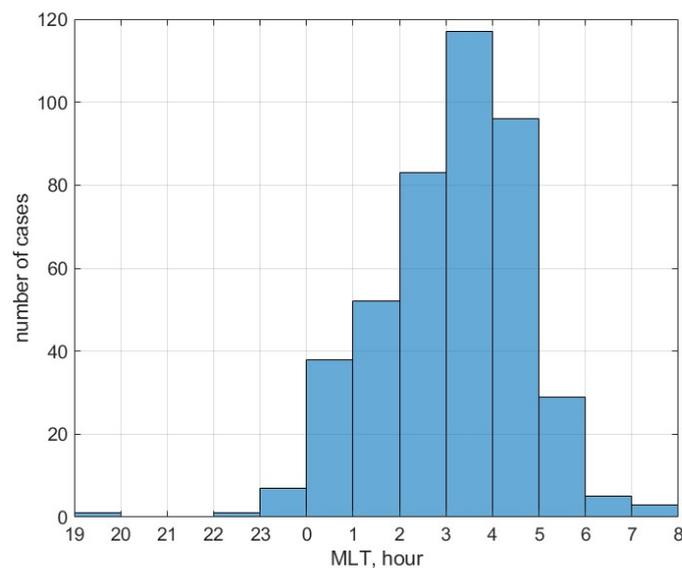
72 Inductive coupling between dB/dt and electric field that drives GIC is not linear due to
73 the finite Earth's conductivity, so a large but short dB/dt impulse does not necessary produce
74 large GIC (Cagniard, 1953; Oyedokun et al., 2020). This nonlinearity in the dB/dt-GIC
75 relationship is less pronounced for the lower frequency magnetic field variations with periods
76 more than 1 minute, including Pi3/Ps6 range of pulsations (Heyns et al., 2021) inherent to omega
77 bands (Saito, 1978; Gustafsson et al., 1981; Opgenoorth et al., 1983; Jorgensen et al. 1999;
78 Viljanen et al., 2001). This gives confidence to use dB/dt as a proxy for GIC in the case of
79 omega bands. In addition, it was shown in Apatenkov et al. (2020) that the largest GIC (>100 A)
80 ever recorded in the Kola Peninsula power grid was caused by omega band activity, and the main
81 inductive effect was linked to the spatial derivative associated with omega motion. Omega
82 bands, being compact transient auroral phenomena, have localized but significant effect on the
83 ground systems in high latitudes. In this paper, we study this effect for the first time on a
84 statistical basis.

85 This paper is structured as follows. The all-sky camera data and the ground magnetic
86 field data for the utilized set of omega cases are described in the next Section. Superposed
87 ground magnetic variations are discussed in Section 3. In Section 4, we evaluate how the
88 presence of omegas affects time derivatives of the geomagnetic field observed on the ground. In
89 Section 5, we present the procedure to derive velocity, direction, and areas of the studied omega
90 structures. In Section 6, we estimate the relation between maximum |dB/dt| and omega's velocity
91 and area. Finally, in the discussion, we look on the typical magnetic variations corresponding to
92 the extreme |dB/dt|>10 nT/s cases.

93

94 **2 Instruments and data**

95 Partamies et al. (2017) [hereinafter P17] provided a list of omega shape auroras which
 96 were observed with the All-sky cameras (ASC) at five MIRACLE network stations during 1996-
 97 2007. These stations are located in Fennoscandian Lapland at the auroral latitudes: Sodankylä
 98 (SOD, 63.92° N corrected geomagnetic latitude), Muonio (MUO, 64.72° N), Abisko (ABK,
 99 65.30° N), Kilpisjärvi (KIL, 65.88° N) and Kevo (KEV, 66.32° N). P17 introduced a semi-
 100 automatic method to detect the omega shape auroras during the nighttime hours from September
 101 to April (when the Sun is more than 10 degrees below the horizon). In our statistical study we
 102 utilize the entire list of 438 omegas introduced in P17 paper.



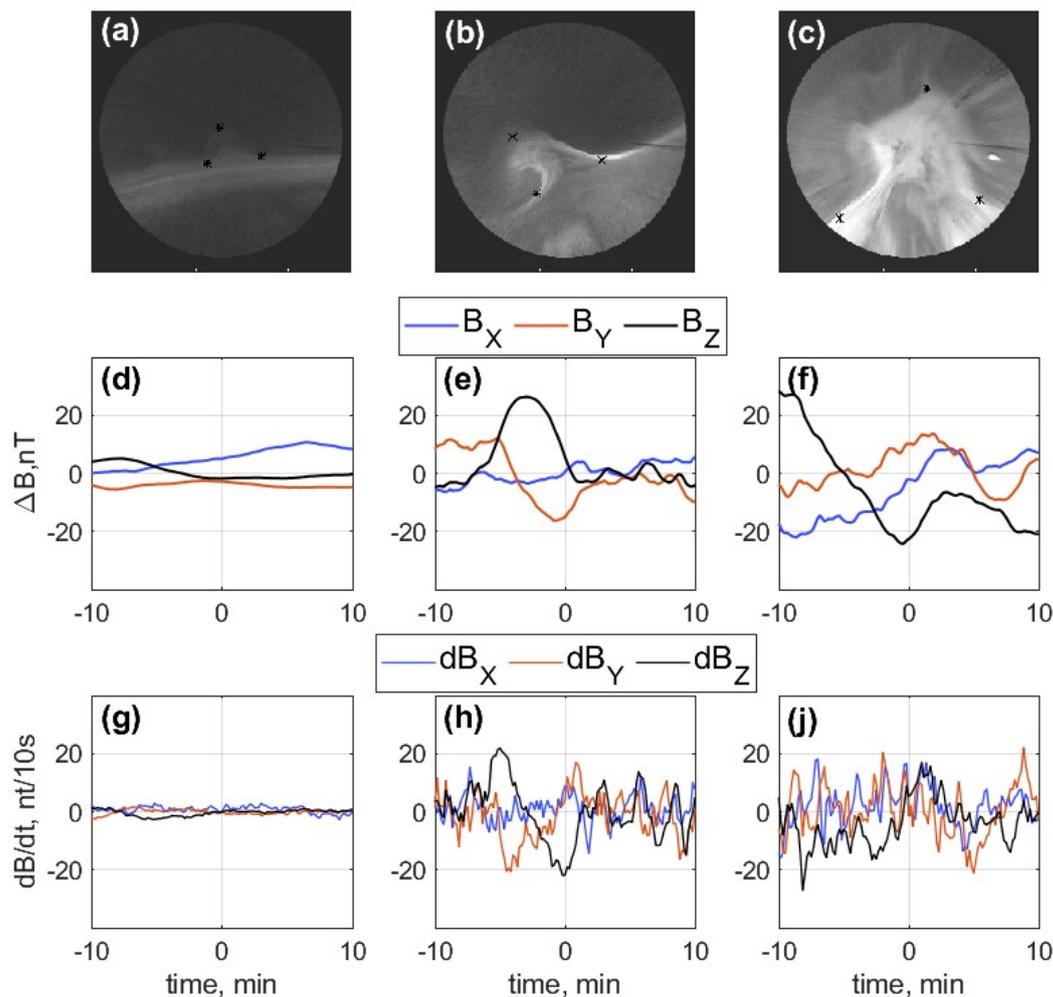
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104 **Figure 1.** Magnetic local time distribution for the observed omega structures.

