

1 **Climatology of marine shallow-cloud-top radiative cooling**

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9 10 11 **Main points:**

- 12 • A one-year's worth of global marine shallow single-layer cloud-top radiative cooling
13 (CTRC) is derived from satellite and reanalysis data.
- 14 • Spatial and seasonal variations of CTRC are largely reflections of changes in free-
15 tropospheric humidity.
- 16 • A neural network model for the CTRC was trained, which substantially speeds up the
17 retrieval while maintaining good accuracy.

32 **Abstract**

33 A one-year's worth of global (except poleward of 65 ° N/S) marine shallow single-layer cloud-top
34 radiative cooling (CTRC) is derived from a radiative transfer model with inputs from the satellite
35 cloud retrievals and reanalysis sounding. The mean cloud-top radiative flux divergence is 61 Wm⁻²,
36 decomposed into the longwave and shortwave components of 73 and -11 W m⁻², respectively.
37 The CTRC is largely a reflection of free-atmospheric specific humidity distribution: a dry
38 atmosphere enhances CTRC by reducing downward thermal radiation. Consequently, the cooling
39 minimizes in the “wet” tropics and maximizes in the “dry” eastern subtropics. Poleward of 30 °
40 N/S, the CTRC decreases slightly due to the colder clouds that emit less effectively. The CTRC
41 exhibits distinctive seasonal cycles with stronger cooling in the winter and has amplitudes of order
42 10~20 Wm⁻² in stratocumulus-rich regions. The datasets were used to train a machine-learning
43 model that substantially speeds up the retrieval.

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45 **Plain Language Summary**

46 Marine low-lying clouds cool the Earth by reflecting incoming sunlight, thus crucially important
47 for the Earth's climate. Marine low clouds cool by emitting thermal radiation. The cooling is
48 known as cloud-top radiative cooling (CTRC). A change in CTRC can influence the properties of
49 marine clouds via many avenues, ranging from altering the vertical motions of the clouds to
50 changing the clouds' ability to reflect sunlight. Despite the importance of CTRC to the climate
51 system, its climatological characteristics, namely how it varies with space and time, remain
52 unknown. This work fills this knowledge gap. We generate the product of the CTRC over the
53 global ocean using a novel satellite methodology developed in our previous work. Analyses of the
54 data show that the spatial and temporal distributions of the CTRC are largely reflections of the
55 atmospheric humidity: the drier the atmosphere, the stronger the cooling. As a result, the CTRC
56 maximizes in the wet tropics and minimizes in the dry eastern subtropical ocean such as the west
57 of California. We also use the CTRC data to train a machine-learning algorithm that can
58 substantially speed up the calculation of CTRC.

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68 **1. Introduction**

69 Marine shallow clouds (MSC) are crucially important to the Earth's climate because they
70 affect both energy and water cycles. MSC cloudiness is dominated by stratocumulus decks
71 sustained by the convection driven by cloud-top radiative cooling (CTRC). An increase in CTRC
72 destabilizes the stratocumulus-topped boundary layer, driving more intense convective circulation
73 that substantially alter the cloud and radiative properties via many avenues (Lilly, 1968; Dearnorff,
74 1976; Nicholls, 1984; Austin et al., 1995; Bretherton and Wyant, 1997; Stevens, 2002; Caldwell
75 et al., 2005; Bretherton et al., 2007; Zheng et al., 2016, 2018; Zhou and Bretherton, 2019). These
76 influences make the CTRC a crucial player in understanding the low cloud feedback, a major
77 source of uncertainty for climate projections (Bony and Dufresne, 2005). For example, as the
78 planet warms, the CTRC will weaken due to the enhanced down-welling thermal radiation in a
79 more opaque atmosphere. The reduced CTRC, via weakening the boundary layer convection, thins
80 the stratocumulus decks, leading to positive low cloud feedback. Representations of CTRC in the
81 global climate models (GCMs) are poor because the cooling typically concentrates near the top
82 several tens of meters of the cloud layer, which the GCMs cannot resolve. An improved
83 representation of CTRC in a modern higher-order turbulence closure scheme in GCMs (Larson et
84 al., 2012) can markedly improve the GCM simulations of low clouds (Guo et al., 2019).

85 Despite the fundamental importance of CTRC, its observations have been scarce. Typical
86 approaches are direct observations of radiative fluxes from aircraft (Bretherton et al., 2010b) or
87 tethered balloon (Slingo et al., 1982) and indirect calculations with a radiative transfer model
88 (RTM) with inputs from field campaign measurements (Nicholls and Leighton, 1986; Wood, 2005;
89 Ghate et al., 2014; Zheng et al., 2016). The ensuing CTRC data are inherently highly limited in
90 spatial and temporal coverage. Active satellite sensors have been used to estimate the radiative
91 fluxes in the cloudy atmosphere using a radiative transfer model (L'Ecuyer et al., 2008; Haynes et
92 al., 2013), but the vertical resolution is too coarse (240 m) to resolve the CTRC that takes place
93 chiefly near the upper several tens of meters in MSC. A systematic analysis of the CTRC
94 climatology over the global ocean is still lacking.

