

1 **Bayesian framework for inversion of second-order stress**
2 **glut moments: application to the 2020 M_w 7.7 Caribbean**
3 **Earthquake**

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6 **Key Points:**

- 7 • We develop a Bayesian inverse scheme to solve for stress glut second moments of
8 earthquakes using teleseismic data.
9 • We sample the positive-definite constrained posterior distribution using Hamiltonian
10 Monte Carlo sampling and automatic differentiation.
11 • Using the 2020 M_w 7.7 Caribbean Earthquake as an example, we demonstrate the
12 efficacy and utility of this inverse framework.

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Abstract

We present a fully Bayesian inverse scheme to determine second moments of the stress glut using teleseismic earthquake seismograms. The second moments form a low-dimensional, physically-motivated representation of the rupture process that captures its spatial extent, source duration, and directivity effects. We determine an ensemble of second moment solutions by employing Hamiltonian Monte Carlo and automatic differentiation to efficiently approximate the posterior. Our method explicitly constrains the parameter space to be symmetric positive definite, ensuring the derived source properties have physically meaningful values. The framework accounts for the autocorrelation structure of the errors and incorporates hyperpriors on the uncertainty. We validate the methodology using a synthetic test and subsequently apply it to the 2020 M_w 7.7 Caribbean earthquake. The second moments determined for this event indicate the rupture was nearly unilateral and relatively compact along-strike. The solutions from this inverse framework can resolve ambiguities between slip distributions with minimal a priori assumptions on the rupture process.

Plain Language Summary

Earthquake science is presented with the challenging problem of determining properties of earthquake sources that occur deep within the Earth using observations made at the surface of the Earth. Typically, the process for determining these important quantities involves finding solutions to complicated optimization problems that, given the necessarily poor data coverage, are poorly constrained. With this challenge in mind, we present a framework to solve for some fundamental properties of earthquake sources like spatial extent, rupture propagation direction, and duration. This approach requires few assumptions about the geometry of the fault that ruptured and the dynamics of the rupture process, in contrast to more traditional methods. This procedure also provides a probabilistic description of these earthquake source properties, which is essential, because the uncertainty inherent to this problem dictates that we cannot confidently choose any one particular solution. We demonstrate this method's utility by applying it to the 2020 Magnitude 7.7 Caribbean Earthquake. Through this application, we show that this framework can both determine properties of earthquake sources that have historically been difficult to constrain and successfully resolve ambiguities between solutions of more traditional techniques.

43 **Introduction**

44 Earthquakes are complicated physical processes that dynamically vary in space and
45 time. Better understanding the factors that control earthquake behavior consequently re-
46 quires constraining the finite source properties of earthquakes. In pursuit of this under-
47 standing, high dimensional estimates of finite source properties are routinely computed for
48 significant earthquakes (e.g. Wald & Heaton, 1992; Ammon, 2005; M. Moreno et al., 2010;
49 Ide et al., 2011; Ross et al., 2019). These estimates usually involve the inversion for slip
50 on a predefined fault plane using some combination of seismic, geodetic, and tsunami data
51 with kinematic constraints placed on the rupture propagation (Hartzell & Heaton, 1983; Du
52 et al., 1992; Saito et al., 2011). These solutions, termed fault slip distributions, are valuable
53 in that they provide a detailed image of time-dependent slip behavior. But, the necessary
54 user-defined parameterization, general lack of sensitivity to rupture velocity, and necessary
55 regularization makes these estimates of finite source properties strongly nonunique (e.g.
56 Lay, 2018). This nonuniqueness presents challenges to objectively comparing finite source
57 properties between events, and thus limits our ability to discern patterns in earthquake
58 behavior that could inform a deeper understanding of earthquake phenomenology.

59 The limitations of routinely computed estimates of finite source properties motivates
60 the development of alternative estimates that overcome these limitations. One potential al-
61 ternative is the second moment formulation (G. Backus & Mulcahy, 1976a, 1976b), in which
62 higher-order mathematical moments of the stress glut, a source representational quantity,
63 are used to describe basic properties of the rupture process in space and time. Higher-order
64 stress glut moments have been successfully computed in the past (Bukchin, 1995; McGuire et
65 al., 2000, 2001, 2002; McGuire, 2004; Chen, 2005; Meng et al., 2020), but this methodology
66 has received little attention compared to slip inversions. The second-moment formulation
67 yields low-dimensional, physically-motivated estimates of the spatial extent, directivity, and
68 duration of earthquake ruptures. It requires no prior knowledge of the rupture velocity,
69 and makes only mild assumptions about the source geometry. Being free of gridding and
70 associated discretization issues that complicate slip inversions, the second moment formu-
71 lation can more objectively facilitate comparisons between events, helping to find common
72 patterns. Illuminating these patterns may help address outstanding questions in earthquake
73 science relating to how fault zones may facilitate or impede earthquake ruptures.

74 Our contributions in this paper are as follows. We develop a Bayesian inverse scheme for
75 second moments using teleseismic data. We employ Hamiltonian Monte Carlo sampling and
76 automatic differentiation to efficiently sample from the posterior distribution. In doing so, we
77 apply a set of transformations that ensure positive definiteness of the second moments. We
78 demonstrate the efficacy of our methodology by applying the inversion scheme to the 2020
79 M_w 7.7 Caribbean Earthquake. We show that our methodology is useful for both inferring
80 source parameters that are poorly constrained by other source estimation procedures and
81 resolving ambiguities between finite slip distributions.

Case study: the 2020 M_w 7.7 Caribbean earthquake

Event background and tectonic summary

On January 28, 2020, a large earthquake occurred in the Caribbean Sea near the Cayman Islands. The global Centroid Moment Tensor (gCMT) (Dziewonski et al., 1981; Ekström et al., 2012) solution of this earthquake suggests that the event was a largely double-couple, nearly vertically dipping, strike-slip earthquake with a moment magnitude of M_w 7.7 (GCMT, 2020). The geographic setting of this event is shown in Figure 1. This event took place near the northern margin of the Gonâve Microplate, an elongated plate that characterizes a portion of the boundary between the North American and Caribbean plates. The dominant local structural feature in this region is the Mid-Cayman Rise, which produces seafloor spreading that is partially accommodated by the transform faults that bound the Gonâve Microplate (Mann et al., 1995; DeMets & Wiggins-Grandison, 2007). The centroid location and focal mechanism of the Caribbean Earthquake suggest that this event likely ruptured the Oriente Fault, a left-lateral transform fault that constitutes the boundary between the North American Plate and the Gonâve Microplate. Though the spreading rate of the Mid-Cayman Rise is slow (DeMets & Wiggins-Grandison, 2007), the segments of the Oriente Fault neighboring the Caribbean Earthquake have produced numerous $M6+$ earthquakes in recent history (Van Dusen & Doser, 2000; B. Moreno et al., 2002).