105 Figure 1 shows the distribution of omegas' magnetic local time (MLT) when most of the
 106 structure was well observed within the camera field of view. The selected cases occupy 23-08
 107 MLT with 68% of the omegas observed within 02-05 MLT morning sector. Majority of the
 108 events (335) corresponds to an individual omega, i.e. the next omega appears after more than
 109 half an hour. The omegas are tracked within the ASC field of view from 4 to 15 minutes. Taking
 110 into account the average altitude of the observed in P17 omegas $h=118$ km, the size of the
 111 omegas is restricted to the area of a circle with diameter of about 600 km. Note that the
 112 horizontal scale size of omegas can be more than 1000 km (Tanaka et al. 2015).

113 Ground magnetic data were provided by the IMAGE network magnetometers
 114 (Tanskanen, 2009) at 10s time resolution at the same observatories with ASCs (20s resolution).
 115 The time derivatives and the variations of the geomagnetic field are investigated in three field
 116 components: horizontal X (northward), horizontal Y (eastward), and vertical Z (directed to the
 117 Earth's center).

118 In Figure 2, we include three examples of the ASC images captured at Sodankylä station
 119 at the following times 01:07:00 UT in 12 September 2002, 01:42:40 UT in 5 March 2001, and
 120 01:38:20 in UT 02 October 2002. These examples show a large diversity of the shape, size, and
 121 brightness of omega structures. Below, we show the variations and time derivatives of the
 122 geomagnetic field components within ± 10 minutes around the noted time. The amplitude of the
 123 perturbations significantly increases for brighter and bigger structures at Figure 2b and c. On the
 124 contrary, no pronounced magnetic effects are seen near the peak time corresponding to the faint
 125 omega in Figure 2a.

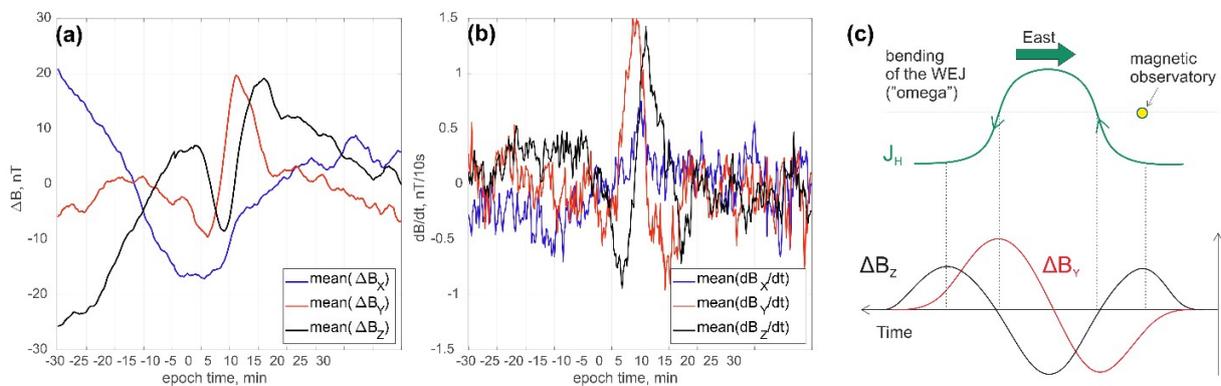


126
 127 **Figure 2.** The examples of omega observations by the ASC at Sodankylä : a) 01:07:00 UT, 12
 128 September 2002; b) 01:42:40 UT, 5 March 2001; c) 01:38:20 UT, 02 October 2002; below are
 129 the corresponding variations and time derivatives in X (blue), Y (red), and Z (black) components
 130 of the geomagnetic field within ± 10 minutes of the time when the images were taken.

131 Figure 2 shows that not every individual omega has specific and clear magnetic
 132 signatures. The variations are different in shape and amplitude. Thus, a superposed epoch
 133 method is used to study the typical magnetic variations associated with an omega passage.

134 **3 Results**135 **3.1. Superposed geomagnetic variations**

136 Using the geomagnetic data of the IMAGE network, we select one hour intervals which
 137 were centered with respect to the peak time (Partamies et al., 2017), which is the time when the
 138 most omega-like structure was observed within the ASC field of view. The magnetic data were
 139 recorded during different years and seasons so the baselines can differ dramatically. The
 140 averaged values were subtracted to be able to superpose and compare the magnetic variations.
 141 This is applied to every component. This is a very rough estimate of the background/baseline
 142 field. Nevertheless, this simple and fast procedure is suitable when studying the magnetic field
 143 variations rather than absolute values. Ps6 pulsations associated with omega bands (Saito, 1978)
 144 have periods 3-5 times shorter than one hour so the average value is expected to be close to the
 145 pulsations' "zero level".



