

# Sources of Uncertainty in Atmospheric Drag: The Drag Coefficient

**Sources of Uncertainty in Atmospheric Drag: The Drag Coefficient**  
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**Space Traffic**  
Near Earth orbit is crowded with satellites and debris.  
**Collisions in Space**  
Uncontrolled orbit perturbations can lead to increased collision uncertainty in space.

**How do we mitigate collision risks? Modeling Satellite Drag**  

$$\vec{a}_{drag} = C_D \frac{A}{m} \rho V_{rel}^2$$
 Factors: Acceleration due to the drag force, Drag Coefficient, Area of cross-section, Mass, Atmospheric mass density, Satellite velocity.  
 Atmospheric mass density and the spacecraft drag coefficient are the primary sources of uncertainty in satellite drag.  
 Atmospheric mass density:  
 • Most important for conjunction analysis  
 • Empirical and physics-based models  
 • Variability over many time scales (diurnal, seasonal, SWP (SWP), IOP (IOP))  
 • Responds to solar energy input

**Drag Coefficient**  
 • Historically fixed or best-fit (1-2.2)  
 • Recent efforts use simple physical models  
 • Momentum and energy exchange between the atmosphere and the satellite  
 • Temperature and composition  
 • Satellite geometry and orientation  
 • Scattering dynamics

**Testing Drag Coefficients**  
 • Method to validate existing assumptions and inform current  $C_D$  model uncertainties  
 • Take drag acceleration measurements → compute model drag or drag coefficients → derive and compare normalized mass densities for satellites with similar orbits  
 • Differences in derived densities for satellites of different shapes point to  $C_D$  model inaccuracies

**Impacts**  
 •  $C_D$  models yield inconsistent derived densities at low altitudes, high altitude atmospheric regimes  
 • Drag-derived densities at low pressures are likely underestimated by up to 20% due to current  $C_D$  model re-entrance assumptions. Mature density algorithms are likely underestimated by the same amount.  
 • We rely on  $C_D$  for constructing and validating atmospheric models → current  $C_D$  modeling introduces biases into atmospheric models.

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San Francisco, CA | 9-13 December 2019

# SPACE TRAFFIC

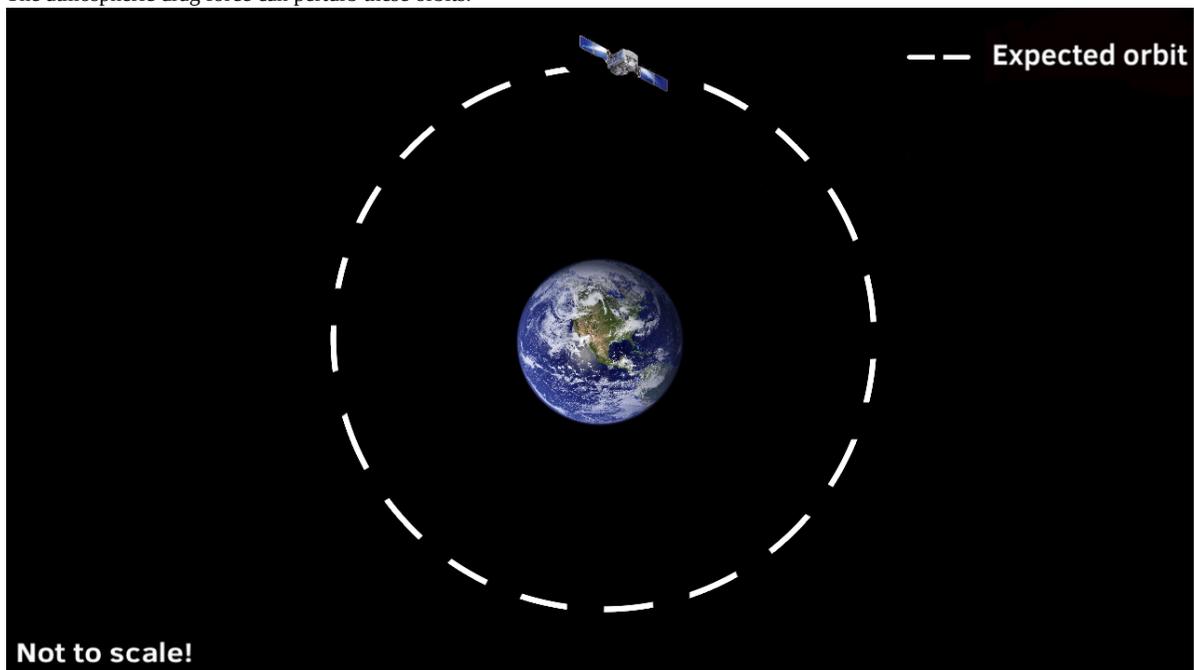
Near-Earth orbit is crowded with satellites and debris.