Despite its large magnitude, there are few finite rupture solutions for the Caribbean Earthquake to date (USGS, 2020; Tadapansawut et al., 2021). Though these solutions agree that the Caribbean earthquake likely ruptured unilaterally to the SW along the Oriente Fault, there is no consensus on some fundamental source parameters, such as the rupture’s lateral extent. In particular, the USGS solution for this event suggests that most of the slip was confined within an 80 km length along the fault, while the Tadapansawut et al. solution suggests a much larger slip region that extends well over 300 km. Thus, in addition to producing statistically robust estimates of rupture characteristics, this second moment formulation may prove useful in resolving first-order differences between slip distributions.

Data

In this study we use vertical component seismic data from 52 Global Seismographic Network (GSN) stations (Figure 1). We selected these stations by evaluating how well the waveforms were approximated by point source synthetics computed using the gCMT solution. The seismograms used in the inversion are 700 second windows about the surface wave packet that we manually selected from 7200 second windows that start at the gCMT centroid time for the Caribbean Earthquake. We down-sample the waveform data to 0.1 Hz sampling rate to somewhat reduce the correlation between samples, while keeping computational demands minimal. As part of the construction of the forward propagation matrix, we computed the Green’s tensor using the gCMT moment tensor and centroid location, which we perturbed to compute the requisite spatial derivatives numerically.

Methodology

Stress Glut Moments

Because an earthquake is constituted by a localized zone of inelastic deformation, we can represent the source region as a localized departure from elasticity. These departures can be quantified using the so-called stress glut, $\mathbf{\Gamma}$, the tensor field computed by applying an idealized Hooke's law to the inelastic component of strain in a system (G. Backus & Mulcahy, 1976a, 1976b). The stress glut is nonzero only within the source region. The stress glut is a complete representation of a seismic source in space and time that can be used to reproduce displacements everywhere on Earth for an arbitrary source (Dahlen & Tromp, 1998). Given the typically sparse distribution of seismic observations, solving for the full stress glut is an ill-posed problem. We can simplify the stress glut by assuming the source geometry is constant in space and time:

$$\mathbf{\Gamma}_{ij}(\xi, \tau) = \hat{\mathbf{M}}_{ij} f(\xi, \tau) \quad (1)$$

Where $\hat{\mathbf{M}}$ is the normalized mean seismic moment tensor and f is the scalar function. This approximation reduces the solution from a tensor field to a scalar field and is most valid for seismic sources with stable source mechanisms.

We can further reduce the dimensionality of the stress glut by first recognizing that any scalar function in a bounded interval may be uniquely determined by its collection of polynomial moments. Because f captures a static displacement, f is nonzero for infinite time and thus occupies an unbounded interval, but \dot{f} vanishes to zero at the cessation of rupture and is thus captured within a bounded interval. Hence, considering that the stress glut prescribes displacements due to an arbitrary seismic source, we can represent seismic displacements as the superposition of the spatio-temporal moments of the rate function \dot{f} . At low frequencies, we can truncate this infinite series such that we only include terms with moments of order $m + n \leq 2$. We can then explicitly define the measured displacements for a station i at low frequencies as:

$$\begin{aligned} u_i(\mathbf{r}, t) = & \dot{f}^{(0,0)}(\xi_c, \tau_c) \mathbf{M}_{jl} \frac{d}{d\xi_l} \int_{-\infty}^{+\infty} \mathbf{G}_{ij}(\xi_c, \tau_c, \mathbf{r}, t) dt \\ & - \dot{f}_m^{(1,1)}(\xi_c, \tau_c) \mathbf{M}_{jl} \frac{d}{d\xi_m} \frac{d}{d\xi_l} \mathbf{G}_{ij}(\xi_c, \tau_c, \mathbf{r}, t) \\ & + \frac{1}{2} \dot{f}_{mn}^{(2,0)}(\xi_c, \tau_c) \mathbf{M}_{jl} \frac{d}{d\xi_m} \frac{d}{d\xi_n} \frac{d}{d\xi_l} \int_{-\infty}^{+\infty} \mathbf{G}_{ij}(\xi_c, \tau_c, \mathbf{r}, t) dt \\ & + \frac{1}{2} \dot{f}^{(0,2)}(\xi_c, \tau_c) \mathbf{M}_{jl} \frac{d}{d\xi_l} \frac{d}{dt} \mathbf{G}_{ij}(\xi_c, \tau_c, \mathbf{r}, t) \end{aligned} \quad (2)$$

Where \mathbf{G} is a Green's tensor prescribing the path effects from a source with the centroid location ξ_c and centroid time τ_c to an arbitrary station with the location \mathbf{r} at time t , and $\dot{f}^{(m,n)}(\xi_c, \tau_c)$ is the moment of the scalar rate function $\dot{f}(\xi, \tau)$ of spatial order m and temporal order n taken about the source centroid in space and time (Bukchin, 1995).

Several of the moments are of routine use in seismology, while the rest are worked with sparingly. The moment of order $m + n = 0$ is the scalar moment of the source. The moments of order $m + n = 1$ correspond to the spatial ($m = 1$) and temporal ($n = 1$) centroids of the source. Perhaps unfamiliar are the moments of order $m + n = 2$; these moments describe low-dimensional finite properties of earthquake sources. In particular, $\dot{f}^{(2,0)}(\xi_c, \tau_c)$ is the spatial covariance of the stress glut, $\dot{f}^{(1,1)}(\xi_c, \tau_c)$ is the spatio-temporal covariance of the stress glut, and $\dot{f}^{(0,2)}(\xi_c, \tau_c)$ is the temporal variance of the stress glut. These so-called second moments yield low-dimensional, physically-motivated approximations of the source volume, source directivity, and source duration respectively (G. E. Backus, 1977).

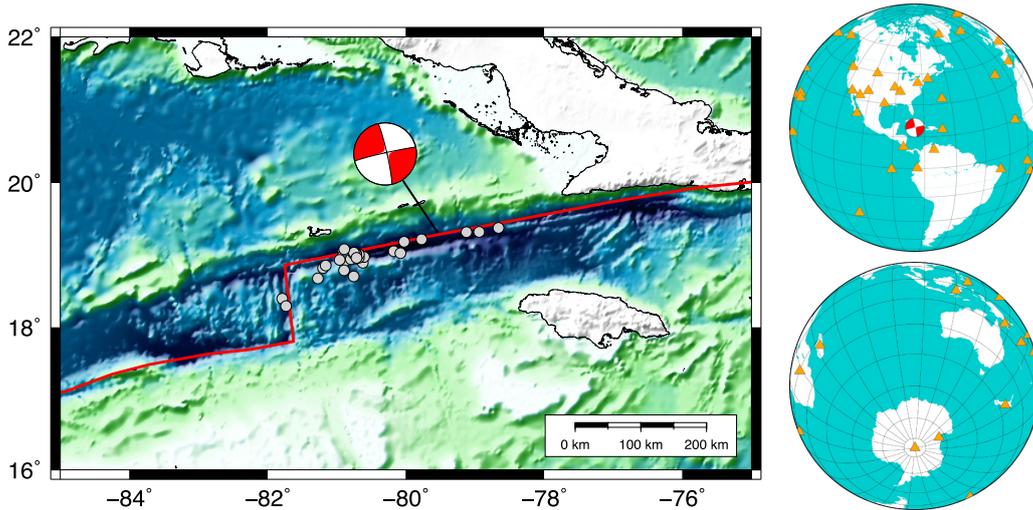


Figure 1. Left: Geographic setting of the 2020 Caribbean earthquake. Focal mechanism is the gCMT solution for the 2020 Caribbean earthquake. Gray dots indicate the locations of USGS cataloged aftershocks for the event. Red line indicates the boundary between the North American and Caribbean plates (Bird, 2003). Map coloring is reflective of seafloor depth. Right: Global distribution of stations from which waveforms were used in this study.