95 This study aims to fill the knowledge gap of CTRC climatology. This work builds upon our
96 previous work by Zheng et al. (2019) who proposed a new remote sensing approach for retrieving
97 the CTRC with passive satellite data. This new methodology calculates the CTRC using an RTM
98 with inputs from satellite-derived cloud properties and reanalysis sounding corrected by satellite-
99 retrieved cloud-top temperature. Here we used the method to generate a full year of MSC CTRC
100 product from the Moderate Resolution Imaging Spectroradiometer (MODIS) onboard the National
101 Aeronautics and Space Administration Aqua and Terra satellites. The data were used in two ways:
102 studying the CTRC climatology and training a machine learning model to speed up the retrieval.

103 The paper is organized as follows: Section 2 introduces satellite data and the algorithm of
104 CTRC retrieval. Section 3 provides a theoretical background of the environmental dependence of
105 CTRC, paving the ground for the subsequent analyses. Section 4 analyzes the climatology of
106 CTRC in terms of spatial and temporal variabilities. Section 5 shows the machine learning of
107 CTRC and its evaluations, followed by the conclusion in Section 6.

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110 2. Data and Methodology

111 2.1.Data

112 Cloud properties are obtained from the MODIS Terra/Aqua Level-1 (MxD06) and Level-2
113 (MxD06_L2) cloud product collection 6.1 (Platnick et al., 2015) over the global ocean in 2014.
114 Each MODIS swath was divided into multiple 110 by 110 km scenes ($\sim 1^\circ$ by 1° at the equator).
115 The criteria for scene selection are the same as our previous works (Rosenfeld et al., 2019; Cao et
116 al., 2021). Scenes with single-layer liquid water clouds with cloud geometrical thickness thinner
117 than 800 m were selected. In each scene, the retrieved cloud optical depth, cloud droplet effective
118 radius, and cloud top temperature are averaged over cloudy pixels. Scenes poleward of 65° N or
119 S are excluded to avoid the known problems of cloud retrievals for high solar zenith angle
120 (Grosvenor and Wood, 2014). A total of ~ 6 million valid scenes were collected.

121 Vertical profiles of temperature and humidity are obtained from the National Centers for
122 Environmental Prediction reanalysis data (Kalnay et al., 1996). The sea surface temperature (T_s)
123 data are from the National Oceanic and Atmospheric Administration (Reynolds et al., 2007). The
124 reanalysis and T_s data are interpolated into the geographical center and time of each satellite scene.

125 2.2.Retrieval algorithm

126 We provide a high-level introduction of this algorithm to elucidate the fundamental concepts
127 (Zheng et al., 2019). The retrieval relies on an RTM (see text S1) with inputs from satellite-
128 retrieved cloud parameters in combination with the reanalysis sounding. The key merit of this
129 algorithm is the revision of the original reanalysis profiles. It is well known that reanalysis data
130 fail to capture the sharp inversion layer topping MSC. This causes large errors in the simulated
131 radiative fluxes across the cloud top that are particularly sensitive to temperature inversion. We
132 tackled this challenge by revising the reanalysis sounding in a physically coherent way. We use
133 the satellite-retrieved cloud-top temperature to reconstruct the inversion-layer sounding by
134 assuming a 100% relative humidity in the cloud layer (see Zheng et al., 2019 for detail).

135 With inputs from the revised sounding and satellite-retrieved cloud parameters, the radiative
136 transfer model outputs the vertical profiles of radiative fluxes. We quantify the CTRC using the
137 divergence of net radiative flux across the cloud top, denoted as ΔF . The upper boundary for ΔF
138 is 100 m above the cloud top and the lower boundary is the height of the grid in the cloud layer
139 where the radiative cooling shifts to radiative warming as one goes down to the cloud base (there
140 is typically radiative warming layer near the cloud base). The ΔF has longwave (LW) and
141 shortwave (SW) components (ΔF_{LW} and ΔF_{SW}).

142 Because Terra/Aqua satellites have fixed overpasses time of approximately 1030 and 1330 h
143 local solar time, the simulated SW fluxes are biased toward the local time of observations when
144 the incoming solar insolation is substantially larger than the daily means. To mitigate such diurnal
145 bias, we follow L'Ecuyer et al. (2008) to correct the instantaneous SW flux by multiplying it by a
146 correcting factor defined as the ratio of the average top-of-atmosphere insolation for the scene's
147 latitude and Julian day to the instantaneous top-of-atmosphere insolation. Figure S1 shows the
148 probability density function (PDF) of the instantaneous ΔF_{SW} (red) and corrected daily mean ΔF_{SW}
149 (green). The daily mean ΔF_{SW} is considerably smaller and more narrowly distributed than the
150 instantaneous ΔF_{SW} , consistent with expectation. In the remainder of the manuscript, the ΔF_{SW}
151 refers to the daily mean ΔF_{SW} unless otherwise noted.

152 Note that the ΔF represents cooling averaged over cloudy pixels of a satellite scene and there
 153 is no contribution from the cloud-free area. In other words, the cloudiness does not directly
 154 influence the ΔF . This is important to keep in mind because some studies refer to the CTRC as the
 155 average of all pixels, both clear and cloudy (Bretherton et al., 2010a; Vial et al., 2016). Such an
 156 all-sky CTRC is not our focus although it will be discussed in Section 4.3.

157 Aerosols are not included in the calculations because of the lack of aerosol vertical information
 158 from passive sensors. We consider it an insignificant issue, motivated by previous research
 159 showing the limited radiative role of aerosols compared with the influence of atmospheric
 160 thermodynamics (Haynes et al., 2013; Henderson et al., 2013).