[VIDEO] <https://www.youtube.com/embed/O64KM4GuRPk?feature=oembed&fs=1&modestbranding=1&rel=0&showinfo=0>

Video credit: Dr. Stuart Grey at University College London

- 1,700+ operational satellites
- 19,400+ debris objects larger than 10 cm orbiting Earth
- 0.5 million debris objects between 1 and 10 cm

The atmospheric drag force can perturb these orbits.



# COLLISIONS IN SPACE

Uncontrolled orbit perturbations can lead to increased collision uncertainty in space.

[VIDEO] [https://www.youtube.com/embed/\\_o7EKlqCE20?feature=oembed&fs=1&modestbranding=1&rel=0&showinfo=0](https://www.youtube.com/embed/_o7EKlqCE20?feature=oembed&fs=1&modestbranding=1&rel=0&showinfo=0)

- In 2009, Iridium 33 and Cosmos 2251 unexpectedly collided at 12 km/s at 800 km altitude
- Collision generated 2100+ debris objects in space
- The number of orbital debris objects is increasing fast

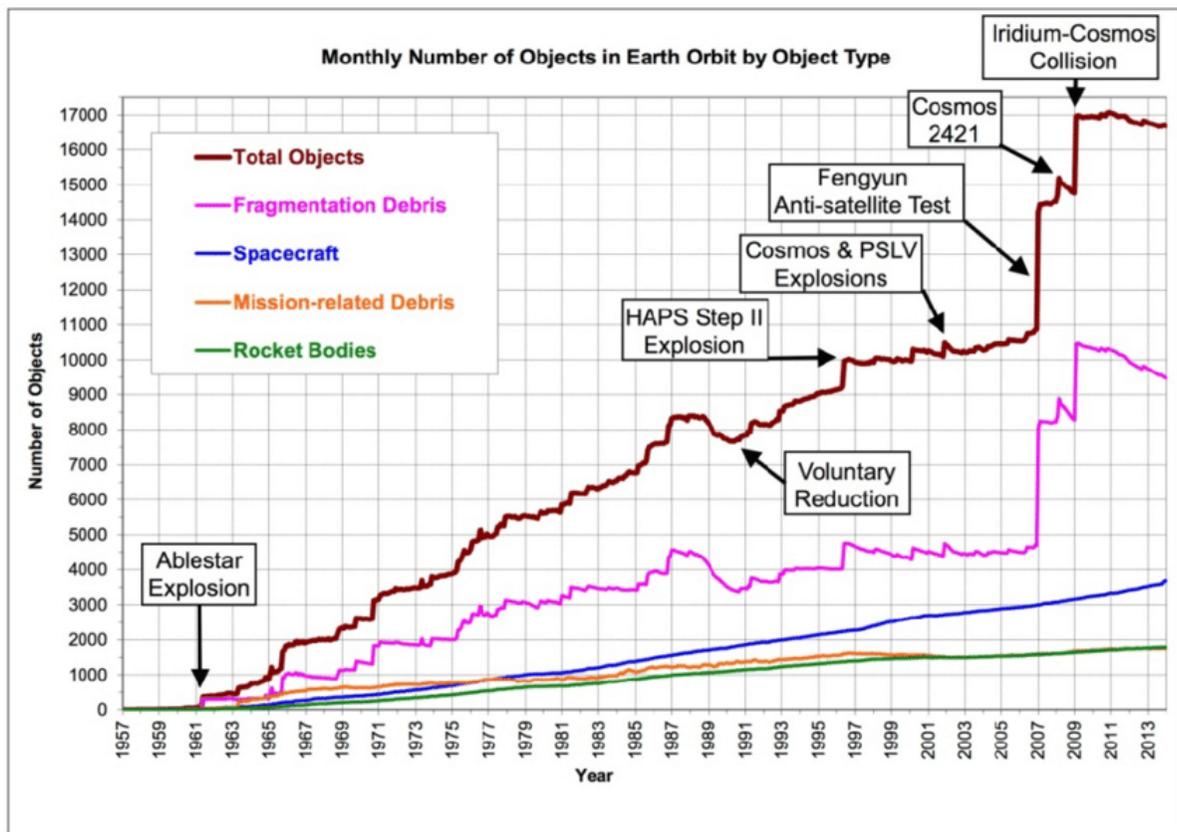
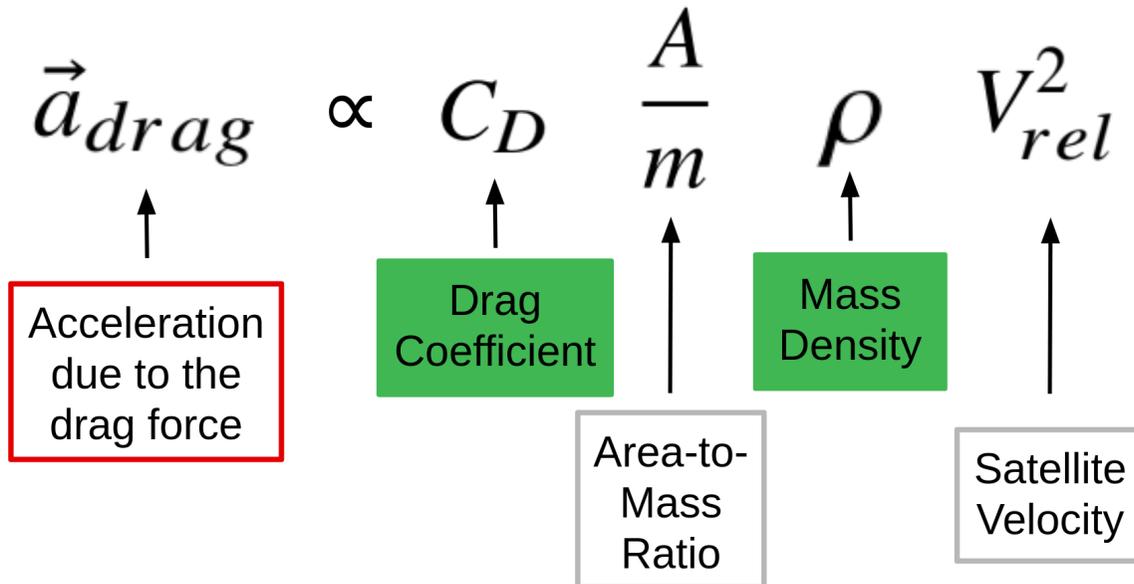


