

Comparison of a Neutral Density Model With the SET HASDM Density Database

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Key Points:

- Thermosphere neutral densities from the EXEMPLAR model are compared with the SET HASDM density database for a 20 year time period
- The use of density totals on spherical shells at several altitudes is an effective way to compare the models
- The EXEMPLAR model performs well at altitudes of 400 km and above where geomagnetic storms produce the largest changes in neutral density

Abstract

The EXospheric TEMeratures on a PoLyhedrAl gRid (EXTEMPALAR) method predicts the neutral densities in the thermosphere. The performance of this model has been evaluated through a comparison with the Air Force High Accuracy Satellite Drag Model (HASDM). The Space Environment Technologies (SET) HASDM database that was used for this test spans the 20 years 2000 through 2019, containing densities at 3 hour time intervals at 25 km altitude steps, and a spatial resolution of 10 degrees latitude by 15 degrees longitude. The upgraded EXTEMPALAR that was tested uses the newer Naval Research Laboratory MSIS 2.0 model to convert global exospheric temperature values to neutral density as a function of altitude. The revision also incorporated time delays that varied as a function of location, between the total Poynting flux in the polar regions and the exospheric temperature response. The density values from both models were integrated on spherical shells at altitudes ranging from 200 to 800 km. These sums were compared as a function of time. The results show an excellent agreement at temporal scales ranging from hours to years. The EXTEMPALAR model performs best at altitudes of 400 km and above, where geomagnetic storms produce the largest relative changes in neutral density. In addition to providing an effective method to compare models that have very different spatial resolutions, the use of density totals at various altitudes presents a useful illustration of how the thermosphere behaves at different altitudes, on time scales ranging from hours to complete solar cycles.

Plain Language Summary

A recently developed computer model predicts the density of the upper atmosphere, in the region known as the thermosphere. Changes in this density following geomagnetic storms can perturb the orbits of the many satellites in this region, leading to imprecise knowledge of their paths and risk of collisions. This model uses measurements of the solar wind and the embedded magnetic field to predict the level of heating in the upper atmosphere, and the resulting expansion of the atmosphere to higher altitudes. In order to test the capabilities of the new model, its calculations were compared with density values derived by an Air Force data assimilation system based on radar tracking of multiple objects in Earth orbit over a 20-year period. The results of this comparison show an excellent agreement, particularly at the higher altitudes where geomagnetic storms have the greatest influence.

1 Introduction

A major focus of space weather research has been on the topic of the mass density of the neutral atoms and molecules in the thermosphere. As the variations in this density perturb the orbital motion of satellites, there has been considerable effort in being able to predict these variations using both empirical models and numerical simulations (Bruinsma et al., 2018; J. Emmert, 2015).

Recently Weimer et al. (2020) had described a new empirical model that calculated exospheric temperatures, the asymptotic limit that the temperature in the thermosphere reaches at high altitudes (Prölss & Bird, 2004), often abbreviated as either T_{ex} or T_{∞} . The temperature inputs to the model were derived from neutral density measurements from multiple satellites. Data from the Challenging Mini-satellite Payload (CHAMP) (Bruinsma et al., 2004) in the years 2002 through 2009 were used, along with the Gravity Recovery and Climate Experiment (GRACE) satellites (Tapley et al., 2004), from 2003 through 2010. These total mass densities were derived from accelerometer measurements of the orbital drag. Additional density data were from the European Space Agency’s Swarm mission (Friis-Christensen et al., 2006), for the time period from 30 Nov 2013 through 2017. Orbital motions obtained from Global Positioning System (GPS) receivers on the spacecraft were used to determine the drag (Astafyeva et al., 2017).

To create the empirical model, the temperature values were sorted into 1620 cells on a geodesic, polyhedral grid. These triangular grid cells have nearly equal areas and their edges have arc lengths of approximately 7° . Multiple linear regression fits were then used to obtain an equation for the exospheric temperature at each cell’s specific location, as a function of the input parameters. For convenience, the unique acronym EXTEMPLAR was given to this method, for EXospheric TEMperatures on a PoLyhedral gRid. The Naval Research Laboratory Mass Spectrometer and Incoherent Scatter radar Extended (NRLMSISE-00) thermosphere model (Hedin, 1991; Picone et al., 2002) was used to convert the density measurements into the exospheric temperatures values that were used for the model development. Afterwards the ”MSIS” model (as commonly known) was used to calculate neutral densities using the exospheric temperatures output from EXEMPLAR for given locations and input parameters. Comparing such density predictions with the original satellite measurements revealed a very good performance by the combination of the EXEMPLAR and MSIS models (hereafter referred to as sim-

ply EXEMPLAR, with the MSIS component assumed). As there were on the order of $\approx 100,000$ data points in each grid cell, the regression formulas that used only six input variable and 16 coefficients could not contain a memory of specific time periods or events, so this was considered a valid test of the model. Nevertheless, a validation trial using an independent dataset is valuable.

The Air Force High Accuracy Satellite Drag Model (HASDM) (Storz et al., 2005) assimilates radar tracking of several dozens of calibration satellites to obtain thermospheric neutral densities. HASDM continuously adjusts coefficients in a modified Jacchia-Bowman 2008 (JB2008) model (Bowman et al., 2008; Tobiska et al., 2008) to match the radar measurements. While the Combined Space Operations Center (CSpOC) of the United States Space Force (USSF) (previously part the Air Force) archives the temperature-corrected coefficients that have been applied to the JB2008 atmosphere, these data are not available to the public. Space Environment Technologies (SET) validates the HASDM outputs under contract and produces a recreation of the densities of the global atmosphere, calling it the “SET HASDM density database” (Tobiska et al., 2021). With approval of the USSF, SET has released the density values for scientific use. These data span two solar cycles, from January 1, 2000 through December 31, 2019. As stated by Tobiska et al. (2021), “all solar cycle, geomagnetic storm and sub-storm, extended solar flare, and thermospheric cooling perturbations are embedded in the data. Because of its accuracy, time resolution, global scale, and information content, the SET HASDM database densities are suitable for use as a new space weather benchmark for atmospheric expansion against which space weather events are measured.” The purpose of this paper is to present the results of a comparison between the EXEMPLAR and HASDM density values. The comparison was run for the entire, 20-year time period. In addition to serving as a useful validation tool, the results have provided helpful insights into the behavior of the thermosphere over the two solar cycles.