161 3. Conceptual background: what determines the CTRC?

162 To assist with interpreting the climatology analysis, we briefly discuss what drives the
 163 changes in ΔF_{SW} and ΔF_{LW} using simple illustrative formulas. The ΔF_{LW} for a single-layer cloud
 164 can be approximated as:

$$165 \quad \Delta F_{LW} \approx \varepsilon_c \sigma T_c^4 - \varepsilon_a \sigma T_a^4, \quad (1)$$

166 where ε , σ , and T are the emissivity, the Stefan-Boltzmann constant, and emission temperature,
 167 respectively. The subscripts “c” and “a” stand for the cloud and the above-cloud atmosphere,
 168 respectively. The ΔF_{LW} is typically positive, meaning a divergence of radiative flux and thus a
 169 cooling. Given the small variability of T_c/T_s (Figure S2) due to low altitudes of MSC, Eq. (1) can
 170 be simplified to:

$$171 \quad \Delta F_{LW} \approx \sigma T_s^4 \times \left(\varepsilon_c - \varepsilon_a \frac{T_a^4}{T_s^4} \right), \quad (2)$$

172 For SW, we use the Schwarzschild equation to derive an illustrative formula for ΔF_{SW} :

$$173 \quad \Delta F_{SW} \approx S \times e^{-\tau_a} \times (1 - e^{-\tau_c}), \quad (3)$$

174 where S stands for the incoming SW radiative flux at the top of the atmosphere, which is negative.
 175 τ is a bulk measure of an atmospheric layer’s ability to absorb SW energy (i.e. SW optical depth).
 176 In a clear atmosphere, its primary contribution is primarily from the water vapor whereas in a
 177 cloudy layer both cloud droplets and water vapor contribute (Li and Moreau, 1996). Note that the
 178 equation is a simplified formula for an illustrative purpose only.

179 Equations 2 and 3 show several important CTRC-controlling factors. The first is the optical
 180 thickness of the free atmosphere. For LW, an optically thicker free atmosphere enhances the
 181 emissivity (ε_a), thereby increasing the downward radiative flux. This decreases the cooling. In the
 182 atmosphere, water vapor is the most important absorber so a more humid atmosphere favors
 183 weaker cloud-top LW cooling. For SW, a humid free atmosphere absorbs more incoming solar
 184 radiation (a smaller $e^{-\tau_a}$), leaving less energy for the cloud to absorb (Davies et al., 1984). So
 185 humid atmosphere weakens cloud absorption of SW radiation. This compensates for the reduced
 186 LW cooling.

187 The second CTRC-controlling factor is the cloud liquid water path (LWP). In the LW, the ε_c
188 increases with the LWP (Pinnick et al., 1979) so that the LW cooling is larger for thicker clouds
189 (Zheng et al., 2016; Zheng et al., 2019). The degree of dependence is large for thin clouds with
190 LWP $< 50 \text{ g m}^{-3}$ and saturates afterward (Kazil et al., 2017). In the SW, the solar absorption also
191 increases with the LWP (Stephens, 1978). A large LWP typically corresponds to a more humid
192 layer, thereby enhancing the solar absorption due to the high concentration of water vapor. As a
193 result, the ΔF_{SW} must increase with LWP. This, again, leads to a cancelation for the net CTRC.
194 The cloud droplet effective radius also alters CTRC but its contribution is much smaller (Zheng et
195 al., 2019).

196 Another two factors are the σT_s^4 and S . We discuss them together because they are highly
197 correlated in nature. Climatologically speaking, more solar insolation corresponds to warmer sea
198 surfaces to maintain radiative balance. This holds in both spatial (zonal-mean meridional
199 distribution) and temporal (seasonal cycle) senses.

200 In summary, to the first order, the CTRC variation can be explained from four factors: the
201 free-atmospheric humidity, LWP, σT_s^4 and S . The climatological co-variation of the last two
202 factors can reduce the number of influential factors to three.

203 4. Result

204 The CTRC product shows that the ΔF , ΔF_{LW} , and ΔF_{SW} have means of 61 W m^{-2} , 73 W m^{-2} ,
205 and -11 W m^{-2} , respectively (Fig. S1). The ΔF PDF is similar to that of ΔF_{LW} , but with weaker
206 cooling and less variability due to the compensation by ΔF_{SW} . Below we analyze the CTRC
207 climatology in terms of spatial (Sect. 4.1) and temporal (Sect. 4.2) variations.