Waveform preprocessing

To compute the Green’s tensor, we use the Preliminary Reference Earth Model (PREM) (Dziewonski & Anderson, 1981) and the normal mode summation package Mineos (Masters et al., 2011). To improve stability when approximating integrals and derivatives, we compute this Green’s tensor at a high sampling rate (20 Hz). We take the necessary temporal and spatial derivatives and integrals of this Green’s tensor numerically using a centered finite difference approximation. For the spatial derivatives, the finite difference offsets from the spatial centroid are 250 m. The construction of the forward propagation matrix described in this study require both the gCMT moment tensor and the Green’s tensor derivatives and integrals.

We bandpass the observed waveforms and green tensor between 100 and 200 seconds and perform a visual quality control by comparing the displacements of the synthetic point source representation of our source with the observed waveforms. Because the contribution of moments of order $m + n \geq 2$ should be small, the synthetic waveforms produced using a point source approximation should be similar to the observed waveforms. We thus remove stations that did not show a good match between the synthetic point source displacements and the observed waveforms. We then align the Green’s tensor and observed displacements of the remaining stations via cross correlation, and we manually pick the arrivals of and determine the window lengths for the surface wave packets at each station. These windows constitute the time-segments of the Green’s tensor and observed waveforms included in the forward propagation matrix and data vector used in this study respectively.

The Inverse Problem

Though equation 2 appears unruly, many of the terms that constitute it are easily accessible. For a given source, we can observe $u_i(\mathbf{r}, t)$ using seismic instrumentation; we can solve for \mathbf{G} , \mathbf{M} , and (ξ_c, τ_c) using routine techniques; and we can compute the necessary derivatives and integrals using numerical methods. Thus, in equation 2, only the moments

184 of the scalar function \dot{f} are unknown. We can then pose equation 2 as a linear inverse
185 problem:

$$\mathbf{d} = \mathbf{F}\mathbf{p} \quad (3)$$

186 where \mathbf{d} is a vector of measured displacements, \mathbf{F} is a forward propagation matrix of spatial
187 and temporal integrals and derivatives of \mathbf{G} , the columns of which are weighted by the
188 components of \mathbf{M} , and \mathbf{p} is a vector of parameters which constitute the lower-order moments
189 of the stress glut.

190 Numerous Bayesian methods for source parameter inversion have been proposed for
191 problems such as focal mechanism estimation (Wéber, 2006; Walsh et al., 2009; Lee et al.,
192 2011; Duputel et al., 2014) and slip distribution estimation (Monelli et al., 2009; Minson et
193 al., 2013). Bayesian approaches for source estimation are growing in popularity because the
194 probabilistic nature of these inversions is such that they do not require the user to choose a
195 single solution for problems that, due to uncertainty, have many potential solutions. Instead,
196 Bayesian approaches provide ensembles of solutions that are informed by prior distributions
197 determined by physical constraints or ground truth. The Bayesian formulation described
198 here allows for the computation of an ensemble of solutions for second moments that rep-
199 resent distributions of potential low-dimensional finite source properties for an earthquake
200 source.

201 The posterior distribution for this problem can be written as follows (e.g. Tarantola,
202 2005),

$$p(\mathbf{p}, \sigma | \mathbf{d}) \propto p(\mathbf{d} | \sigma, \mathbf{p}) p(\sigma) p(\mathbf{p}), \quad (4)$$

203 where σ is a hyperparameter. For the likelihood term, $p(\mathbf{d} | \sigma, \mathbf{p})$, we use a multivariate
204 normal distribution,

$$p(\mathbf{d} | \sigma, \mathbf{p}) \propto \frac{1}{\sqrt{|\Sigma|}} \exp\left(-\frac{1}{2}(\mathbf{d} - \mathbf{F}\mathbf{p})^T \Sigma^{-1} (\mathbf{d} - \mathbf{F}\mathbf{p})\right) \quad (5)$$

205 Since the observations are time-series data, errors in the forward model will result in tempo-
206 ral autocorrelation. We can account for this correlation structure through the data covari-
207 ance matrix, Σ , as outlined in (Duputel et al., 2014). If both points d_i and d_j are recorded
208 by the same station:

$$\Sigma_{ij} = \sigma \cdot \exp(-|i - j|\delta t / \Delta t) \quad (6)$$

209 Where δt is the sampling rate, and Δt is the shortest period information included in the
210 time-series. This correlation structure accounts for temporal correlation in the errors, but
211 not any spatial correlation. In this paper we assume that the observations are spatially
212 distributed sparsely enough that spatially-correlated errors are negligible.

213 We use uninformed priors in this case study. But, this framework is flexible such that
214 informed priors can easily be incorporated (Gelman et al., 2010). That is, with the physical
215 interpretation of the second moment properties that we will describe shortly, priors on the
216 spatial extent, directivity, and duration may be imposed given observational ground truth.
217 For example, if the true nodal plane of an earthquake is known, Gaussian priors may be
218 placed on the spatial second moment parameters to restrict the principal eigenvector of the
219 spatial covariance matrix to abut the true nodal plane.

220 The total number of parameters in this inverse problem is 11, and we approximate
221 $p(\mathbf{p}, \sigma | \mathbf{d})$ using Markov Chain Monte Carlo (MCMC) sampling to obtain an ensemble of
222 solutions. We do not solve for the zeroth or first order moments, and instead use the
223 gCMT solution as our moment tensor and centroid location. Because the parameter space
224 is quite large, we sample the posterior distribution using Hamiltonian Monte Carlo (HMC)
225 sampling (Neal, 2010), which is an instance of the Metropolis-Hastings algorithm that can
226 efficiently sample large parameter spaces using principles from Hamiltonian dynamics. This

227 is accomplished in part by incorporating gradient information into the sampling process;
 228 however, it requires a means to also compute gradients efficiently. Here, we accomplish this
 229 through the use of reverse-mode automatic differentiation (Innes, 2019).

230 For each chain in this inversion, we draw 5000 samples from the posterior distributions
 231 after drawing 5000 burn-in samples. In this inversion, the momentum distribution has a
 232 diagonal mass matrix and the samples are updated using an ordinary leapfrog integrator
 233 (Neal, 2010). The only hyperparameter in this inversion is σ , which we use to construct
 234 the covariance matrix according to equation 6. To evaluate convergence, we run at least
 235 3 chains of the inversion and compute the Gelman-Rubin diagnostic using the computed
 236 set of chains (Gelman & Rubin, 1992). That is, we compare the variability within chains
 237 to the variability between chains to determine if the chains all converge to the same target
 238 distributions.