2 Recent EXEMPLAR Modifications

Work is presently under way to improve the EXEMPLAR method and develop a real-time, operational program, so the version used in this comparison is similar to but not exactly identical to what was described by Weimer et al. (2020). One difference is that the we now use the newer NRLMSIS 2.0 model (J. T. Emmert et al., 2020) rather than NRLMSISE-00 to calculate the neutral density from the exospheric temperatures.

114 This change will enable use of future updates to the model. It was found that for the
115 same values of exospheric temperature the densities from the NRLMSISE-00 version were
116 generally 2% greater than from the NRLMSIS 2.0 version at 400 km altitude. These lower
117 density values are actually in better agreement with the CHAMP density dataset pro-
118 vided by Mehta et al. (2017), which had been increased by 2% by Weimer et al. (2016)
119 and Weimer et al. (2020) in their calculations. For the development of the most recent
120 version of EXTEMPLAR, all of the exospheric temperature values were recalculated from
121 the original density measurements (Mehta et al., 2017) using NRLMSIS 2.0. The EX-
122 TEMPLAR model that was used in this comparison with the HASDM data is referred
123 to as Version 2.4.2, since is a second-generation model, using the fourth (of several) it-
124 erations that were tested, and using version 2 of the NRLMSIS model.

125 The previous work by Weimer et al. (2020) originally had an objective to deter-
126 mine whether or not measurements of emissions from nitric oxide could be used in pre-
127 dictions of thermospheric temperatures and density. Six formulas or versions of the EX-
128 TEMPLAR calculations were reported. As nitric oxide emission measurements are not
129 presently available in real time, the most recent EXTEMPLAR model is most closely
130 related to the previous Version 6, that used only solar indices and Poynting flux values
131 from an empirical model (Weimer, 2005a, 2005b) that can use historical or real-time so-
132 lar wind and Interplanetary Magnetic Field (IMF) measurements.

133 As before, the exospheric temperatures are calculated separately for each of 1620
134 grid cells; this grid is obtained from a 20-facet icosahedron, in which each facet is sub-
135 divided into 81 equilateral triangles, with the new vertices projected outward to a sphere.
136 A new feature is that the Poynting flux values are delayed in time, with different time
137 delays used for each grid cell. The result is that when the auroral heating suddenly in-
138 creases the temperatures in the grid cells near the pole will increase sooner than at lo-
139 cations near the equator, that have a delayed response. Details about these delays will
140 be reported in a separate publication.

141 The exospheric temperature in each grid cell is obtained from this formula:

$$\begin{aligned}
 T_{\infty N} = & C_0 + C_1 S_{10} + C_2 S_{10} \sin(\theta_D) + C_3 S_{10} \cos(\theta_D) + \\
 & C_4 \sqrt{M_{10}} + C_5 \sqrt{M_{10}} \sin(\theta_D) + C_6 \sqrt{M_{10}} \cos(\theta_D) + \\
 & C_7 \sin(2\theta_D) + C_8 \cos(2\theta_D) + C_9 \sin(\phi_{UT}) + C_{10} \cos(\phi_{UT}) + \\
 & C_{11} S_T(\delta t_N) \sin(\phi_{UT}) + C_{12} S_T(\delta t_N) \cos(\phi_{UT}) + C_{13} S_T(\delta t_N) + \\
 & C_{14} \Delta T \sin(\theta_D) + C_{15} \Delta T \cos(\theta_D) + C_{16} \Delta T
 \end{aligned} \tag{1}$$

143 $T_{\infty N}$ is the exospheric temperature in cell number N . S_{10} and M_{10} are solar proxy in-
 144 dices that were developed for use in the JB2008 density model (Tobiska et al., 2008; Thayer
 145 et al., 2021). Predictions of these indices are produced by SET, with updated values pro-
 146 vided in near real-time. θ_D is calculated using $2\pi DOY/365.25$, which is the Day-Of-Year
 147 date converted to radians, and $\phi_{UT} = 2\pi UT/24$ is the Universal Time (UT) converted
 148 to radians. The C_7 and C_8 terms reproduce semi-annual/inter-annual variations in the
 149 data. $S_T(\delta t_N)$ represents Poynting flux values that have been delayed in time by an amount
 150 that is unique for each grid cell N . Sums of the Poynting flux are actually calculated for
 151 both the Northern and Southern Hemispheres. As described by Weimer et al. (2020),
 152 these totals are combined with a formula that varies smoothly from one hemisphere to
 153 the other:

$$S_T = S_N \sin^2(0.5 * (Latitude + \pi/2)) + S_S \sin^2(0.5 * (Latitude - \pi/2)) \tag{2}$$

155 where S_N and S_S are the total Poynting flux values in the Northern and Southern hemi-
 156 spheres respectively. The latitude is determined from the geometric center of each grid
 157 cell's geometric center. In radians, this latitude ranges from $-\pi/2$ to $+\pi/2$. The Poynt-
 158 ing flux values in this version are smoothed with a boxcar averaging function having a
 159 width of 1 hr, prior to the application of the time delays, that range from 39 min in po-
 160 lar regions to 6.6 hr at low latitudes.

161 The ΔT in (1) represent a global perturbation to the exospheric temperature, that
 162 varies in each grid cell in proportion to C_{14} , C_{15} , and C_{16} . ΔT varies in time, as calcu-
 163 lated with the following numerical difference equation:

$$\Delta T(t_{n+1}) = \Delta T(t_n) - \Delta T(t_n) \left(\frac{\delta t}{\tau_c} \right) + \alpha S_T(t_n) - P_{NO}(t_n) \tag{3}$$

165 In each time step ΔT increases in proportion (α) to the total Poynting flux in both hemi-
 166 spheres (S_T), and decays at an exponential rate with time constant τ_c . ΔT is further
 167 decreased by the radiative, cooling power of nitric oxide emissions, represented by P_{NO} .

168 This power is simulated with use of difference equations, using exactly the same meth-
 169 ods described by Weimer et al. (2020) in equations (10) and (11). As in the previous ver-
 170 sions of the model, the various parameters in the difference equations were optimized through
 171 reiterative fits of the $T_{\infty N}$ from (1) with the temperature values in each cell.