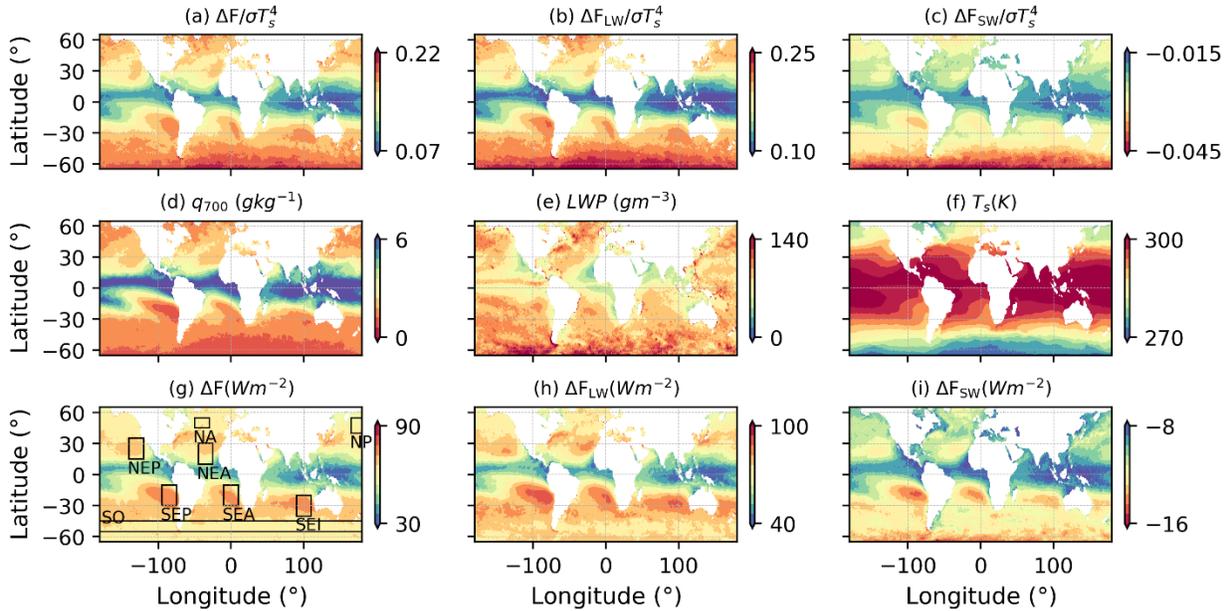
208 4.1. Annual mean

209 Figure 1 a~c show the annual-mean ΔF scaled by the σT_s^4 and its LW and SW components.
210 The scaling temporarily frees us from considering the roles of T_s and, to a great extent, S . The σT_s^4 -
211 scaled ΔF , ΔF_{LW} , and ΔF_{SW} share a similar spatial pattern: a strong latitudinal dependence with the
212 weakest cooling (or heating) in the tropics and the strongest in the extra-tropics, regional peaks in
213 the eastern subtropics adjacent to the major continents, and hemispheric asymmetry with stronger
214 cooling/heating in the Southern Hemisphere.

215 Such a spatial pattern can be well explained by the free atmospheric humidity. The specific
216 humidity at 700 hPa (q_{700}) (Fig. 1d) highly resembles the σT_s^4 -scaled CTRC variables in terms of
217 the spatial pattern. This is consistent with the theoretical argument that drier free atmosphere
218 enhances the cloud-top LW cooling by weakening the down-welling thermal radiation (Fig. 1b)
219 and strengthens the cloud-top SW heating by increasing the exposure of clouds to solar insolation
220 (Fig. 1c). The reduced SW heating compensates for the LW cooling, but because the magnitude of
221 the ΔF_{SW} is considerably smaller than the ΔF_{LW} , the net effect, ΔF , largely follows the ΔF_{LW} .

222 The LWP contributes little. Over most regions, the climatological LWP is large enough ($>$
223 50 gm^{-3}) that the sensitivity of ΔF_{LW} to the LWP already saturates (Zheng et al., 2016; Kazil et al.,
224 2017). The most illustrative example is the tropical eastern Pacific Ocean where there is a band of
225 high LWP. The local LWP peak is caused by the strong convective activities that also moisten the
226 free atmosphere, leading to large q_{700} . The two factors oppositely change the ΔF . The pattern of

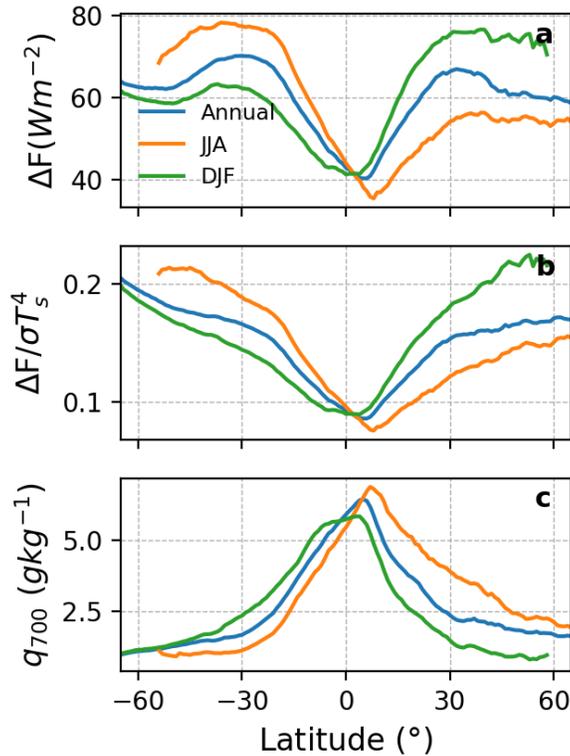
227 $\Delta F/\sigma T_s^4$ and its components still follows the q_{700} whose influences dominate over the LWP. There
 228 are some footprints of LWP on the local variability of $\Delta F_{SW}/\sigma T_s^4$ such as the scattered blobs and
 229 bands of red colors in the southern part of the Southern Oceans, but the overall spatial pattern of
 230 the scaled $\Delta F/\sigma T_s^4$ is a reflection of the free-tropospheric humidity.