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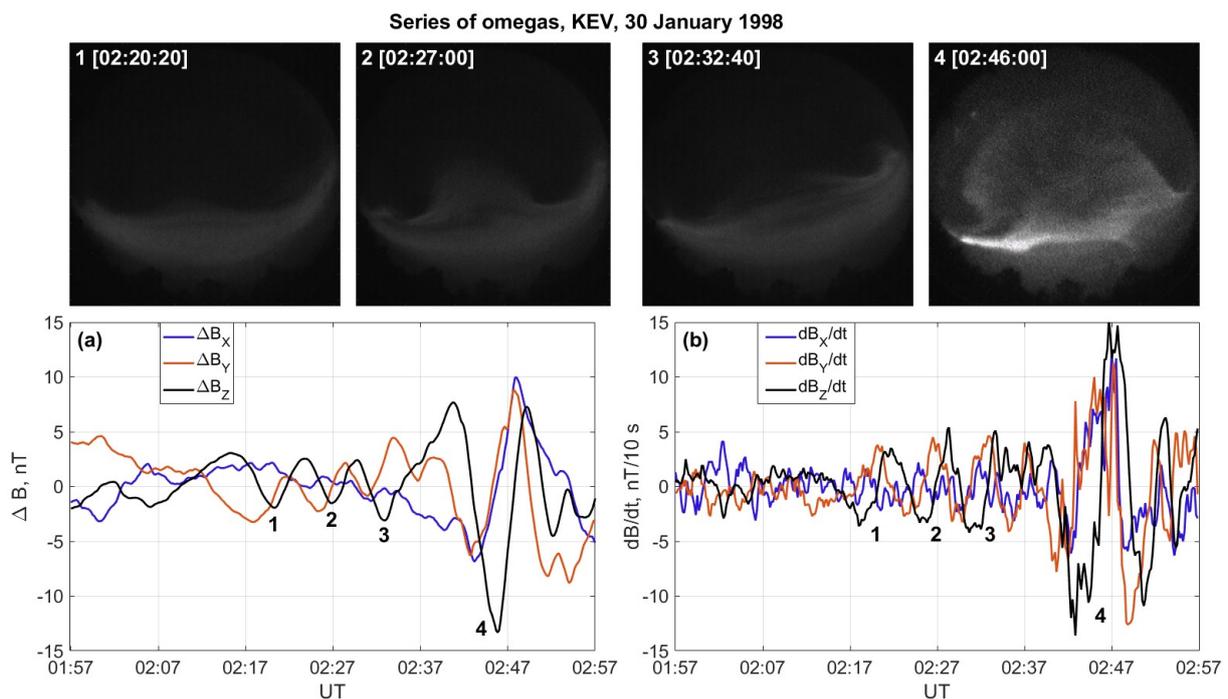
147 **Figure 3.** The examples of omega observations by the ASC at Sodankylä : a) 01:07:00 UT, 12
 148 September 2002; b) 01:42:40 UT, 5 March 2001; c) 01:38:20 UT, 02 October 2002; below are
 149 the corresponding variations and time derivatives in X (blue), Y (red), and Z (black) components
 150 of the geomagnetic field within ± 10 minutes of the time when the images were taken.

151 Figure 3a shows superposed variations of X (geographic North), Y (geographic East), and
 152 Z (downwards) geomagnetic field components for the entire set of 438 observed omegas. We
 153 found a surprising fact that so different individual magnetic recordings being summed up show
 154 the distinct variation attributed to the omega passage. Two time scales can be distinguished
 155 within these magnetic signatures: (1) short - ten minutes around the omega, ± 5 minutes close to
 156 zero epoch time, and (2) long - about 30 minutes preceding to the omega.

157 The short time scale can be explained by eastward propagation of the ionospheric current
 158 structure typical for the omega. Opgenoorth et al. (1983) and Amm et al. (2005) show the intense
 159 current directed equatorward at the western part of the omega carried mainly by Hall current.
 160 Clear bipolar variations in Y and Z field components can be explained by the eastward
 161 propagation of this equatorward (southward for IMAGE) current. At the -5 min time moment
 162 (Figure 3a) the current is on the west side from the station, at the +5 min time moment the
 163 current propagates eastward and appears on the right side. We show this propagation
 164 schematically in Figure 3c. Note that time goes to the left on the sketch, i.e. opposite to that in
 165 the observations.

166 The longer variation has no such straightforward and expected explanation, we interpret
 167 it as an equatorward expansion of the westward electrojet (WEJ). Decrease of B_x is caused by
 168 the approaching westward current and/or its intensity growth. The growth of B_z and its sign
 169 change from negative to positive denotes the equatorward propagating WEJ: at -30 min time
 170 moment the current was poleward from the station, at -10 min the current was located overhead
 171 or even passed further equatorward. Note that the effect in Figure 3a is only a qualitative
 172 estimate. The amplitude of the effect is about 30 nT but might be significantly higher (see Figure
 173 4 for example) for individual cases - the standard deviation of the field values observed within
 174 the ± 5 min time is about 50 to 60 nT.

175 In Figure 3b, the average time derivatives (dB/dt is expressed in nT per 10 seconds)
 176 reveal the presence of the omega effect even more clearly. Distinctive dB/dt signature stands out
 177 from the background noise within the ± 5 minutes of zero epoch time. Result in Figure 3b was
 178 obtained without any manipulations with the data, like background field subtraction, and should
 179 be considered as a more reliable evidence of the magnetic effect of the omegas. The mean
 180 amplitude of superposed time derivatives is about 1.0 to 1.5 nT/10 s, while the standard deviation
 181 of the observed values is about 4 nT/10 s. The most probable time to see the highest dB/dt is
 182 when the omega moves right over the observation site within ± 5 minutes of zero epoch time.
 183 Overall, omegas increase the probability of high dB/dt observation which is discussed in more
 184 detail in the next section.