172 3 Density Calculations Using NRLMSIS 2.0

173 It is helpful to review how the MSIS model is used with the EXEMPLAR pro-
 174 gram in order to obtain the neutral densities. This description helps with understand-
 175 ing some of the results that will be shown. The standard input parameters for MSIS
 176 are the geographic coordinates, altitude, date, time, solar $F_{10.7}$ index (both daily and
 177 81-day average), and the daily A_p index of geomagnetic activity. There is an option to
 178 include values of the ap index over six, 3-hour intervals. To obtain the neutral densities

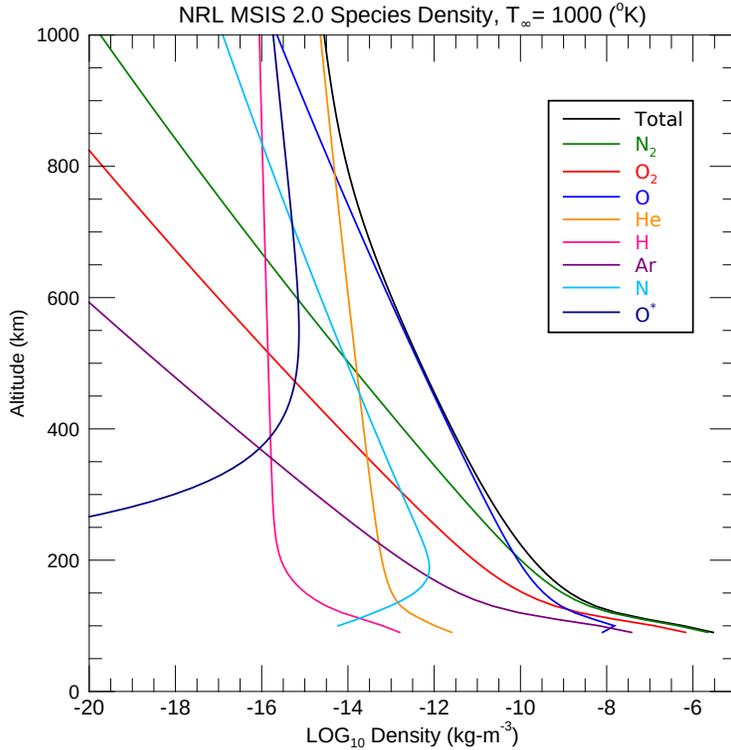


Figure 1. Example of densities from NRLMSIS 2.0 as a function of altitude. All species that are calculated are shown, using colors indicated in the legend. Total density shown in black. Input values were 80° latitude, 0 longitude, on Spring equinox at 0 Universal Time. $F_{10.7}$ index was 120 sfu, and A_p index zero, with exospheric temperature set to 1000°K.

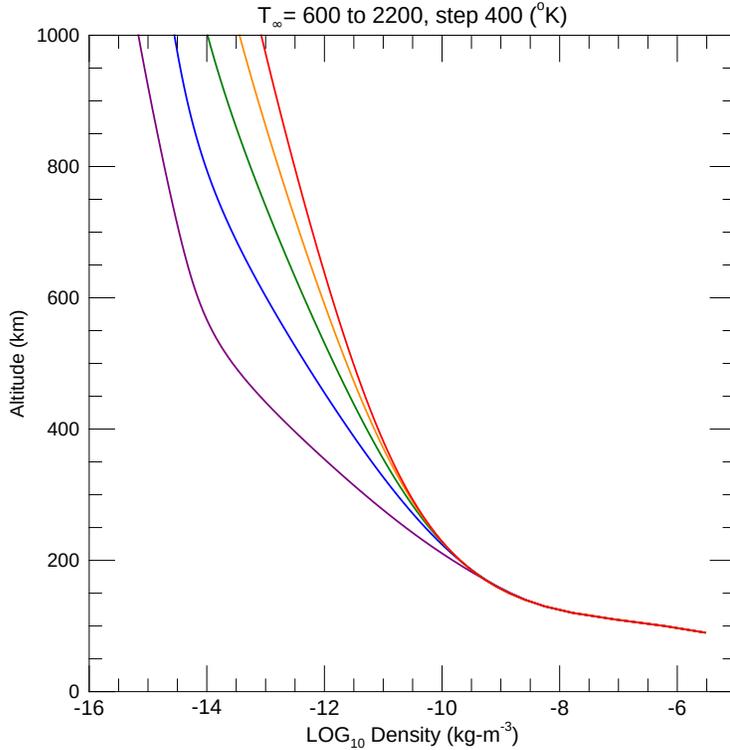


Figure 2. Example of total densities from NRLMSIS 2.0 as a function of altitude, for different values of exospheric temperature. The five lines show results with the exospheric temperature set to 600° , 1000° , 1400° , 1800° , and 2200° K, using the colors purple, blue, green, orange, and red, respectively. Other input parameters are the same as in Figure 1.

179 in the thermosphere, NRLMSIS 2.0 calculates the density of each atomic and molecu-
 180 lar species at a boundary at 122.5 km altitude, along with the temperature and temper-
 181 ature gradient. Normally, MSIS also calculates the exospheric temperature for the given
 182 conditions and coordinates. The boundary conditions and exospheric temperature are
 183 then used to compute the density of each species as a function of altitude, as illustrated
 184 in the example in Figure 1. The species densities are summed to obtain the total den-
 185 sity (the black line in the figure).

186 One shortcoming to the MSIS model is that the actual values of the A_p index are
 187 obtained only after measurements from magnetometers at selected, global locations are
 188 processed. So real-time indices are not available. While there are predictions of A_p avail-
 189 able, they are only estimates. As geomagnetic indices are only an indirect proxy for the
 190 amount of heating that occurs in the polar regions, it is assumed that a model of the Poynt-

ing flux should be more accurate. Furthermore, as the solar wind velocity and IMF values are the primary input needed to obtain the Poynting flux, values can be obtained from real-time measurements having an approximately 1 hr lead time, rather than much later. That is one reason why the use of exospheric temperatures from the EXTEMLAR model is advantageous. It also uses the solar indices S_{10} and M_{10} , that are considered to be more accurate than $F_{10.7}$ alone since they represent the actual solar irradiance being deposited into the thermosphere (Bowman et al., 2008; Tobiska et al., 2008).