231
 232 Figure 1: Global distribution of annually-averaged cloud-top radiative cooling scaled by σT_s^4 (a),
 233 its LW (b) and SW components (c), specific humidity at 700 hPa (d), liquid water path (e), sea
 234 surface temperature (f), and cloud-top radiative cooling (g) and its LW (h) and SW components
 235 (i). In (g), black rectangles mark regions with persistent low clouds and the locations are adopted
 236 from Klein and Hartmann (1993), with slight modifications of limiting regions within 55 °N/S to
 237 avoid seasonal sampling bias.

238 Having known the ability of free-tropospheric humidity in explaining the $\Delta F/\sigma T_s^4$, we now
 239 look at the ΔF (bottom panel of Figure 1). The pattern is overall similar to the $\Delta F/\sigma T_s^4$ in the
 240 tropical regions where the variation of T_s is not large enough to alter the ΔF feature. The influence
 241 of σT_s^4 is most distinctive in the extratropical regions where the low solar zenith angle and the cold
 242 sea surface considerably weaken the SW heating and LW cooling, respectively, despite the bands
 243 of maximums in the southern flank of the Southern Ocean likely due to the large LWP. As a result,
 244 the peaks of ΔF no longer concentrate in the extratropical oceans where the q_{700} is lowest but locate
 245 in the eastern subtropical basins where both the dry free atmosphere and the moderate sea surface
 246 favor the strong LW cooling.

247 The roles of q_{700} and σT_s^4 can be more clearly seen from the zonal-mean meridional
 248 distributions (Fig. 2). The annual-mean scaled CTRC (Fig. 2b) monotonously increases with the
 249 latitude, consistent with the q_{700} variation (Fig. 2c). Without the scaling of σT_s^4 , the CTRC starts
 250 to weaken poleward of $\sim 30^\circ$ N or S (Fig. 2a) due to the cold temperature. This leads to local
 251 maximums of ΔF in $\sim 30^\circ$ N or S where the downward branches of the Hadley circulation generate
 252 a very dry atmosphere and thus enhance LW cooling.



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255 Figure 2: Zonal-mean meridional variations of cloud-top radiative cooling (a), cloud-top
 256 radiative cooling scaled by σT_s^4 (b), and specific humidity at 700 hPa (c) for the annual mean
 257 (blue) and boreal summer (orange) and winter months (green).

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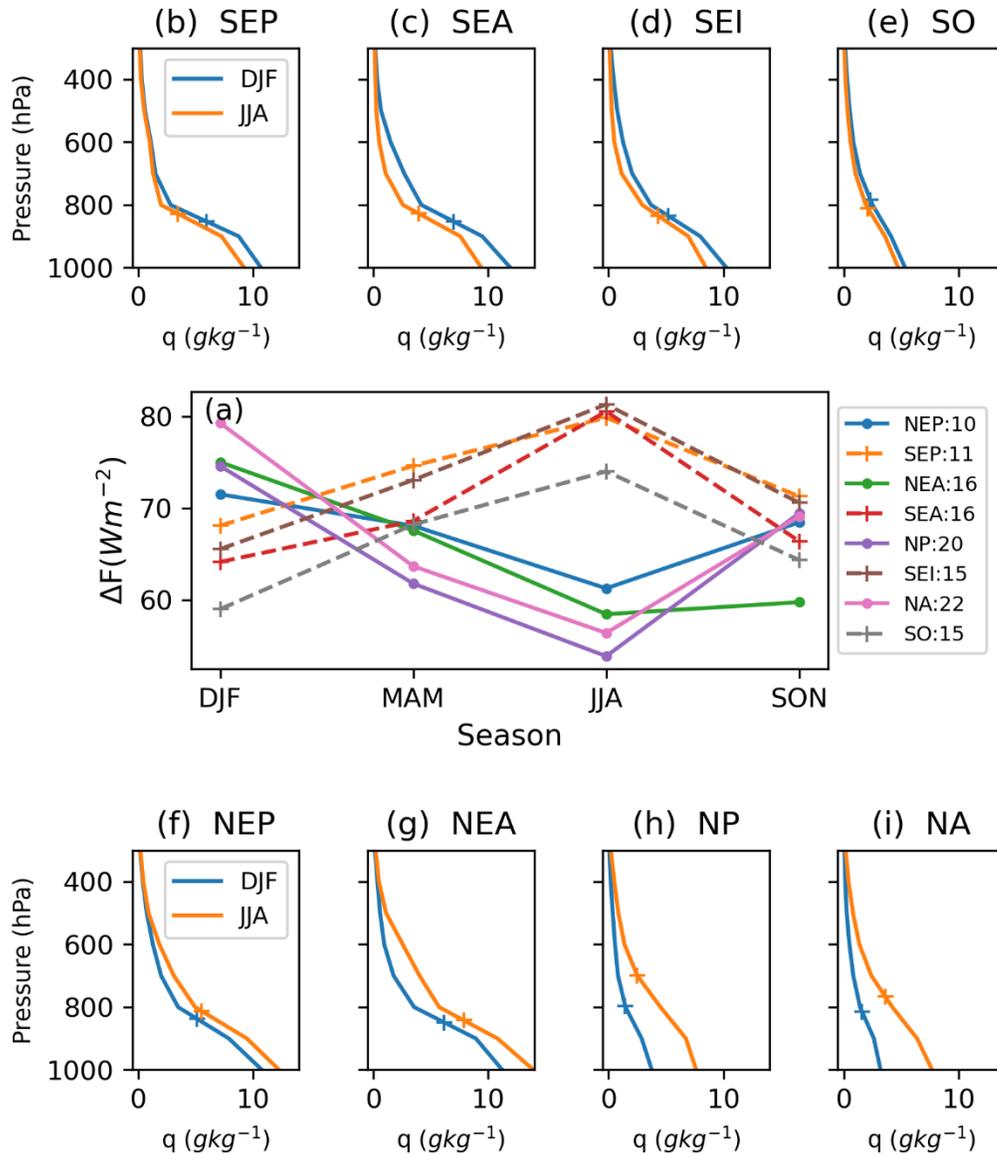
259 4.2. Seasonal cycle