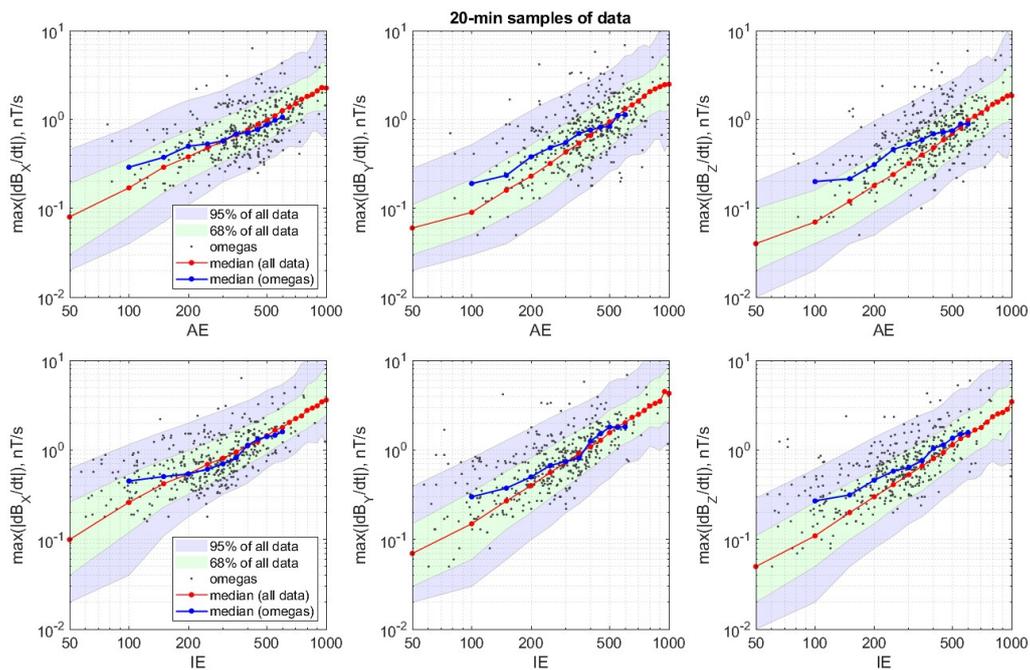
186 **Figure 4.** (a) Variations in the northward X (blue), eastward Y (red), and downward Z (black)
187 geomagnetic field components at the Kevo station from 02 to 03 UT, 30 January 1998. The
188 numbers in ASC images at the upper left corner correspond to the variations indicated with
189 numbers 1-4; omega #2 is from the list by Partamies et al. 2017. (b) time derivatives of the
190 magnetic field components.

191 An example of magnetic field variations at Kevo station on 30 January 1998 is shown in
192 Figure 4. This example from the analyzed list nicely corresponds to the signature revealed in
193 Figure 3a. P17 includes only one omega at 02:27 UT (omega #2 in Figure 4), while there are
194 certainly more omega signatures within ± 30 min interval. Four omega patterns are enumerated
195 below the local minima of Z component (black curve). The ASC images shown on the top panel
196 of Figure 4 confirm that each of these minima indeed corresponds to the auroral omega structure.
197 During this event, the train of the observed omegas produces the quasi-periodic pulsations with
198 5-10 min period, resembling the known Ps6 type of pulsations observed in Y and Z components
199 of the ground magnetic field in auroral zone and frequently accompanying omega bands (Saito,
200 1978; Gustafsson et al. 1981; Viljanen et al., 2001).

201 The amplitude of the magnetic effect from omegas 1-3 is about 50 nT for both Bx and By
202 - twice the amplitude of the superposed epoch result. These omegas occur within 20 minutes -
203 about 7 minutes for each omega. Figure 4b shows that the corresponding time derivatives are
204 about 5 nT/10 s. The biggest and brightest 4-th omega causes the largest variations. Magnetic
205 perturbation of about 150 nT corresponds to very high derivatives of about 10-15 nT/10 s in all
206 magnetic components. The dependence of magnetic derivatives from the area covered by omega
207 is investigated in Section 6.

208 3.2. Superposed geomagnetic variations

209 Omega structures may induce significant ground magnetic perturbations up to hundreds
210 of nanoteslas. In the omega band event on 29 June 2013 studied by Apatenkov et al. (2020), time
211 derivatives peaked at 15 nT/s (150 nT/10 s), which led to extremely high GIC in the power grid
212 >100 A. The omega structures in that event were relatively big $120\text{-}150\cdot 10^3$ km², as estimated
213 from DMSP satellite UV images, and fast 0.5-1.7 km/s. Yet it is interesting to estimate the
214 derivatives of the ground magnetic field caused by more regular omegas from the P17 list.



215

216 **Figure 5.** Comparison of the omegas' magnetic field derivatives (scatterplot and blue curve)
 217 with all derivatives in this sector (shaded areas and red curve) depending on AE (upper row) and
 218 IE (bottom row) activity indices. Blue curve indicates median values for the omegas $\max|dB/dt|$
 219 within the ± 50 nT window of the corresponding activity index. Shaded areas characterize
 220 distribution of maximum $|dB/dt|$ values for all 20-min samples of the corresponding magnetic
 221 data depending on AE/IE indices. Red curve shows the median and shaded blue and green areas
 222 show 2.5-97.5% and 16-84% quantiles for all observed values of $\max|dB/dt|$ in this sector.

223 In Figure 5, we show maximum $|dB/dt|$ values (black dots) calculated from the 10-s
 224 magnetic observations within ± 10 minutes of the average time when omega was seen at the ASC.
 225 The derivatives are placed against two geomagnetic indices (averaged within the analyzed 20
 226 min samples) measuring the auroral disturbance: (1) global auroral electrojet AE index (Davis
 227 and Sugiura, 1966) which is calculated from the perturbations of H component at auroral
 228 observatories covering most of longitude sectors, and (2) local IE electrojet indicator (Partamies
 229 et al., 2015) which is calculated in the same way but for IMAGE magnetometer network only.
 230 Blue curves indicate median values of maximum $|dB/dt|$ in the ± 50 nT moving window. Clearly,
 231 higher $|dB/dt|$ in all three components of the geomagnetic field correspond to disturbed periods,
 232 i.e. to higher AE and IE indices (note the logarithmic scale of both horizontal and vertical axes).