With a small modification to the MSIS program, the exospheric temperature that is calculated by the EXTEMLAR model is included as a new input parameter. This temperature (if included) replaces the value that MSIS calculates internally. Figure 2 illustrates the effect of changing the exospheric temperature in MSIS, with densities as a function of altitude shown for temperatures of 600, 1000, 1400, 1800, and 2200°K. Note that at an altitude of 200 km, the exospheric temperature variations have little effect on the total density.

4 Comparison with HASDM

The complete SET HASDM density database is available at <https://spacewx.com/hasdm/>. As indicated by Tobiska et al. (2021), this data “covers the period from January 1, 2000 through December 31, 2019. Data records exist every 3 h during solar cycles 23 and 24. The database has a grid size of $10^\circ \times 15^\circ$ (latitude, longitude) with 25 km altitude steps between 175 and 825 km.” One difficulty is that the resolution of this grid is much more coarse than the approximately 4° spanned by the sides of the 1620, triangular cells in the EXTEMLAR model. As the HASDM model, and the JB2008 model from which it was derived, use spherical harmonics having low order and degree, using smaller grid spacings for the HASDM data archive would not have helped much to improve the resolution of details.

For purpose of comparison, the HASDM grid values were interpolated to the centers of the geodesic grid cells used in EXTEMLAR. An example of such a comparison is shown in Figure 3, from 26 October, 2003 at 6 h Universal Time (UT). In this example (and others not shown) it is apparent that the EXTEMLAR densities have features that do not appear in the HASDM map. On the other hand, comparisons of EXTEMLAR densities with CHAMP and GRACE measurements had indicated that small-scale

222 variations in the density variations do exist (Weimer et al., 2020). Reports on complex,
 223 localized density enhancements had previously been reported on numerous occasions (Schlegel
 224 et al., 2005; Sutton et al., 2005; Bruinsma et al., 2006; Crowley et al., 2010).

225 It was decided that the best way to compare the results from models having dif-
 226 ferent resolutions is to calculate the total density integrated over the surface of a sphere
 227 at a given altitude, and compare these totals. The totals are obtained by taking the den-
 228 sity value in each grid cell and multiplying it by the area of that cell at the selected ra-
 229 dius, and then summing these products. In the case of the HASDM database, the in-
 230 terpolated values are used. As the grid areas were precomputed in units of square ra-
 231 dians, they only needed to be multiplied by the radius squared, in units of m^2 . Since the
 232 densities have units of kg/m^3 , these integrated sums have units of kg/m . In the exam-
 233 ple in Figure 3, the totals are indicated above each map in the upper-right corners. These
 234 sums were computed for every 3 hr interval in the SET HASDM density database, for

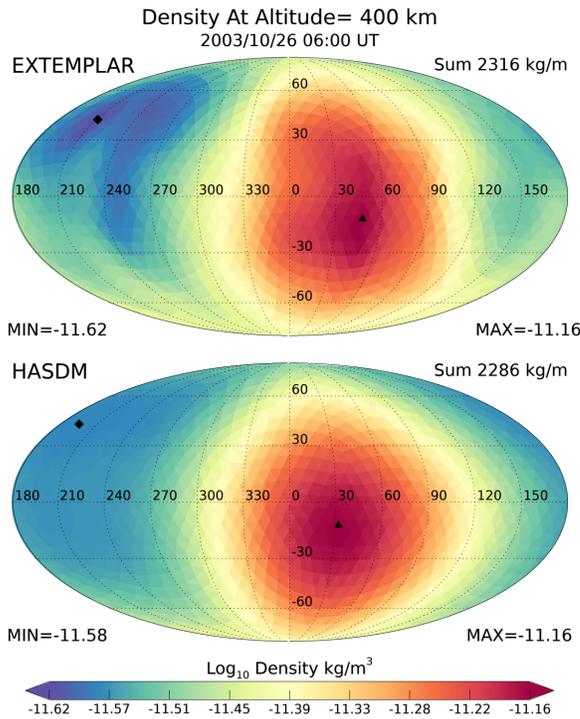


Figure 3. Example of neutral densities from EXTEMLAR (top) and HASDM (bottom), mapped at 400 km altitude. Values are calculated for 26 October, 2003, at 6 h UT. Results from integrating over the surface of a sphere at 400 km altitude are indicated in the upper right corners.