260 The seasonal cycle manifests as the change in atmospheric temperature. The atmospheric
 261 temperature influences the ΔF both directly (via σT_s^4) and indirectly (via q_{700} under the constraint
 262 of Clausius-Clapeyron physics), with the former opposing the latter. The vapor effect dominates,
 263 suggested by Figure 2. The ΔF is stronger in the winter because of the low specific humidity
 264 (favoring the strong cooling) despite the lower temperature (not favoring strong cooling). The
 265 determinant control of atmospheric humidity is more clearly seen by the seasonally varying ΔF
 266 (and the scaled ΔF) being in phase with the q_{700} (Fig. 2c), both shifting with the seasonal movement
 267 of the solar insolation.

268 We further look at specific regions with frequent occurrence of stratocumulus decks:
 269 Northeast Pacific (NEP), Northeast Atlantic (NEA), North Pacific (NP), North Atlantic (NA),
 270 Southeast Pacific (SEP), Southeast Atlantic (SEA), Southeast Indian Ocean (SEI), and Southern
 271 Ocean (SO). The locations of these regions are marked by rectangles in Figure 1g. Figure 3 shows
 272 the seasonal cycles of ΔF , along with the specific humidity profiles in boreal summer (June, July,
 273 and August) and winter (December, January, and February), for these regions. All regions show
 274 distinctive seasonal cycles with stronger cooling in the winter when the atmosphere is drier. The
 275 magnitudes are smallest over the subtropical Pacific oceans (NEP, 10 Wm^{-2} , and SEP, 11 Wm^{-2})

276 and largest over northern mid-latitudes (NP, 20 Wm^{-2} , and NA, 22 Wm^{-2}). There are two reasons
277 for the larger amplitudes in the northern mid-latitudes. First, the atmospheric temperature and thus
278 q experience more distinctive seasonal cycles in the mid-latitudes than the subtropics. Second, the
279 response of LW cooling to the humidity of the overlying atmosphere is non-linear. The increase
280 of the CTTC with the atmospheric desiccation is more rapid in a dry atmosphere than in a humid
281 atmosphere (Zheng, 2019). The mid-latitudes are drier than the subtropics. Note that the cloud-top
282 height is another influential factor for the CTTC because for a given humidity profile a higher
283 cloud intrudes into a drier atmospheric layer, increasing the exposure of the cloud to the cold space,
284 which enhances the cooling. In the northern mid-latitudes, cloud tops are higher in the summer
285 due to the stronger convection propelled by warmer sea surface (Fig. 3d and e). This enhances the
286 summertime CTTC, somewhat damping the humidity-driven seasonal cycle.

287 Interestingly, the SO experiences a markedly smaller degree of seasonal cycle (15 Wm^{-2})
288 than its counterparts in the northern hemisphere (NA and NP). The moisture profiles of SO (Fig.
289 3i) show only a slight increase in the moisture in the austral summer. This seems consistent with
290 previous studies documenting a lack of seasonal cycle for SO MSC properties (Huang et al., 2012;
291 Muhlbauer et al., 2014). Note that samples are selected for the single-layer MSC only. In mid-
292 latitudes, such a cloud regime typically occurs in the colder section of mid-latitude cyclones,
293 causing a sampling bias toward these regions. This sampling bias may be responsible for the lack
294 of seasonal variation. To confirm this idea, needed is investigating the complex coupling between
295 the low clouds, atmospheric thermodynamics, and synoptic dynamics, which is beyond the scope
296 of this study.



297

298 Figure 3: Seasonal cycle of cloud-top radiative cooling for selected regions marked in Fig. 1g
 299 (a). The numbers shown in the legend are the amplitudes of the seasonal cycle. (b)~(i) show the
 300 specific humidity profiles of the boreal summer and winter months for the eight selected regions.
 301 The plus symbols mark the cloud tops.