239 Additionally, because the second moments of the stress glut are covariances, only a
 240 subset of the parameter space produces valid solutions. Specifically, the second moments
 241 are symmetric positive definite,

$$\mathbf{X} = \begin{bmatrix} \dot{f}^{(2,0)}(\xi_{\mathbf{c}}, \tau_c) & \dot{f}^{(1,1)}(\xi_{\mathbf{c}}, \tau_c) \\ \dot{f}^{(1,1)}(\xi_{\mathbf{c}}, \tau_c)^T & \dot{f}^{(0,2)}(\xi_{\mathbf{c}}, \tau_c) \end{bmatrix} \succeq 0. \quad (7)$$

242 Physically, this is equivalent to saying that the spatial extent and duration of the source are
 243 both non-negative. Typically, when performing a constrained Bayesian inversion, the easiest
 244 course of action is to sample under an unconstrained parameter space and subsequently
 245 transform those parameters into the necessarily constrained parameter space (Gelman et al.,
 246 2010). To this end, we note that, by the Cholesky Factorization Theorem, every symmetric
 247 positive-definite matrix can be decomposed into the product of some lower triangular matrix
 248 with a positive diagonal and the transpose of that same lower triangular matrix. This means
 249 that given \mathbf{X} , there exists a lower triangular matrix \mathbf{L} with positive diagonal components
 250 such that:

$$\mathbf{X} = \mathbf{L}\mathbf{L}^T \quad (8)$$

251 Thus, we can sample freely from the unconstrained off-diagonal components of \mathbf{L} and from
 252 the natural logarithm of the diagonal components of \mathbf{L} . Then, to evaluate our sample
 253 against our data, we can simply build \mathbf{L} using our sample components and then construct
 254 \mathbf{X} using equation 5. From \mathbf{X} we can extract a valid \mathbf{p} with which we evaluate the likelihood
 255 of our sample. A keen observer may notice that while \mathbf{X} need only be symmetric posi-
 256 tive semi-definite, the Cholesky factorization forces \mathbf{X} to be positive definite. In practice,
 257 this distinction is inconsequential, as a positive semi-definite \mathbf{X} suggests that at least one
 258 dimension of the source is identically zero, which will never be true in reality.

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Results

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Before showing the application of this methodology to real data, we will show a test of the outlined inversion procedure using a synthetic source. We can also use this test to determine the resolvability of the parameters of the Caribbean earthquake. To these ends, we prescribe a 60x20 km rectangular fault with a strike and dip corresponding to the nodal plane of the gCMT solution that is aligned with the Oriente Fault. We then define a grid of point sources, each with the gCMT source mechanism and equal fraction of the gCMT moment, along this prescribed fault such that the spatial release of moment can be approximated as uniform distributions of moment release along the strike and dip of the fault. We delay the activation of these point sources according to a prescribed rupture velocity of 1.2 km/s along strike, resulting in an event duration of 50 s, such that the moment release with time can also be approximated as a uniform distribution. Using the fact that the width of a uniform distribution is equal to $2\sqrt{3}\sigma$, where σ is the standard deviation of the Gaussian approximation of that uniform distribution, we can determine the true second moment solution for this synthetic source. In the interest of evaluating the resolvability of parameters for the Caribbean earthquake, we invert for these second moments using the same distribution of stations and the same windowing procedure that we use for the real event. For this test, we also use the mean σ from the inversion of real data so we could assess how visible known features are in the presence of realistic error. The joint probability distributions for each pair of inverted parameters are shown in Figure 7. These plots show that most of the parameters are either uncorrelated or weakly correlated with each other, with the exception of some of the spatio-temporal terms with their spatial counterparts and some closely related spatial terms.

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We can further test the fidelity of our inversion results by computing synthetic waveforms using equation 2 and evaluating the fit to the observed waveforms generated for this synthetic example. The waveforms for an ensemble of second moment solutions from a single chain for the synthetic test are shown for a subset of stations with a large diversity of azimuths and distances in Figure 3. The waveform fits match the synthetic observations very well, particularly when the full ensemble of solutions is considered.

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In order to represent the second moment solutions for the synthetic test in a more physically interpretable way, we convert the second moments into measures of volume, directivity, and duration. To estimate the volume of moment release from this source, we define an ellipsoid using the eigenvalues and eigenvectors of the spatial second moment of the event, $\dot{f}^{(2,0)}(\xi_c, \tau_c)$. Assuming the spatial moment distribution follows a 3-dimensional Gaussian function, this ellipsoid represents the volume encompassing 95% of the moment released during the earthquake. The projections of the ellipsoids for the ensemble of solutions from a single chain from the synthetic test are shown in Figure 4. We can also infer the instantaneous velocity of the moment centroid, an estimate of directivity, by dividing the spatiotemporal second moment of the source, $\dot{f}^{(1,1)}(\xi_c, \tau_c)$, by the temporal second moment of the source, $\dot{f}^{(0,2)}(\xi_c, \tau_c)$. The map-view projections and Z-components of these velocity vectors for the synthetic test are given in Figure 4. Finally, we can estimate the source duration if we assume the moment rate function of the earthquake is a Gaussian distribution about the temporal centroid. Then, the second temporal moment of the source, $\dot{f}^{(0,2)}(\xi_c, \tau_c)$, defines the variance of that moment-rate function. These Gaussian approximations to the moment-rate function for the synthetic test are plotted in Figure 4. Figure 4 also allows us to evaluate how well the ensemble of solutions captures the true solution for this test. Indeed, the true along-strike length, vertical extent, directivity, and duration all fall within the ensemble of solutions which suggests these are well constrained features in this inversion.

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Now, we invert for the second moments of the 2020 Caribbean event using the real data. The distributions of the 10 independent parameters of the second moments for a single chain of the inversion using the real data are shown in Figure 5. We run the inversion for a set of chains, shown in Figure S1, and compute the Gelman-Rubin diagnostic (Gelman & Rubin,