233 The effect of the omegas on the ground dB/dt can be estimated by comparing with the
 234 distribution of maximum $|dB/dt|$ values in arbitrary 20-min samples from IMAGE network
 235 selected for the similar to omega conditions. For this, we restrict the time to 1997-2006 and
 236 magnetic local time to 01-05 MLT, i.e. corresponding to the time when the analyzed omegas
 237 from the P17 list were observed. In Figure 5, the distribution of maximum $|dB/dt|$ values in
 238 arbitrary 20-min samples are characterized by the median value, calculated in ± 50 nT moving
 239 window (red curve), and four quantile levels, indicating 2.5, 16, 84, and 97.5 % of all data

240 within the window. Area between 2.5 and 97.5% is shaded blue. Area between 16 and 84% often
 241 related to \pm one standard deviation for the normal distribution is shaded green.

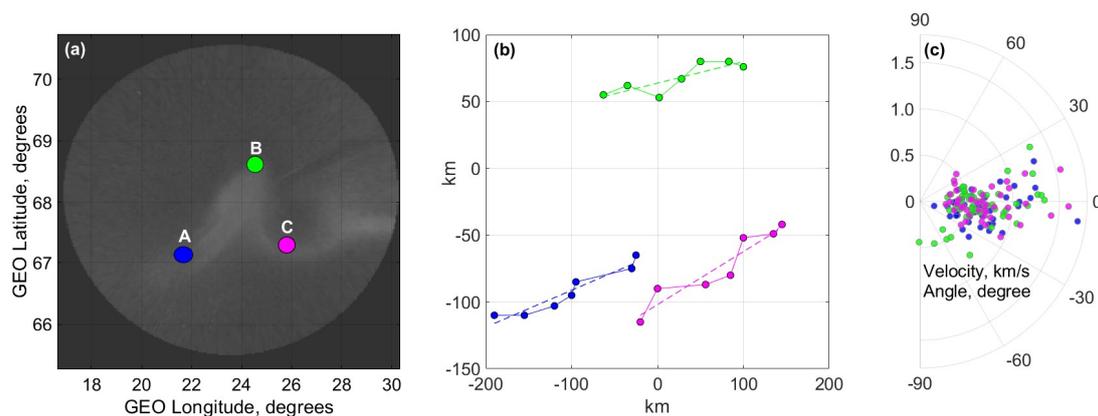
242 Figure 5 reveals that for the same activity level, drifting omega structures produce faster
 243 changes in the ground magnetic field, specifically in the Y and Z components. Higher $|dB/dt|$
 244 derivatives for omegas, as compared to baseline values obtained within 20-min samples, are
 245 more often observed during low and moderate geomagnetic activity below 250(200) nT for
 246 AE(IE) for Bx component, below 400(300) nT for By component, and below 500(600) nT for Bz
 247 component. Median values of the maximum $|dB/dt|$ for these ranges of AE and IE indices are on
 248 average 0.1-0.2 nT/s higher, which is 50-100% higher than the baseline derivatives. Therefore,
 249 even regular omegas of small size (fit in the ASC field of view) on average lead to faster changes
 250 of the ground geomagnetic field.

251 3.3. Omega motion

252 The drift of the omega bands can be investigated from the auroral observations. The all-
 253 sky cameras have 20 second cadence, so the majority of omegas from the P17 list were observed
 254 at several sequential frames during 1-15 minutes. To track the omega motion, we select three
 255 specific points connected to the omega shape, namely (A) western bottom, (B) top point and (C)
 256 eastern bottom (Figure 6a). We admit this is subjective, however, the formal method has not
 257 been invented yet to our knowledge.

258 We also note the raw ASC images were mapped to the ionosphere assuming constant 118
 259 km altitude. Near horizon pixels, 70-90 degrees from zenith, were removed as they bear large
 260 uncertainties. The mapping procedure described in Syrjasuo (1996) transforms auroral ASC
 261 images into rectangular coordinates.

262 An example of point selection for omega tracking is shown in Figure 6a by blue, green,
 263 and purple circles corresponding to the previously described A, B, and C points. We assume the
 264 constant velocity for each point, allowing the velocities V_A , V_B , V_C to be different. The time
 265 sequence of point locations $X(t)$ is fitted by linear function. This is done independently for X,
 266 northward, and Y, eastward, coordinates. So, we find V_X and X_0 in the set of equations $X(t_i)$
 267 $=V_X t_i + X_0$. The same is done for V_Y and Y_0 .



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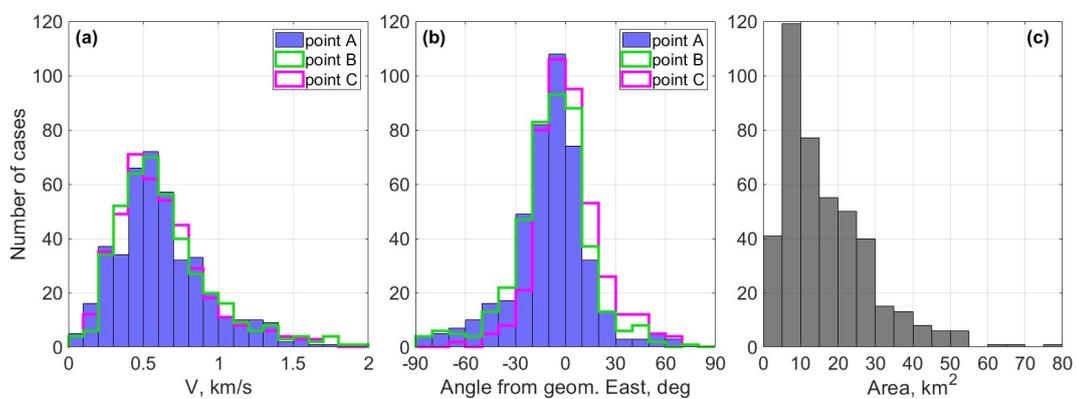
269 **Figure 6.** (a) Example of ASC image taken at Muonio on 11 January 2002 at 01:26 UT and three
 270 reference points for the analysis of omega velocity and area. (b) linear fit of the coordinates of

271 each point corresponding to consecutive images of this omega. (c) polar plot for the angles and
 272 velocities obtained for the omegas observed at Muonio. Zero direction is the geomagnetic East.