302

303 4.3. Discussion: relationship to stratocumulus cloudiness

304 The scaled ΔF spatial distribution closely resembles that of the cloudiness of marine
 305 stratocumulus (Fig. 4a in Wood 2012): the cloudiness peaks in the eastern subtropics and mid-
 306 latitudes, and has minimums in the tropics and western sides of the major ocean basins, and there
 307 is a hemispheric asymmetry with greater cloudiness in the southern hemisphere. One might take
 308 this resemblance for granted because the convective circulation in the stratocumulus is primarily

309 driven by the CTRC. Without sufficiently strong CTRC, the stratocumulus decks cannot last long.
310 Here we explain the resemblance from another perspective, with a focus on the environmental
311 dependences of the two factors. Stratocumuli typically occur in subsiding atmospheres (Wood,
312 2012). On one hand, the subsidence helps maintain the shallowness of the cloud-topped boundary
313 layer, sustaining the cloud-surface coupling that feeds moisture from the sea surface to the clouds.
314 On the other hand, the subsiding portion of a region typically corresponds to the cold surface (the
315 physics of thermally driven circulation). Cold water favors overcast stratocumuli in two ways.
316 First, the more stable lower troposphere associated with the cold water helps sustain cloudiness
317 via trapping water vapor within the boundary layer (Klein and Hartmann, 1993; Wood and
318 Bretherton, 2006). Second, the weak surface fluxes associated with the cold water prevent the
319 surface-heating-driven convection that breaks the stratocumulus decks (Wyant et al., 1997;
320 Stevens et al., 1998). Both factors (subsidence and coldness) cause strong CTRC. The subsidence
321 dries out the free atmosphere above the cloud top, enhancing CTRC. The cold temperature drops
322 the free atmospheric specific humidity via Clausius-Clapeyron relationship, again strengthening
323 the CTRC. In a nutshell, environments favoring the occurrence of overcast stratocumulus decks
324 also favor strong CTRC.

325 The rough correspondence between CTRC and MSC cloudiness can be used to explain the
326 spatial pattern of all-sky CTRC (Fig. S3), computed as the multiplication of the two. There is a
327 substantial contrast between the eastern subtropics and the tropics. The all-sky CTRC in eastern
328 subtropics and mid-latitudes remain as large as $> 50 \text{ W m}^{-2}$ due to the large cloud coverage (annual
329 mean of 40 ~ 60%) whereas tropical oceans have all-sky CTRC of only a few W m^{-2} largely caused
330 by the small shallow cloud coverage.

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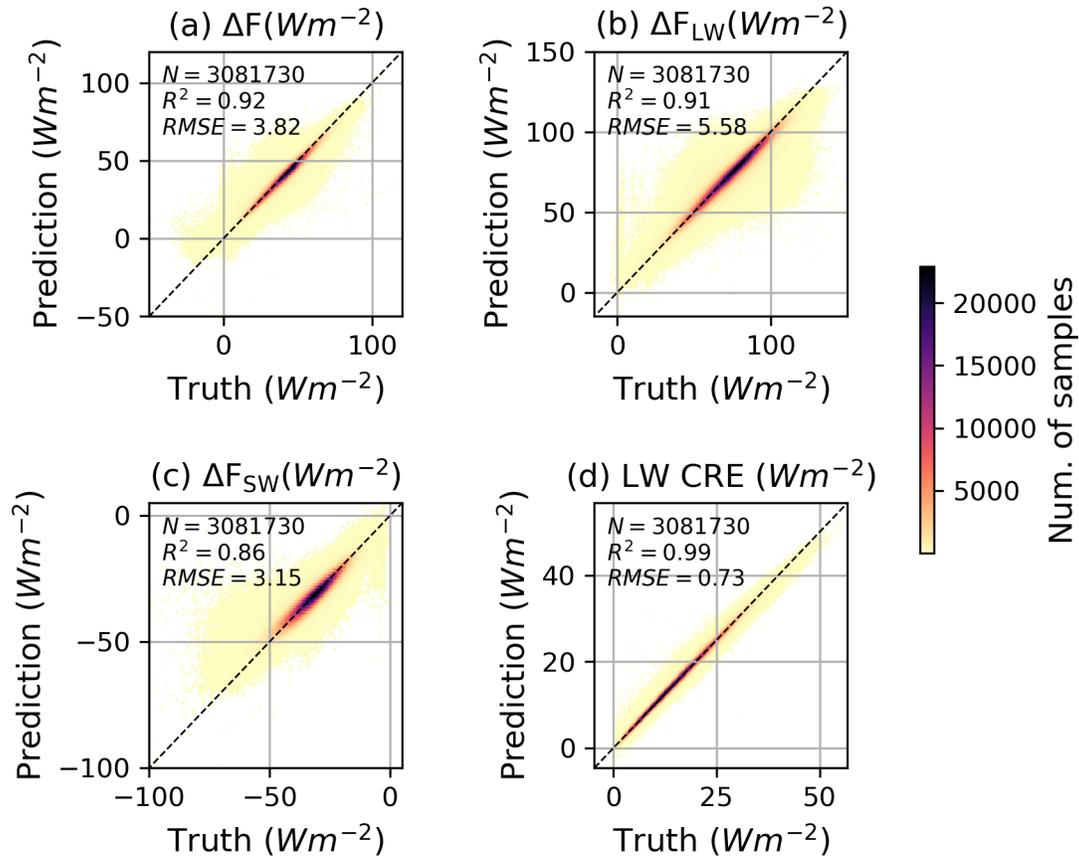
332 **5. Machine learning the CTRC**

333 The major limitation of this CTRC retrieval algorithm is its reliance on running an RTM that
334 is computationally expensive. To address this issue, we propose to use machine learning. Machine
335 learning has been widely used in radiative transfer modeling (e.g. Krasnopolsky et al., 2010;
336 Ukkonen et al., 2020). Among the machine learning algorithms, the artificial neural network (NN)
337 is of particular interest because of its advantage of low computational cost: once it is trained, it is
338 computationally efficient. This strength makes it suited to our needs.