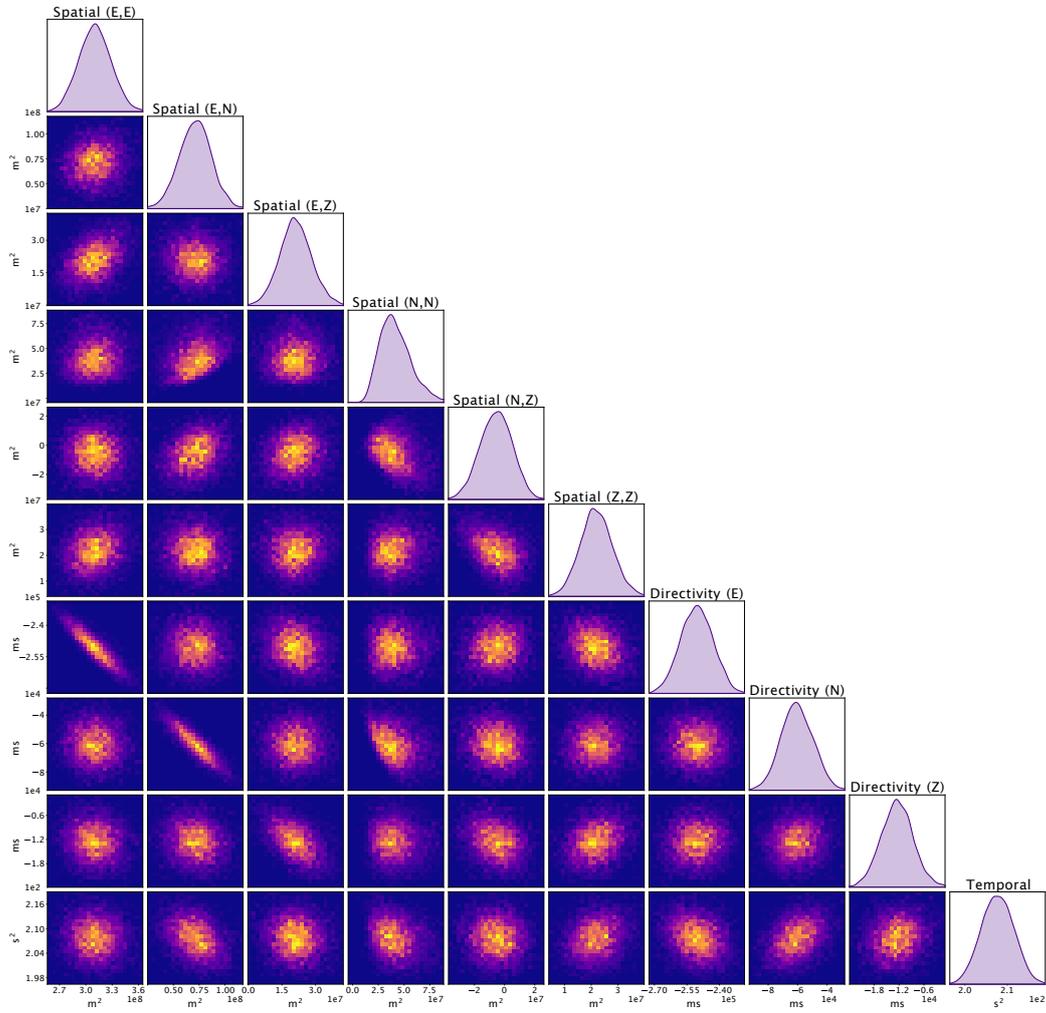


Figure 2. Marginal and joint probability density plots for the 10 independent parameters inverted for the synthetic test in this study. Off-diagonal plots are 2-dimensional histogram plots representing the joint probability distribution for each pair of independent parameters. On-diagonal plots are kernel density estimate plots for the marginal distributions of the adjacent joint probability distributions.

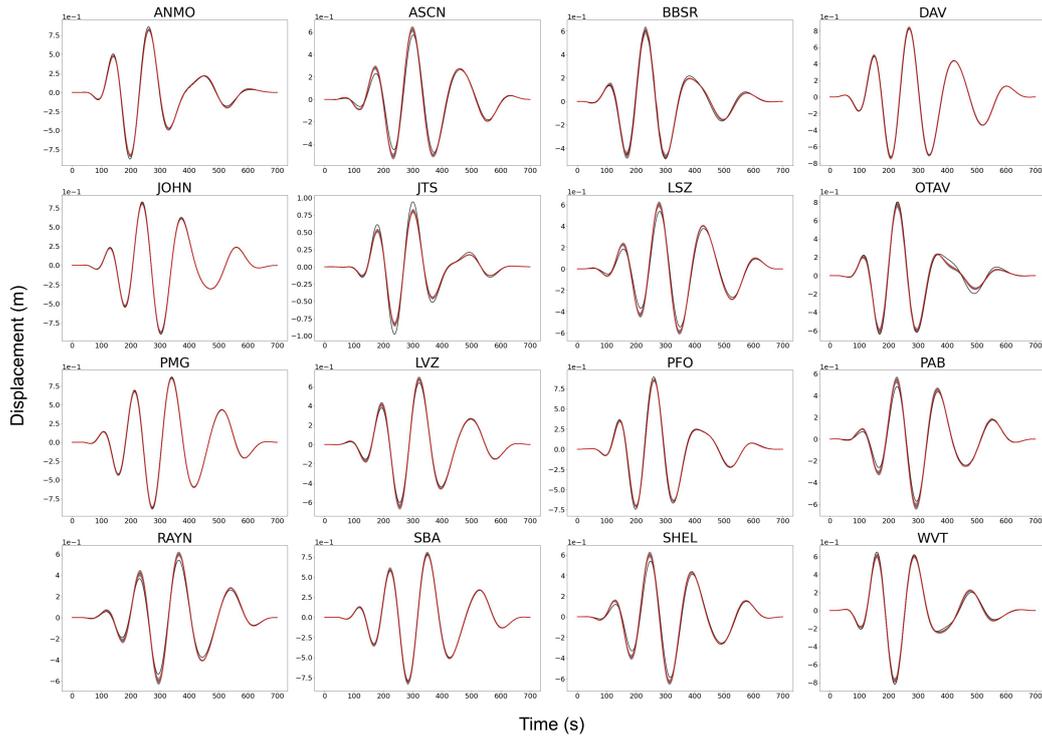


Figure 3. Waveform fits for a subset of the windowed waveforms for the synthetic test conducted in this study. Waveforms are labeled according to the GSN station at which they were generated. Black waveforms are synthetic observations. Gray waveforms are generated using a single solution from the ensemble of solutions from our inversion. Waveforms from each solution in the ensemble are plotted. Red waveforms are generated using the mean solution of the ensemble of solutions from our inversion.