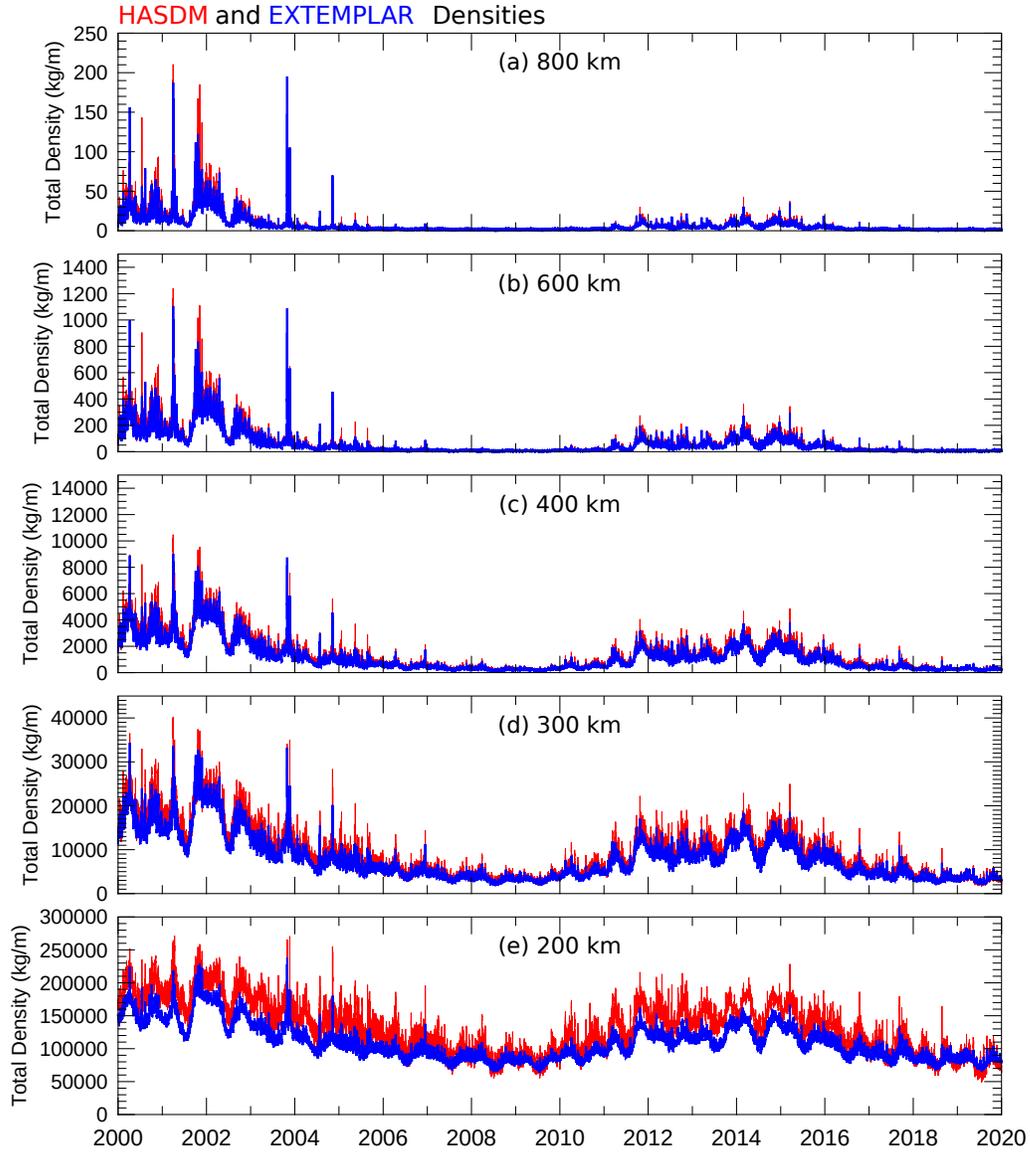


Figure 4. Integrated densities graphed as a function of time, for the time period from 1 January, 2000 through 31 December, 2019. HASDM results are shown in red and EXTEMLAR in blue, for altitudes of 800, 600, 400, 300, and 200 km (top to bottom).

235 the entire 20-year time period, at altitudes of 200, 300, 400, 600, and 800 km. The re-
 236 sults are shown as a function of time in Figure 4. Solar wind velocity and IMF values
 237 measured by the Advanced Composition Explorer (ACE) spacecraft during this time pe-
 238 riod were input to the Poynting flux model used in the EXTEMLAR program.

239 Obviously, the two models are in excellent agreement at most altitudes, although
240 HASDM often has slightly larger values. The differences are largest at 200 km. While
241 both models track the same trends over time, the HASDM values at this altitude tend
242 to be larger than from EXEMPLAR. However, as illustrated in Figure 2, at 200 km
243 altitude the variations in the exospheric temperature have little influence on the den-
244 sity at this altitude; the density values at this altitude are determined entirely by the
245 conditions calculated within the MSIS 2.0 model.

246 A closer look at the time period spanning years 2001 through 2004 is shown in Fig-
247 ure 5, for altitudes 800, 600, 400, and 300 km, from top to bottom. An expanded look
248 at the active time period in late 2003 is presented in Figure 6, covering the time period
249 from 16 October through 24 November 2003, containing two extreme geomagnetic storms.
250 Figure 7 contains another interesting time period, from 1 July 2004 through 30 Novem-
251 ber 2004. The first event within this time has three, successive peaks in the neutral den-
252 sity, followed by an event in November having two larger density peaks in succession. Ad-
253 ditional details can be seen in the Supporting Information document that contains 20
254 separate plots for each of the years in the SET HASDM density database.

255 5 Correlations and Standard Deviations

256 Linear correlation coefficients of the two time series were calculated for each year,
257 with the results shown in Figure 8(a). The blue, red, green, brown, and black lines rep-
258 resent altitudes of 200, 300, 400, 600, and 800 km, respectively. In general, the correla-
259 tions hover around 0.95 for altitudes of 300 to 600 km, while the correlation for 200 km
260 altitude tends to range from only 0.85 to 0.90. The correlation at 800 km is more vari-
261 able, being in the high range in some years, but decreasing in years associated with lower
262 solar activity.

263 Standard deviations are shown in Figure 8(b), using the same line coloring at each
264 altitude. Dividing the deviations by the mean of the HASDM density in each year re-
265 sults in the deviation expressed as a percentage, shown in 8(c). With the exception of
266 the deviations at 800 km before 2005, these percentage errors mostly fall in the range
267 of 10% to 20%.

268 For comparison, Figure 9 contains estimates of the HASDM errors, that were pro-
269 duced by B. Bowman and provided by Tobiska et al. (2021) in a supplement at <https://>