Image credit: NASA Orbital Debris Program (2014), annotated by Mika McKinnon

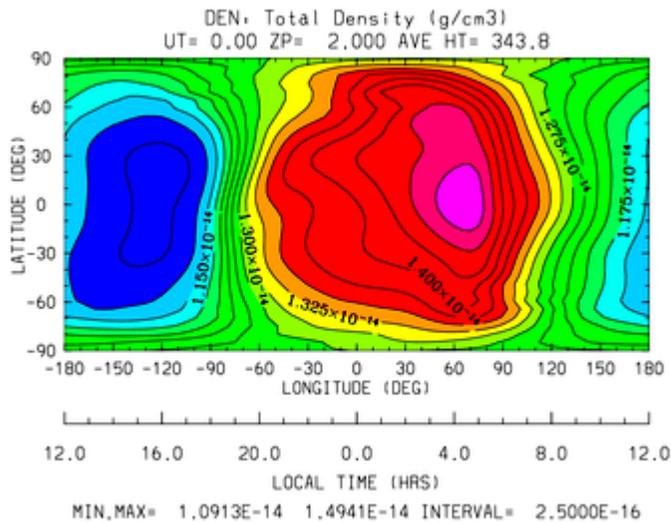
# HOW DO WE MITIGATE COLLISION RISKS? MODELING SATELLITE DRAG



Atmospheric mass density and the spacecraft drag coefficient are the primary sources of uncertainty in satellite drag.