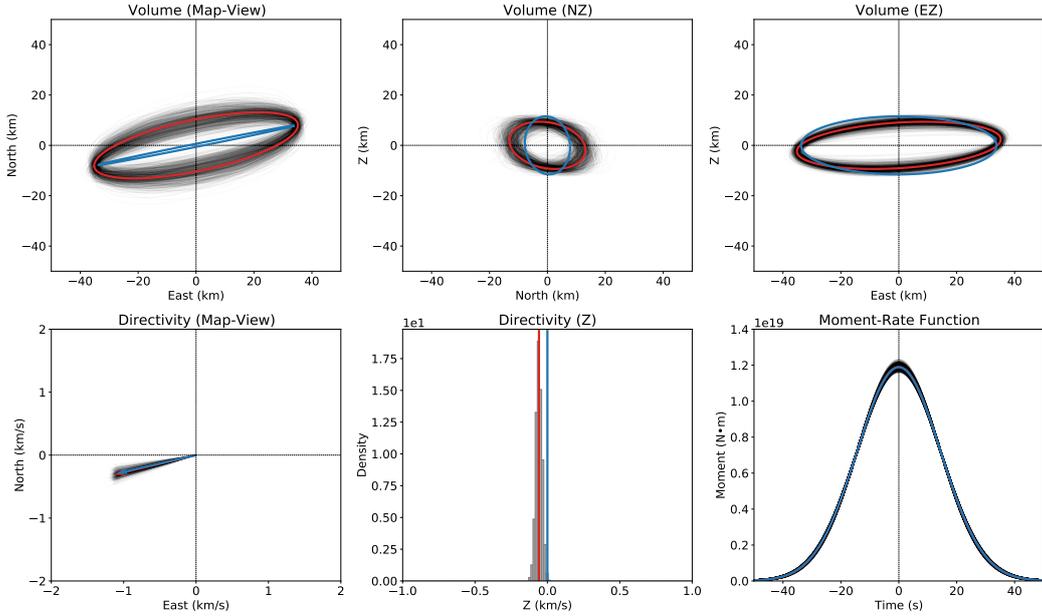


Figure 4. Physically motivated representation of the ensemble of second moment solutions for the synthetic test. Top row: Projections of the spatial ellipsoid generated using the eigenvalues and eigenvectors of the spatial covariance matrix of the stress glut distribution. This ellipsoid is projected into map-view (left), into the NZ-plane (middle), and into the EZ-plane (right). Bottom row: Instances of the directivity vector representing the instantaneous velocity of the centroid of the source and instances of the Gaussian approximation of the source-time function of the source. Directivity vectors are projected into map-view (left) and the distribution of Z-components of the directivity vectors is plotted as a histogram (middle). Gaussian approximations of the source-time function are plotted relative to the centroid time (right). Gray-scale represents the ensemble of solutions for which, with the exception of the histogram of directivity vector Z-components, darkness represents the density of the plotted solutions. Red represents the mean solution. Blue represents the true solution.

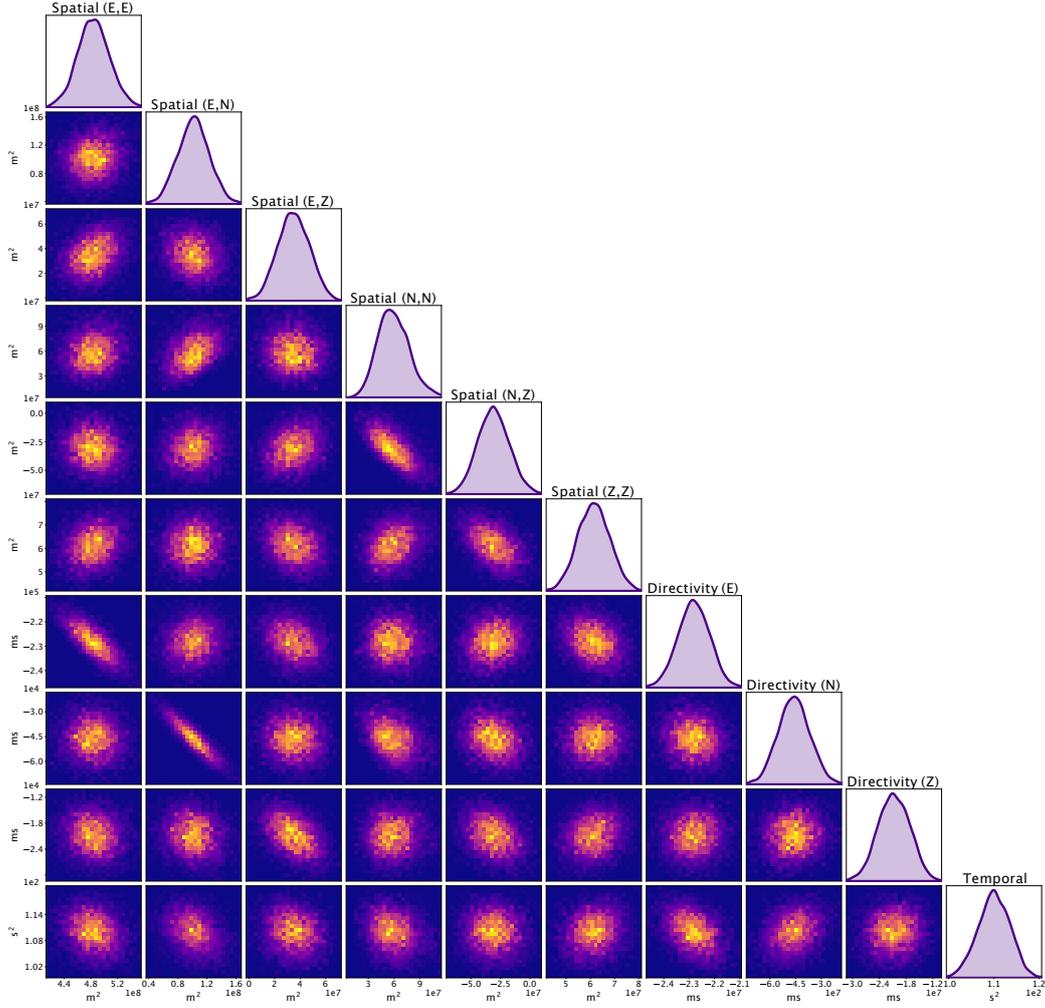


Figure 5. Marginal and joint probability density plots for the 10 independent parameters inverted for in this study. Off-diagonal plots are 2-dimensional histogram plots representing the joint probability distribution for each pair of independent parameters. On-diagonal plots are kernel density estimate plots for the marginal distributions of the adjacent joint probability distributions.

1992) using these chains. The Gelman-Rubin values are far less than 1.1, suggesting that the chains have converged to the target posterior distributions for the second moments. The joint probability distributions for each pair of parameters are shown in Figure 5. The distribution for the hyperparameter σ is shown in Figure S2. As with the synthetic test, these joint distributions show that the inverted parameters are mostly uncorrelated with each other. We can also evaluate the waveform fits for the inversion using real data. These waveform fits are shown in Figure 6. The computed waveforms for the ensemble of solutions inverted for under this framework fit the observed waveforms reasonably well.