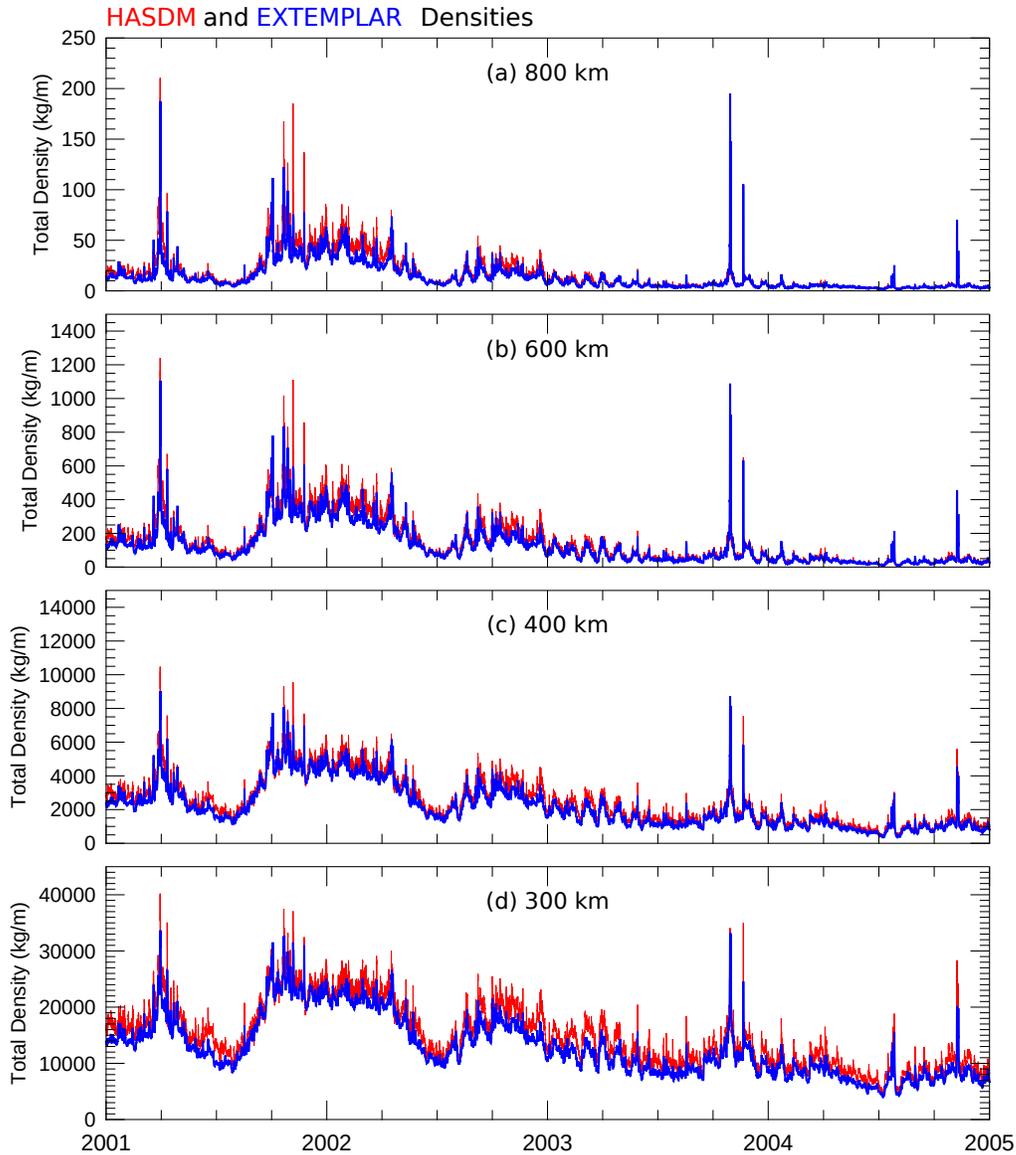


Figure 5. Integrated densities graphed as a function of time, for the time period from 1 January, 2001 through 31 December, 2004. HASDM results are shown in red and EXEMPLAR in blue, for altitudes of 800, 600, 400, and 300km (top to bottom).

270 spacewx.com/hasdm/. These errors are derived within HASDM by a process known as
 271 the Dynamic Calibration Atmosphere (DCA) (Storz et al., 2005). The dots in Figure 8
 272 show the HASDM error for each of the calibration satellites. The HASDM errors tend
 273 to range between 2% and 6% during the peaks in the solar cycle (e.g., Figures 8(a) and
 274 8(c)) and increasing to 4% to 10% when solar activity is low (e.g., Figures 8(b) and 8(d)).
 275 These uncertainties were obtained by comparing the derived HASDM data assimilated

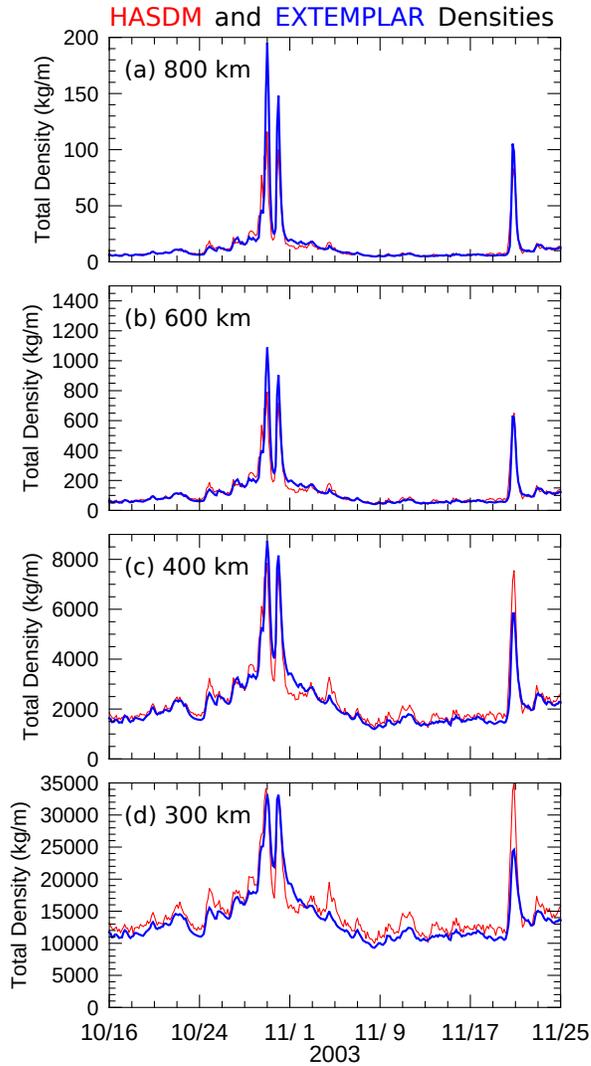


Figure 6. Integrated densities graphed as a function of time, for the time period from from 16 October through 24 November 2003. HASDM results are shown in red and EXTEMLAR in blue, for altitudes of 800, 600, 400, and 300km (top to bottom).

276 densities with sets of densities derived from segmented tracking orbit fits to calibration
 277 satellites. It is seen in these graphs that the errors are largest at 750 km altitude and
 278 above.