## Atmospheric mass density

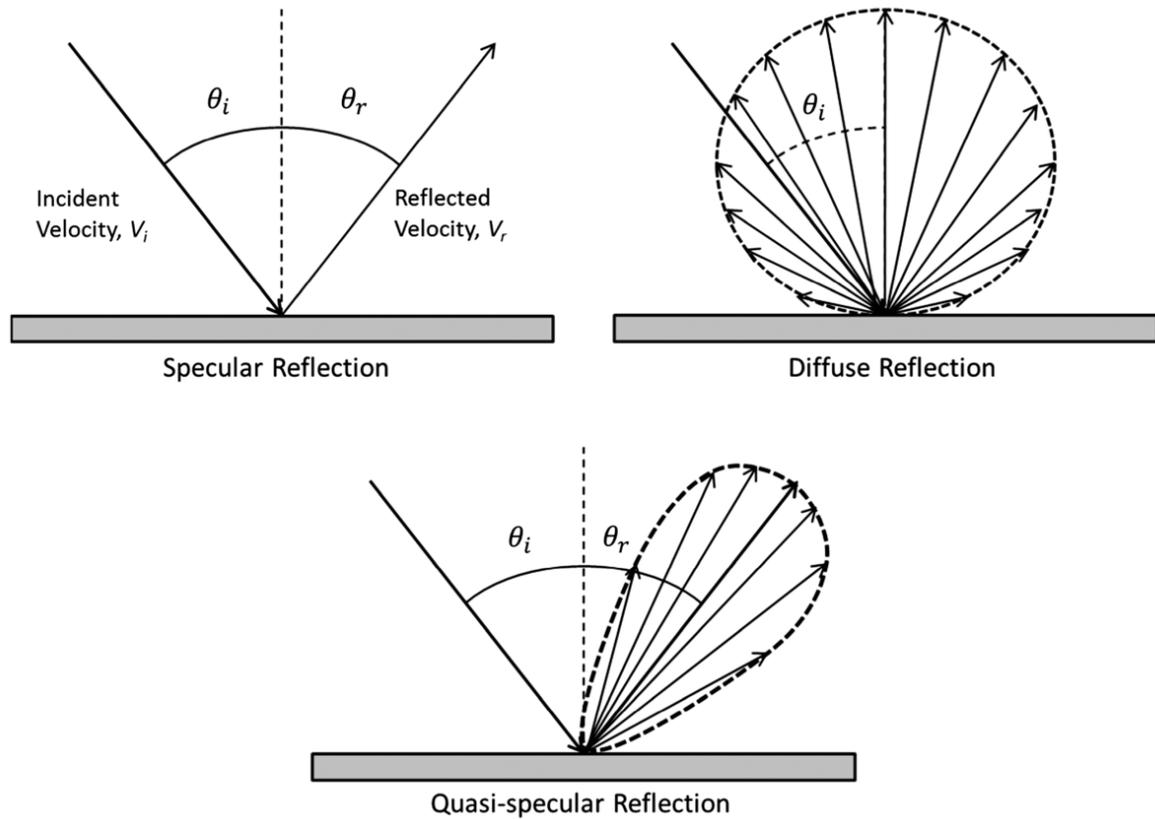
- Most important for conjunction analysis
- Empirical and physics-based models
- Variability over many time scales (diurnal, seasonal, solar cycle)
- Responds to solar energy input



TIE-GCM model density - a global map at 344 km

# DRAG COEFFICIENT

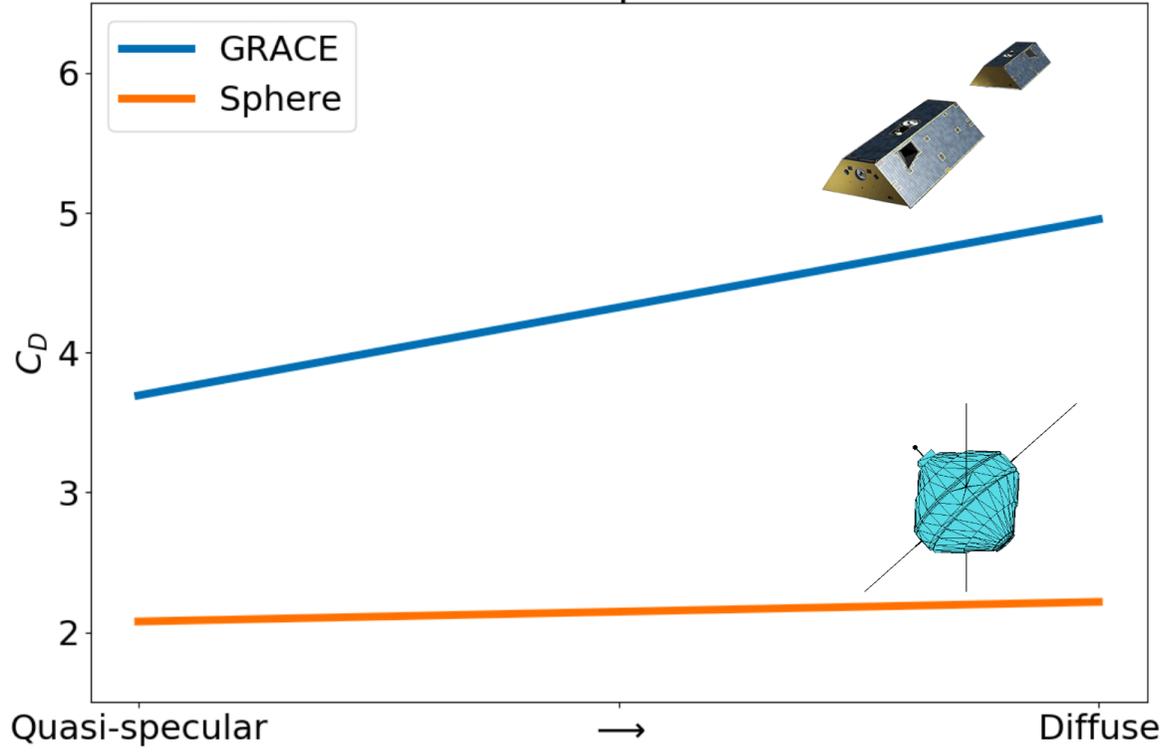
- Historically fitted or fixed ( $\sim 2.2$ )
- Recent efforts use simple physical models
  - Momentum and energy exchange between the atmosphere and the satellite
  - Temperature and composition
  - Satellite geometry and orientation
  - Scattering dynamics