339 The NN used in this study is based on the Python library Keras from TensorFlow (see Text
340 S2 for detail). Table S1 lists the input and output variables. We use half of the MODIS data (~ 3
341 million) for training and the remaining half for validation. It takes the trained model less than 10
342 seconds to compute the CTRC for ~3 million validation datasets. As a comparison, the original
343 algorithm based on the RTM requires more than a half year on a single regular Central Processing
344 Unit.

345 Figure 4a~c shows the validations of the NN-predicted CTRC variables. The agreements are
346 overall excellent. There is a certain degree of scattering but the number of scattered samples is
347 small (yellowish area). Most cases concentrate near the one-to-one line. The major source of error
348 stems from the discretization of the RTM, which can induce random fluctuations when extracting

349 the ΔF from the profiles of radiative fluxes. This is particularly so for geometrically shallow clouds
 350 whose depth is comparable to the model vertical grid size of 50 m. Such randomness may reduce
 351 the NN learning accuracy given the deterministic nature of the NN. This can be demonstrated by
 352 the better performance of the NN for the LW cloud radiative effect (Fig. 4d), a parameter that is
 353 height-independent. The performance is slightly poorer for ΔF_{SW} than ΔF_{LW} , consistent with a more
 354 complex radiation physics in the SW. As expected, the NN-predicted global CTCR climatology
 355 well agrees with the “truth” one (Fig. S4) despite a slight overestimation of CTCR in the
 356 hemispheric winter when the atmosphere is the driest (Fig. S5).



357

358 Figure 4: Validation of the neural network prediction against the “truth” from MOIDS retrieval
 359 for the instantaneous cloud-top radiative cooling (a), its LW (b) and SW components (c), and the
 360 LW cloud radiative effect (d).

361

362 6. Conclusion

363 We generate a one-year climatology of cloud-top radiative cooling (CTRC) and its longwave
 364 and shortwave components for global (except poleward of 65° N/S) marine shallow clouds using
 365 a radiative transfer model with inputs of cloud properties from MODIS in combination with
 366 reanalysis sounding revised by MODIS-retrieved cloud-top temperature. The CTCR retrieval

367 algorithm was developed in our previous study (Zheng et al., 2019). Analyses of the spatial and
368 temporal distributions of the CTRC yield the following findings:

- 369 (1) The global mean cloud-top radiative flux divergence (ΔF) is -61 W m^{-2} , decomposed into
370 the LW cooling of -73 W m^{-2} and SW heating of 11 W m^{-2} . The ΔF is largely a reflection
371 of the LW cooling.
- 372 (2) The ΔF has a strong latitudinal dependence with a cooling minimum in the tropics. The
373 cooling increases with the latitude until $\sim 30^\circ \text{ N}$ or S. The increase in cooling is primarily
374 driven by the increasing dryness of the free atmosphere that reduces the down-welling LW
375 flux. The cooling peaks in the subtropical eastern ocean under the downward branches of
376 the Hadley circulation. Poleward of 30° N or S, the cooling decreases slightly, primarily
377 due to the colder atmospheric temperature that weakens the cloud's outgoing thermal
378 emission. If we scale the ΔF by the σT_s^4 to remove the effect by temperature-driven
379 emission, the zonal-mean scaled cooling increases all the way from the tropics to the extra-
380 tropics, a reflection of the decreasing specific humidity of the atmosphere.
- 381 (3) There is a hemispheric asymmetry with stronger cooling in the Southern Hemisphere.
- 382 (4) The CTRC exhibits distinctive seasonal cycles, with amplitudes of the order 10 to 20 W
383 m^{-2} . The cooling maximizes during the winter when the atmospheric specific humidity is
384 low, which favors the cooling.
- 385 (5) The CTRC spatial patterns resemble the marine stratocumulus cloudiness. The
386 resemblance is a result of the fact that environments favoring the formation of
387 stratocumulus decks also favor the strong CTRC.

388 Finally, we examine the potential of machine learning in speeding up the CTRC retrieval.
389 Trained by the half-year's worth of CTRC datasets with a sample size of ~ 3 million and validated
390 against the other half, the neural network model exhibits a satisfactory performance with the
391 absolute retrieval error of $\sim 6\%$. The neural network model speeds up the radiative-transfer-model-
392 based retrieval by the order of million times. This will enable generations of much larger CTRC
393 datasets, useful for future more comprehensive research.

394

395 **Acknowledgments**

396 This study is supported by the Department of Energy (DOE) Atmospheric System Research
397 program (DE-SC0018996).

398 **Data Availability Statement**

399 The MODIS data are from [ladsweb.modaps.eosdis.nasa.gov](https://adsweb.modaps.eosdis.nasa.gov). NCEP reanalysis data are
400 collected from rda.ucar.edu/datasets/ds083.2/. NOAA sea surface temperature data are obtained
401 from <https://psl.noaa.gov/data/gridded/data.noaa.oisst.v2.highres.html>. The code used to produce
402 the results and the neural network model is available at <https://doi.org/10.5281/zenodo.5043713>.

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