273 The fitting results are shown in Figure 6b. The dashed lines correspond to the coordinates
 274 obtained from the constant velocity approach. The velocities for points A, B, and C in this case
 275 slightly differ from each other. $V_A = (V_{AX}, V_{AY}) = (0.18, 0.68)$, $V_B = (0.10, 0.72)$, $V_C = (0.31,$
 276 $0.73)$ km/s. To simplify reading and analysis, we further present velocity absolute value and its
 277 direction as the angle (in degrees) with respect to the geomagnetic East (positive is
 278 counterclockwise). The difference between geomagnetic and geographic East is about 11
 279 degrees. The (V_{AX}, V_{AY}) values from example above transform to $(|V|, \text{angle})$ values, giving V_A
 280 $= (0.70, 3.5)$, $V_B = (0.73, -3.5)$, $V_C = (0.79, 11.8)$.

281 In total we managed to track 433 omega structures based on the P17 list (60 for ABK, 77
 282 for KEV, 105 for KIL, 61 for MUO, and 130 for SOD). The resulting velocities and angles are
 283 summarized in Figure 6c for Muonio station and Figure 7 for all five sights. Figure 6c and Figure
 284 7(a,b) demonstrate that the speeds are in the 0.2-2 km/s range, the majority of the directions are
 285 within the -30 to +30 degrees sector from the geomagnetic East, the main direction is definitely
 286 eastward. The most probable speed values are in 0.2-0.8 km/s range that is in good agreement
 287 with previous case studies papers (e.g. Opgenoorth et al., 1983). We did not observe any
 288 significant difference between the distributions at any particular station; indeed, all ASC are at a
 289 very narrow range of the magnetic latitudes.

290 There is a visual tendency that the omega velocity distribution is shifted slightly
 291 equatorward. The histograms of angle and speed distributions are presented in Figure 7a-b. The
 292 equatorward motion tendency is confirmed in Figure 7b, there are more omegas moving slightly
 293 equatorward (negative values of the angle) than poleward in addition to main eastward
 294 propagation. This equatorward drift can be related either to (1) earthward motion of the
 295 magnetospheric source or (2) to the overall expansion of the polar cap and the auroral oval
 296 during the substorm development. It is worth noting that if the first statement is correct, then this
 297 subtle north-south shift in the distribution of ionospheric velocities can lead to a significant radial
 298 velocity of the magnetospheric source. Indeed, in a recent study by Andreeva et al. (2021), the
 299 same set of omega cases was magnetically mapped to the equatorial magnetosphere. They
 300 showed that the magnetospheric counterpart statistically has the radial velocity component of
 301 several tens of km/s, which is comparable to the velocity in the azimuthal direction.



303 **Figure 7.** Distributions of omegas velocity (a), angle from geomagnetic East (b), and area (c).

304 In addition to velocity, we provide rough estimation of the area covered by an omega
 305 shown in Figure 7c. We use triangles constructed from the points A, B and C (Figure 6a) to
 306 calculate this area. The average area during the omega passage is further considered. The area
 307 has values in the range 2-80·10³ km² with the mean value 18·10³ km². Note, the upper limit for
 308 the omegas' area is instrumentally limited by the size of the ASC field of view in our study. The
 309 much larger omegas have been observed by spaceborne imagers. For example, we estimate the
 310 omega area from DMSP/SSUSI observations describes by Apatenkov et al. (2020) as 120-
 311 150·10³ km².

312 3.4. Dependence on omega velocity and area

313 In order to analyse how time derivatives of the ground magnetic field depend on omega
 314 velocity, we consider 433 cases with tracked omegas. As a very rough assumption, we can
 315 estimate the relation between ground magnetic field and velocity and area of omegas by
 316 considering a linear X-directed equivalent current J_X moving in Y direction above the station.
 317 This current may be roughly interpreted as a poleward directed Hall current between two vortices
 318 of equivalent currents, associated with each individual omega. Time variation of the magnetic
 319 field B in a fixed point on the ground induced by a moving horizontal wire with current J_X
 320 (directed strictly northward) in the ionosphere is given by the expression following Biot-Savart
 321 law:

$$322 \quad B(t) = \frac{\mu_0 J_X}{2\pi\sqrt{(H^2 + V^2 t^2)}}, \quad (\text{Eq 1})$$