Given that some of the features are well resolved, under the assumption that the stress glut rate is distributed as a 4-dimensional Gaussian function, we can use these ensembles of second moments to constrain features of the fault rupture. In particular, the map-view projection of the volume ellipsoid shown in Figure 7 closely follows the strike of the Oriente Fault, and suggests that 95% of the moment of this event was released in an along-strike length of approximately 90.31 ± 4.59 km. Additionally, the vertical extent of the volume

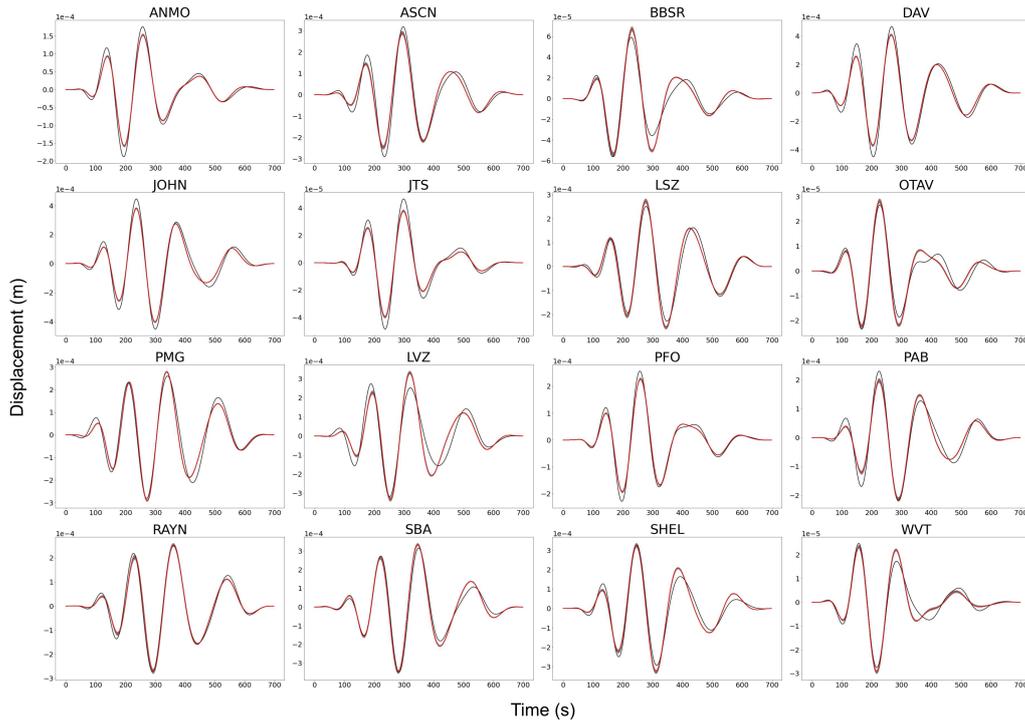


Figure 6. Waveform fits for a subset of the windowed waveforms used in this study. Waveforms are labeled according to the GSN station at which they were recorded. Black waveforms are observations. Gray waveforms are generated using a single solution from the ensemble of solutions from our inversion. Waveforms from each solution in the ensemble are plotted. Red waveforms are generated using the mean solution of the ensemble of solutions from our inversion.

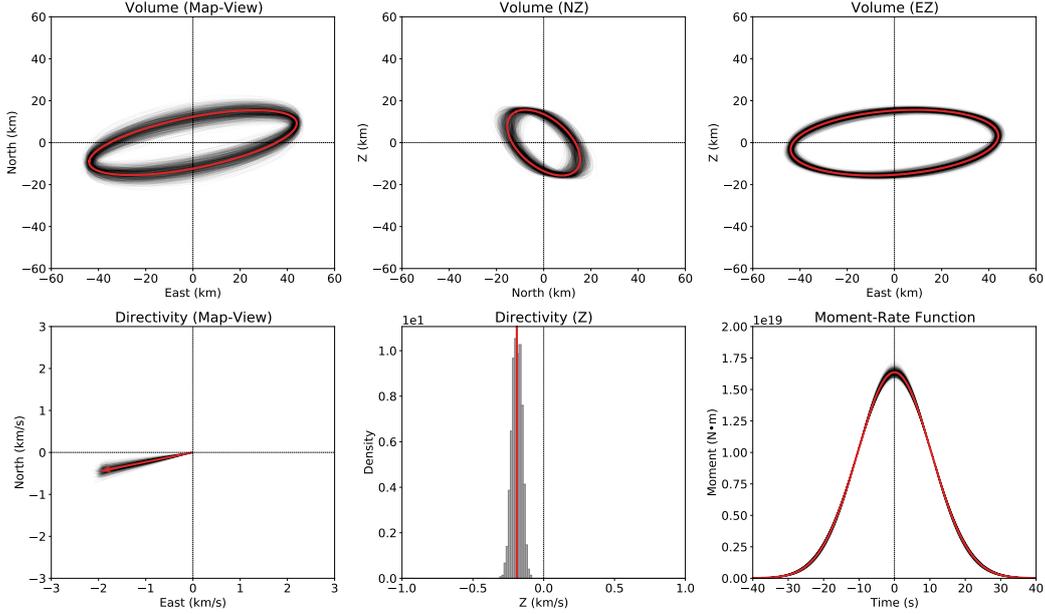


Figure 7. Physically motivated representation of the ensemble of second moment solutions for the 2020 Caribbean event. Top row: Projections of the spatial ellipsoid generated using the eigenvalues and eigenvectors of the spatial covariance matrix of the stress glut distribution. This ellipsoid is projected into map-view (left), into the NZ-plane (middle), and into the EZ-plane (right). Bottom row: Instances of the vector representing the instantaneous velocity of the centroid of the source and instances of the Gaussian approximation of the source-time function of the source. The directivity vectors are projected into map-view (left) and the distribution of Z-components of the directivity vector is plotted as a histogram (middle). Gaussian approximations of the source-time function are plotted relative to the centroid time (right). Gray-scale represents the ensemble of solutions for which, with the exception of the histogram of directivity vector Z-components, darkness represents the density of the plotted solutions. Red represents the mean solution.

326 ellipsoid suggests that 95% of the moment of this event was released in a depth range of
 327 approximately 30.01 ± 3.96 km. The directivity vectors inform both the preferred direction
 328 of rupture and the magnitude of the directivity. As illustrated by Figure 7, this event
 329 is unilateral to the SW and aligned with the Oriente Fault. Also, there is a smaller Z-
 330 directional component in all of the directivity vectors in our ensemble. The magnitude
 331 of the directivity measured in this study is approximately 2.128 ± 0.148 km/s to the SW.
 332 Finally, under the assumption that the moment of this event was released as a Gaussian
 333 distribution in time, the moment-rate functions derived from the temporal second moments
 334 from this solution suggest that 95% of the moment for our earthquake was released in a
 335 span of 41.92 ± 1.28 seconds.

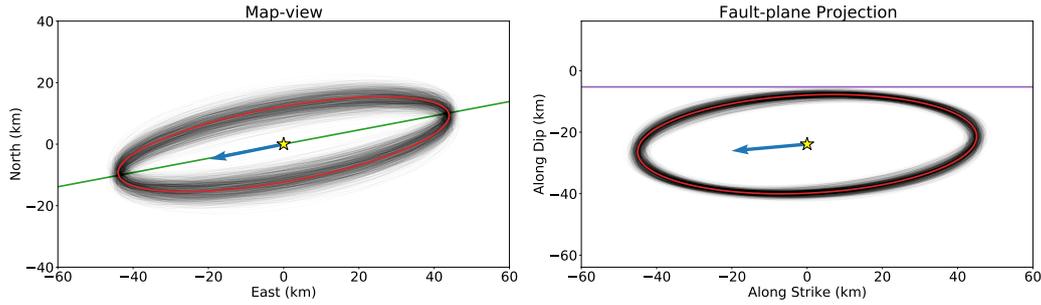


Figure 8. Summary figure of the spatial and directivity features of the 2020 Caribbean Earthquake as derived from the second moment inversion. Left: Map view projection of the second moment ellipsoid and the second moment directivity vector. Gray-scale lines represent the ensemble of solutions and their density. Red line represents the mean solution. Blue vector represents the directivity vector according to the same values shown on the axes but in units of km/s and exaggerated by a factor of 10. Green line represents the true nodal plane from the gCMT solution for the event, which is approximately aligned with the strike of the Oriente Fault. Yellow star represents the centroid position. Right: On-fault projection of the second moment ellipsoid and second moment directivity vector. Line colors match the line colors of the plot to the left. Purple line represents the elevation of the seafloor at the centroid position.