279 **6 Discussion**

280 The method in which the neutral densities from different models were integrated
 281 over the surface of a sphere at a given altitude has proven to be an effective way to make

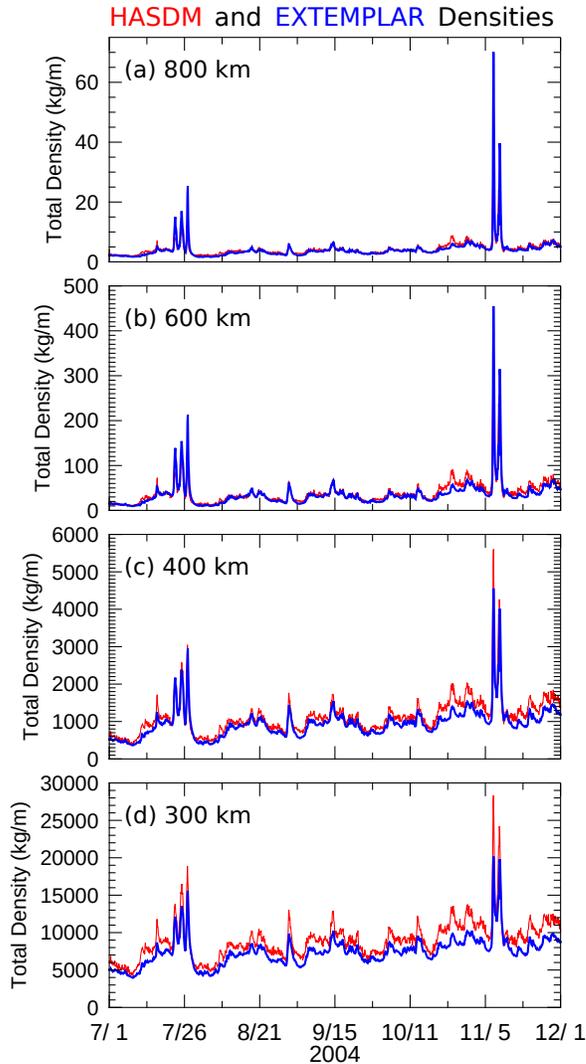


Figure 7. Integrated densities graphed as a function of time, for the time period from from 1 July 2004 through 30 November 2004. HASDM results are shown in red and EXTEMLAR in blue, for altitudes of 800, 600, 400, and 300 km (top to bottom).

282 comparisons. The results show a very good agreement between the EXTEMLAR and
 283 HASDM models on scales ranging from years down to hours. The correlations between
 284 the two models at the smallest scales, as seen in Figures 6 and 7 is excellent. The EX-
 285 TEMPLAR predictions match the HASDM values especially well during the most ex-
 286 treme events, most notably at 400 km altitude and above.

287 The results are helpful for illustrating how the thermosphere behaves over time at
 288 different altitudes, including the annual and solar cycle variability in addition to dur-

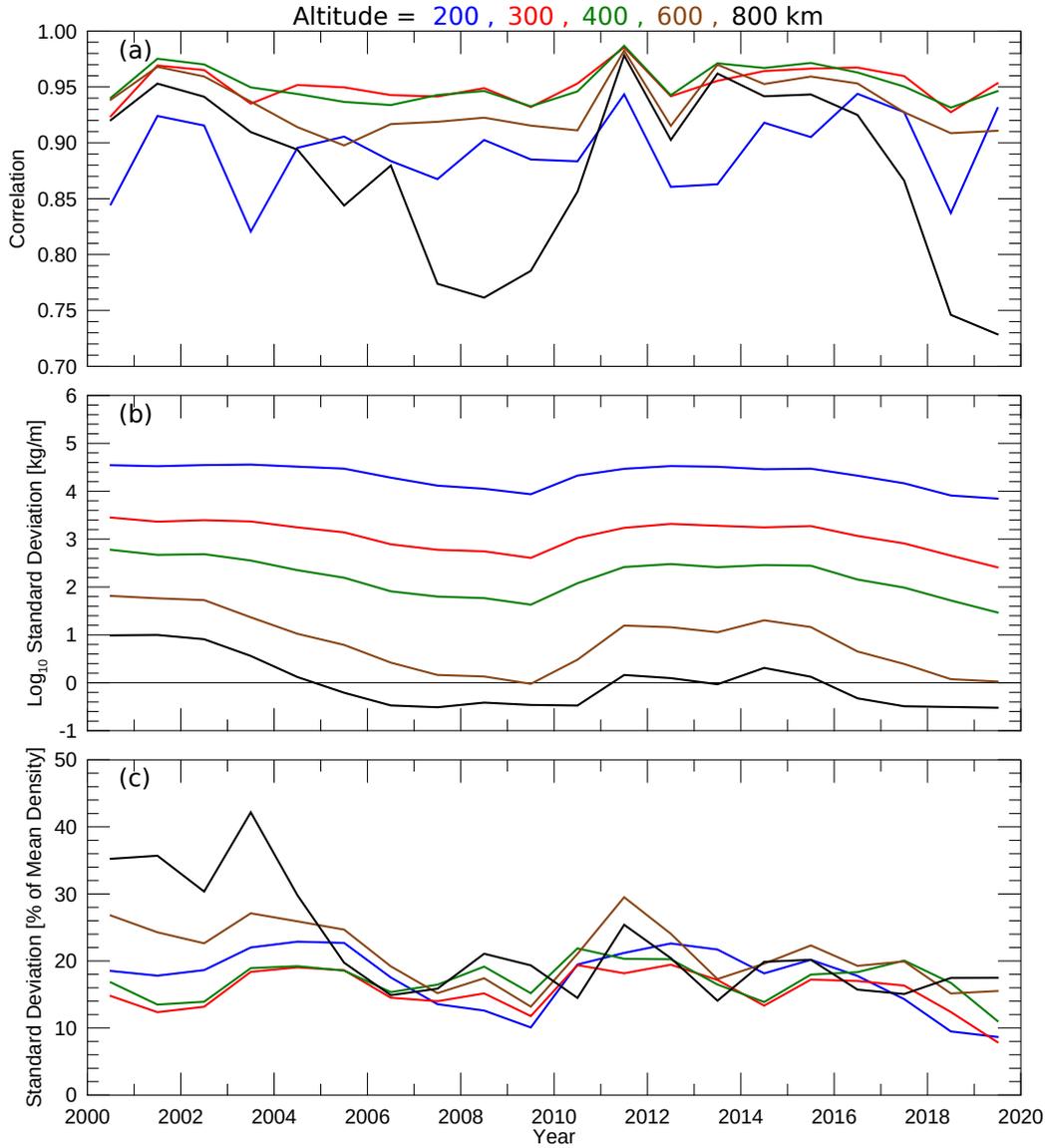


Figure 8. Correlations and Standard Deviations. (a) HASDM and EXEMPLAR correlation coefficients for all years. The blue, red, green, brown, and black lines represent altitudes of 200, 300, 400, 600, and 800 km, respectively. (b) Standard deviations, in units of kg/m, using the same line colors. (c) Standard deviations expressed as a percentage of the mean density in each year.