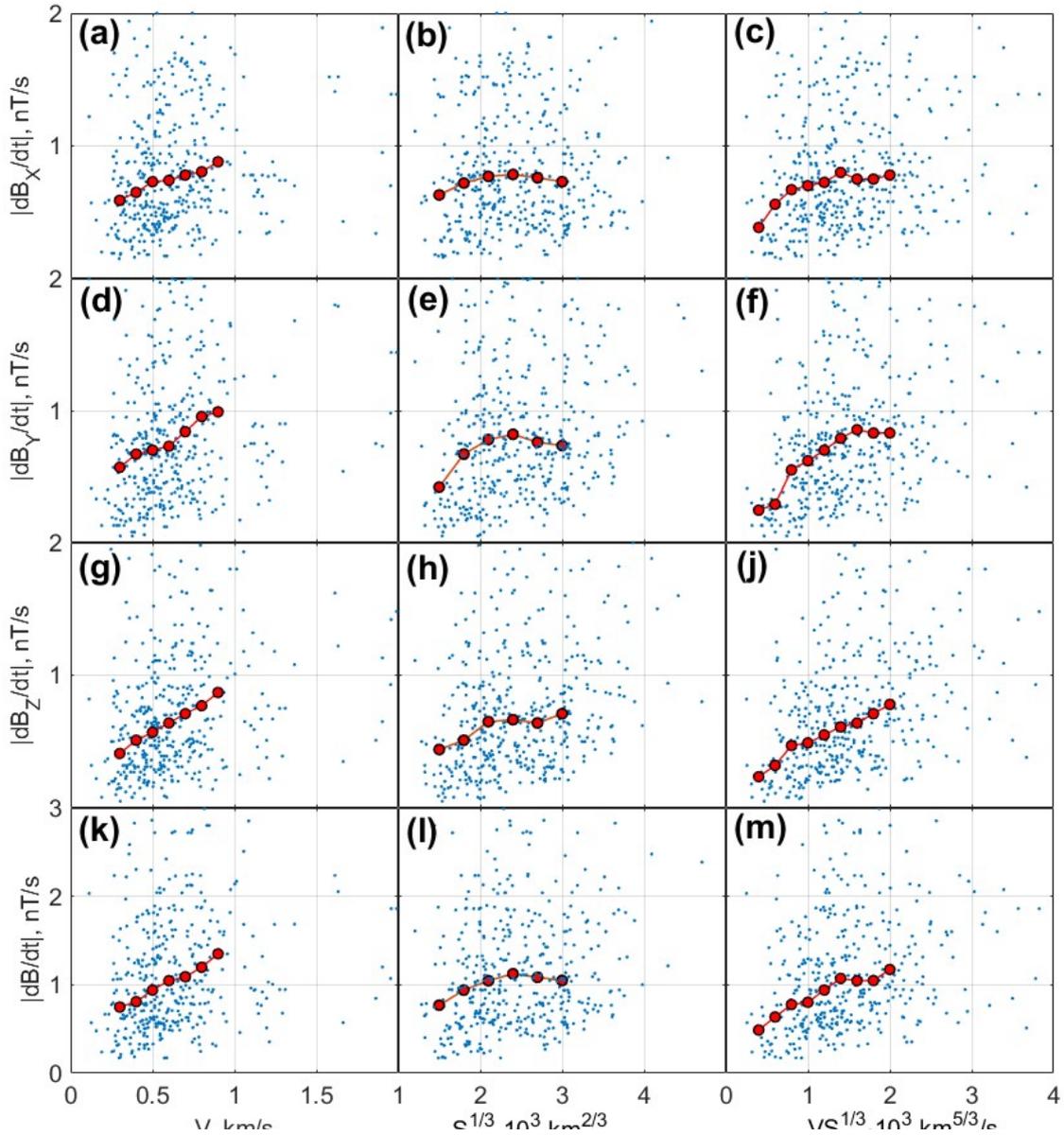
323 where H - altitude of the equivalent currents (110 km), V - velocity of the current moving
 324 in Y direction, t - time from the omega peak (when the current is right above the station). In
 325 assumption of constant J_X and V , we obtain the time derivative for $B(t)$:

$$326 \quad \frac{dB}{dt} = \frac{\mu_0 J_X V^2 t}{2\pi\sqrt{(H^2 + V^2 t^2)}^3}, \quad (\text{Eq 2})$$

327 In order to get an expression for the maximum time derivative of the induced magnetic
 328 field, we find the root of the equation $(dB/dt)'=0$ and substitute it to the Eq 2:

$$329 \quad \left(\frac{dB}{dt}\right) = \frac{\mu_0 J_X V}{3\pi\sqrt{3}H^2}, \quad (\text{Eq 3})$$

330 Equation 3 indicates the linear dependence of maximum dB/dt on the omegas' velocity.
 331 Figures 8(a,d,g,k) show maximum values of time derivatives in 20 min intervals in X (a), Y (d),
 332 Z (g) components of the geomagnetic field and its magnitude (k) versus the omegas' velocity
 333 (first column). Despite the large spread the tendency for higher dB/dt occurrence during higher
 334 velocities is clearly seen, especially in the median values (red circles) for the corresponding
 335 ranges of V . Dependence is roughly linear, as predicted by Equation 3.



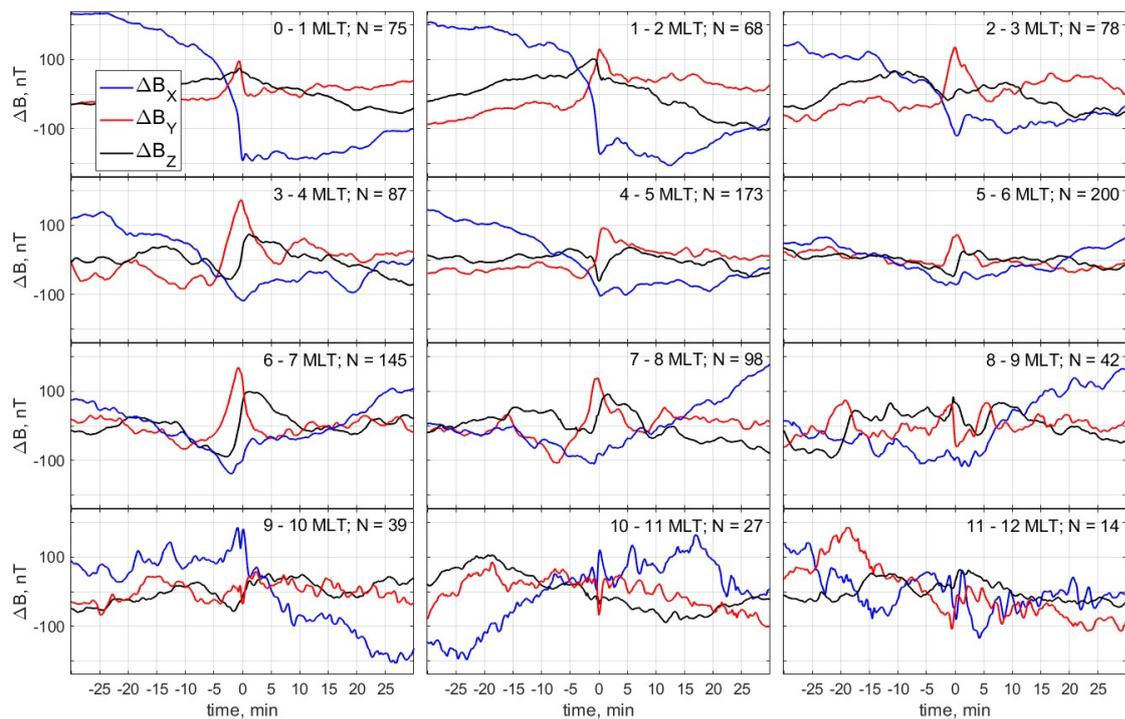
336

337 **Figure 8.** Maximum values of $|dB/dt|$ in X (a-c), Y (d-f), and Z (g-j) geomagnetic field
 338 components and their magnitudes (k-m) depending on the omegas' velocity (first column), area
 339 $S^{1/3}$ (second column), and $VS^{1/3}$ (third column). Red circles denote median values for the
 340 corresponding ranges of V , S , and $VS^{1/3}$.