Walker et al. 2014

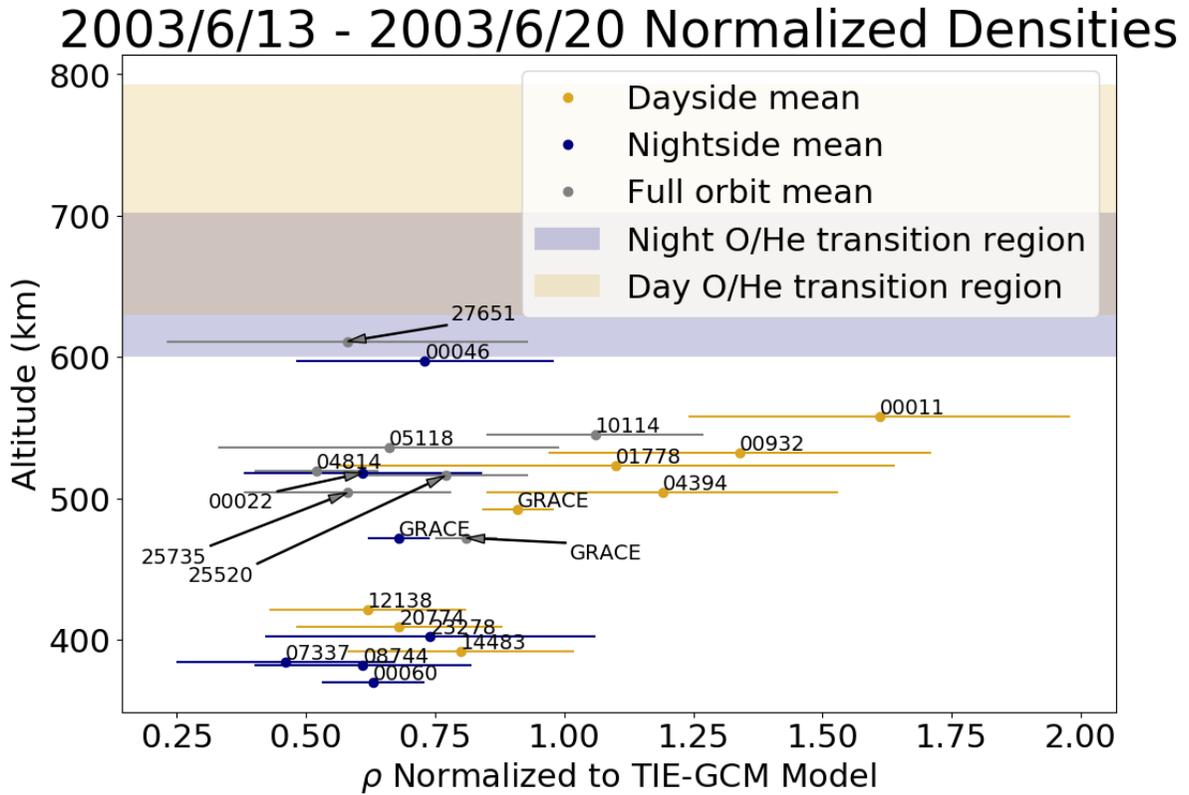
Drag coefficient variability with scattering assumptions:

# Helium Atmosphere, 1500 K

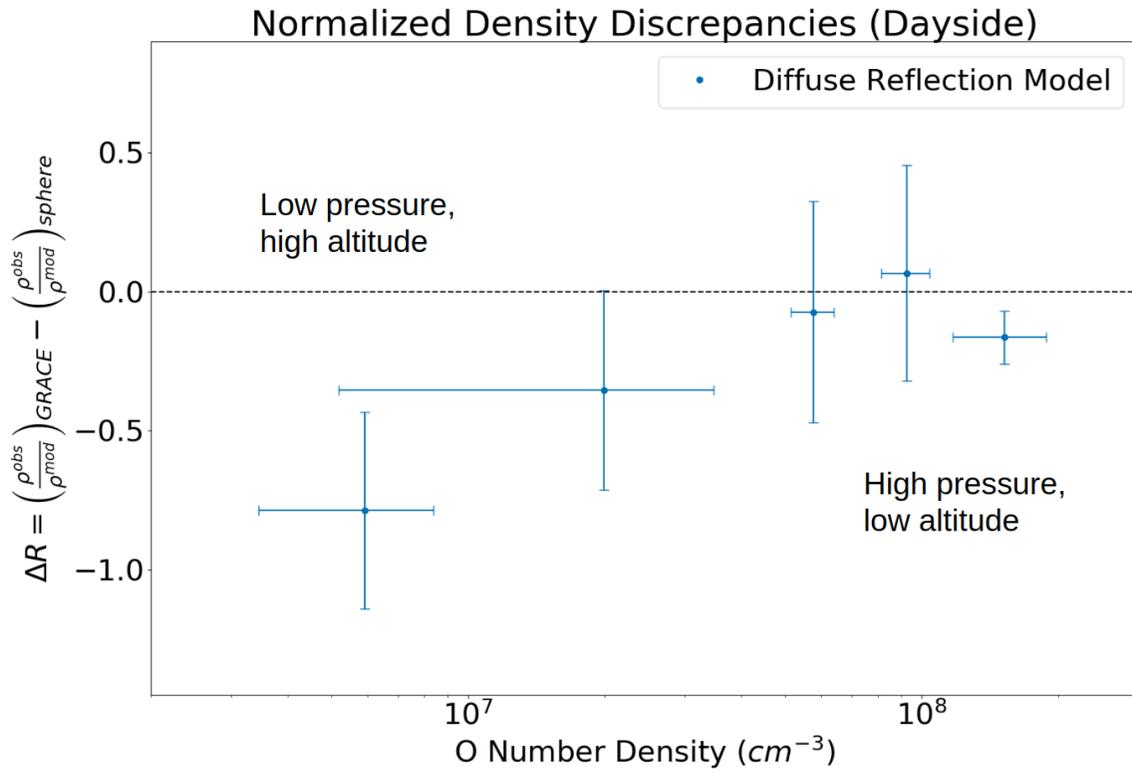


# TESTING DRAG COEFFICIENTS

- Method to validate scattering assumptions and inform current  $C_D$  model uncertainties
- Take drag acceleration measurements  $\rightarrow$  compute, modify and plug in drag coefficients  $\rightarrow$  derive and compare normalized mass densities for satellites with similar orbits
- Differences in derived densities for satellites of different shapes point to  $C_D$  model inconsistencies



- Mean normalized densities for our selected satellites with similar orbits are shown above, spatially organized by their perigee altitudes
- At higher altitudes, derived densities at dayside local times are more inconsistent than nightside densities



- Largest density ratio discrepancies at the dayside low pressure, high altitude atmospheres
- Modeling  $C_D$  with diffuse reflection is inappropriate in this regime → quasi-specular would be a better choice

# IMPACTS

- $C_D$  models yield inconsistent derived densities in low pressure, high altitude atmospheric regimes.
- Drag-derived densities at low pressures are likely underestimated by up to 30% due to current  $C_D$  model scattering assumptions. Helium density estimates are likely underestimated by the same amount.
- We rely on  $C_D$  for constructing and validating atmospheric models → current  $C_D$  modeling introduces biases into atmospheric models

Sorry but time is up!