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Discussion

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In general, the ensemble of solutions for the Caribbean earthquake is well constrained and largely agrees with what is already known about the event. As is shown in Figure 8, the largest principal axis of the ellipsoid representation is well-aligned with the Oriente Fault. Also shown in Figure 8, the directivity vector aligns with the Oriente Fault and suggests a rupture that propagates from the NE to the SW. This unilateral behavior is well-constrained in other estimates of directivity for this source. Additionally, the Gaussian source-time functions for this event suggest that the bulk of the moment release occurs within a span of 40 seconds, and nearly all of the moment release occurs within 80 seconds. This source duration agrees reasonably well with other duration estimates for this source (USGS, 2020; Tadapansawut et al., 2021).

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The joint probability distributions shown in Figure 5 suggest that most of the independent parameters of the second moments of the stress glut are uncorrelated. While there are exceptions, this suggests that the lengths of the principal axes of the ellipsoid describing the source volume vary independently. Likewise, changing the magnitude of the directivity along one axis does not necessitate a change of the magnitude of the directivity along another axis. Interestingly, the source duration, determined by the second temporal moment, is uncorrelated with the spatial second moments of the stress glut. This suggests that changing the volume of the source does not imply a change in duration. This non-correlation implies that a change in volume may be correlated with changes in rupture propagation speed and/or directivity. This relationship is partially evidenced by the high correlation between some of the spatial moments with some of the spatiotemporal moments.

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The low dimensional second moment estimate of the 2020 Caribbean Earthquake illustrates the unique potential of this methodology for producing probabilistic estimates of finite source properties with few a priori assumptions on the fault geometry and rupture dynamics. The only requirement is a centroid moment tensor solution, which fits nicely into this framework, as the zeroth and first moments represent the scalar moment and centroid position of the earthquake respectively. In fact, the centroid moment tensor solution may be

364 solved concurrently with the second moment solution, but this introduces nonlinearity and
 365 significant additional computational/numerical complexity. The only constraint required
 366 in the inversion is that the source be non-negative in extent, which does not exclude any
 367 possible source scenarios. However, it is indeed easy to impose additional constraints on the
 368 second moments through the use of informed priors on the inversion parameters. Such in-
 369 formed priors should be imposed with the understanding that the second moments describe
 370 a covariance matrix of a 4-dimensional Gaussian function. That is, informed priors are not
 371 necessarily being placed on the possible source dimensions, but instead are being placed on
 372 the possible Gaussian approximations of the source dimensions.

373 Indeed, the physical representations of these second moment solutions, such as the rep-
 374 resentation of the Caribbean Earthquake shown in Figure 7, should be interpreted with the
 375 understanding that these solutions are probabilistic estimates of Gaussian approximations
 376 of the source characteristics. For example, if a spatial extent ellipsoid solution has a vertical
 377 extent that exceeds the surface of the Earth, this solution is not necessarily unphysical, but
 378 instead may suggest a rupture distribution with a moment release that is biased towards
 379 shallower depths. In fact, Gaussian functions only vanish at infinity. The ellipsoid represen-
 380 tation extends out to 2σ of the spatial distribution of the stress glut, but the choice of the
 381 factor of 2 is to some extent arbitrary. Indeed, for any solution for any earthquake source,
 382 there exists an n such that $n\sigma$ exceeds the surface of the Earth with nonzero probability.
 383 The spatial and temporal components of the second moment solution should be interpreted
 384 from this perspective.

385 With an understanding of the character of these solutions, we can draw probabilistically
 386 motivated conclusions regarding characteristics of the Caribbean Earthquake from these
 387 solutions. For example, there are large discrepancies in the along-strike spatial extent of
 388 this rupture between fault slip distribution studies. The estimate for the extent of the
 389 along-strike rupture most agrees with the USGS finite slip distribution results. That is, we
 390 estimate that most of the moment of the earthquake was released within an along-strike
 391 distance of approximately 90.31 ± 4.59 km.

392 One remarkable insight into this earthquake comes from the estimate of the vertical
 393 spatial extent of the second moment solution. The solution suggests that the moment release
 394 of this earthquake was distributed over a large depth range that spanned approximately
 395 30.01 ± 3.96 km. The GCMT solution for this earthquake places the centroid depth at 23.9
 396 km, which is fairly deep for an oceanic strike-slip earthquake. The large vertical extent
 397 estimate suggests that this earthquake ruptured perhaps much deeper than the centroid
 398 depth, and thus implies that, as illustrated in Figure 8, the seismogenic zone is thick in this
 399 location. This observation may signify that the section of oceanic lithosphere that ruptured
 400 is cold (Abercrombie & Ekström, 2001) and may yield insights into the vertical structure
 401 and heat flow of ocean-continent transform margins.

402 Additionally, the directivity metric, the instantaneous velocity of the centroid of the
 403 source, is quite large at 2.128 ± 0.148 km/s. The instantaneous velocity of the centroid is
 404 identically zero for purely bilateral ruptures and equal to the rupture speed for unilateral
 405 ruptures. We can estimate the maximum rupture speed for this event by dividing the square
 406 root of the largest eigenvalue of the stress glut spatial covariance with the square root of the
 407 stress glut temporal covariance, which yields an average maximum rupture speed of 2.155
 408 km/s. The agreement between the instantaneous velocity of the centroid of this source and
 409 the average maximum rupture speed suggests a near purely unilateral rupture for this event.

410 **Conclusions**

411 In this study, we develop a Bayesian framework for computing second moments of the
412 stress glut of earthquakes using teleseismic data. This framework incorporates a positive-
413 definite constraint under Cholesky decomposition and employs Hamiltonian Monte Carlo
414 sampling to efficiently probe the parameter space. This methodology provides robust esti-
415 mates of uncertainty by sampling the posterior distribution of solutions with dynamic error
416 computation and accounting for the temporal correlation structure in the waveform data.
417 These second moments of the stress glut provide a low-dimensional, physically-motivated
418 representation of source volume, directivity, and duration that requires no *a priori* assump-
419 tions and is repeatable and comparable between events. We verify this methodology using
420 a synthetic test and apply this framework to the 2020 M_w 7.7 Caribbean earthquake. We
421 show that our solutions for this event provide event parameters that largely agree with the
422 available ground truth. We also show that our solutions can be used to resolve ambiguities
423 between higher-order finite source solutions. Finally, we show that our solution may be used
424 to infer source parameters that have historically been difficult to constrain, such as vertical
425 rupture extent.

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