341 Here, we also investigate how dB/dt may depend on the area covered by the bright part of
 342 the omega (second column, Figure 8(b,e,h,l)). The logic behind it is that larger structures may be
 343 associated with stronger currents. Although this relation is weaker than for velocity, we still can
 344 see an increase in median dB/dt values. We also found that the relation is better between dB/dt
 345 and a product of velocity and area, where area is in the $1/3$ degree (third column, Figure
 346 8(c,f,j,m)). These figures indicate that faster and larger omegas provide higher time derivatives
 347 of the surface magnetic field.

348 **4 Discussion**

349 In the previous sections, we show that omegas from the P17 list are sources of increased
 350 time derivatives of the ground magnetic field (Figure 5). The analyzed omegas are restricted in
 351 size by a 2.8105 km^2 circle area covered by the ASC field of view at 118 km altitude. For the
 352 P17 list, the largest area of a triangle formed by A, B, and C points is about 0.8105 km^2 , one
 353 third of the camera's field of view. Larger omegas cannot be tracked using ASCs. Besides, P17
 354 list is a small fraction of the variety of omegas and lacks a representative set of extreme cases
 355 (big/fast/faint omegas).



356

357 **Figure 9.** Superposed magnetic variations observed on five Fennoscandia stations with zero time
 358 for the cases with $|\text{dB}/\text{dt}| > 10 \text{ nT/s}$. Number of cases and MLT sectors are shown in each panel.

359 Apatenkov et al. (2020) show that large scale omega bands can be responsible for
 360 extremely high dB/dt values up to 15 nT/s . Using the same 10s magnetic data of five stations
 361 during 1996-2018, we search for the time when $|\text{dB}/\text{dt}|$ was greater than 10 nT/s .

362 In order to find unique cases, we select only those that are separated by at least one hour.
 363 This gives over 1715 cases for five stations (1046 in 00-12 MLT and 669 in 12-24 MLT). In
 364 Figure 9, the corresponding variations were superposed like in Section 3 with zero time being the
 365 time of maximum $|\text{dB}/\text{dt}|$. The results are shown separately for each hour within the 00-12 MLT
 366 sector. The interesting finding is that the omega-like magnetic signatures (Section 3, Figure 3a)
 367 are clearly observed in the 03-08 MLT sector: negative to positive B_y change near zero epoch
 368 time and the same change in B_z several minutes after.

369 Note also, that this MLT sector is characterized by the largest number of cases with
 370 $|\text{dB}/\text{dt}| > 10 \text{ nT/s}$. This is similar to the Ps6 pulsation occurrence distribution (Rostoker and

371 Barichello, 1980) with maximum in 04-06 MLT. Thus, we speculate that a significant part of the
372 extreme ground dB/dt events at auroral latitudes might be associated with the passage of the
373 omega bands, in agreement with Apatenkov et al. (2004).

374

375 **5 Conclusions**

376 In this study, we estimate the ground magnetic effect produced by the omega auroral
377 structures. The list provided by Partamies et al 2017 includes 438 omegas observed by the ASCs
378 at the Fennoscandia region. The omegas from this list are highly versatile in form, size (limited
379 by the ASC field of view), velocity, and brightness.

380 Typical magnetic signature of the ground magnetic perturbation due to omegas was
381 estimated using superposed epoch analysis. We found that the typical magnetic variation has a
382 short time signature: depression of the Z and bipolar variation of the Y geomagnetic field
383 components within ± 5 minutes of the omega peak time (when the omega is above the site of the
384 magnetic observations). This reflects the eastward propagation of the WEJ mesoscale bend
385 which has almost north-south directed segments. The variations at the longer time scale, from 30
386 to 0 minutes before omega peak time, probably denote equatorward expansion of the WEJ which
387 is seen in gradual decrease of X and increase of Z geomagnetic field components. This kind of
388 WEJ behavior usually indicates the global convection growth or substorm expansion.

389 The moving current system associated with omega causes high dB/dt at the Earth's
390 surface. We found that on average the appearance of omega structures increases the rate of
391 change in the surface magnetic field by 50 to 100% for moderate geomagnetic activity level, as
392 compared to all dB/dt in the morning sector.

393 We also track omega bands using three reference points manually selected on the ASC
394 images and obtain their average velocities, directions and areas. The velocity range is 0.2-2 km/s
395 with the average value of 0.7 km/s. The directions range from -30 to +30 degrees from the
396 geomagnetic East with the average value of -6 degrees (to the South) indicating small
397 equatorward motion.

398 Linear dependence was found between dB/dt and omega velocity, verifying that faster
399 omegas induce higher dB/dt on the ground. Although the omega size seems to have a weaker
400 effect on dB/dt, the product of the velocity and area shows better correlation than with only
401 velocity.

402 Moreover, it was found that the highest dB/dt values observed at the Fennoscandia region
403 in 1996-2018 within 03-08 MLT sector resemble the omega magnetic signatures. Extremely
404 big/intense/fast omega bands therefore might be responsible for the fast changes of the ground
405 magnetic field and thus triggering the formation of intense GIC.

406

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414 The MIRACLE data could be requested at <https://space.fmi.fi/MIRACLE/>. The list of
415 omega events from Partamies et al. (2017) is available at <http://doi.org/10.5281/zenodo.4541669>.

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422

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