289 ing major events. It is seen that geomagnetic storms have the greatest influence at higher
 290 altitudes, where there are substantial changes in the neutral density with respect to pre-
 291 storm levels.

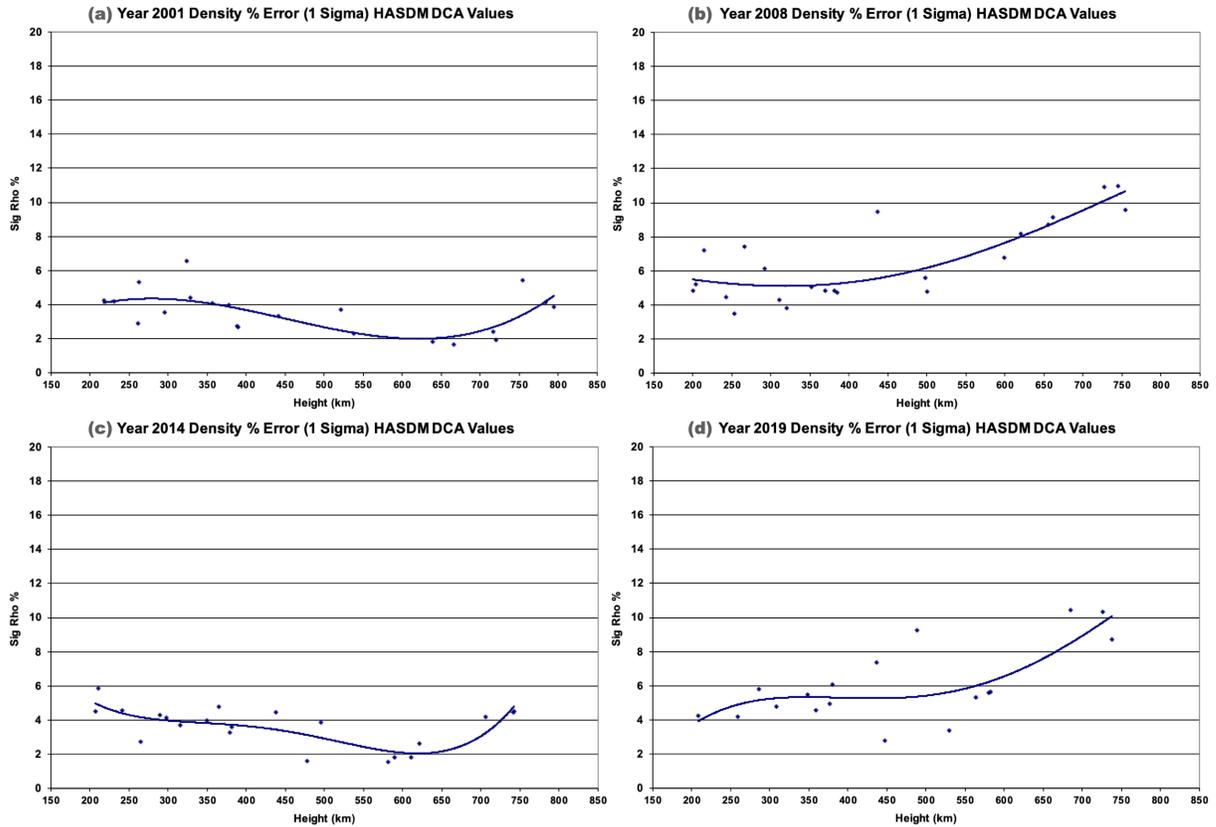


Figure 9. HASDM errors as a function of altitude. The four parts show the errors for the years (a) 2001, (b) 2008, (c) 2014, and (d) 2019.

292 The correlations graphed in Figure 8(a) between 300–600 km are 0.95, which we
 293 consider to be very good. While the correlations at 200 km and 800 km altitude are lower
 294 (in the range of 0.85 to 0.90), they are still reasonable. At 200 km altitude the exospheric
 295 temperature calculations have little effect on the density variations, as shown in Figure 2.
 296 Perhaps the differences could be reduced with some fine tuning of the MSIS 2.0 model,
 297 and we are studying this possibility.

298 Results at 800 km are the most inconsistent. Figure 9 also indicates that the HASDM
 299 errors are the largest here, particularly during times of low solar activity, as shown in
 300 9(b) and 9(d). Solar minimum also coincides with the lowest correlations at 800 km (black
 301 line in 8(a). The plots in the Supporting Information for the years 2007, 2008, 2009, 2017,
 302 2018, and 2019 show that the HASDM system has a nearly flat line during the early and
 303 mid-year time periods when semi-annual variations usually occur, while EXTEMLAR

304 produced the decreases in the density that are the expected signatures of these semi-annual
305 variations (J. T. Emmert & Picone, 2010).

306 At 800 km altitude the EXTEMLAR densities tend to exceed the HASDM val-
307 ues during the large geomagnetic storms, such as in late October in Figure 6(a). This
308 is the cause of the increase in the black line in 2003 in Figure 8(c). It can be argued that
309 the densities calculated by the EXTEMLAR-MSIS combination could more accurate
310 than HASDM at this altitude, since the sparse atmosphere may have little effect on the
311 segmented orbit density fits.

312 It was mentioned earlier that HASDM has a coarse spatial resolution, while satel-
313 lite measurements indicate that the density often varies over distances that are smaller
314 than can be resolved with this model. In cases where the total densities of the two mod-
315 els are in agreement, the EXTEMLAR-MSIS combination is likely more accurate.

316 Oftentimes the integrated densities from HASDM are slightly greater than those
317 from EXTEMLAR. In a comparison between the SET HASDM dataset with the JB2008
318 model and CHAMP and GRACE density measurements, Licata et al. (2021) had found
319 that the HASDM density values were also consistently greater than the values derived
320 from the CHAMP and GRACE accelerometer measurements, while matching better than
321 the JB2008 model. Licata et al. (2021) also found that during the major storm in Oc-
322 tober 2003 (the same event shown here in the first half of Figure 6), while the HASDM
323 dataset had slightly larger densities than measured with CHAMP and GRACE, it did
324 very well at matching the relative changes in density during this period.

325 **7 Conclusion**

326 The comparison of the densities calculated by the EXTEMLAR program with the
327 values in the SET HASDM database show that EXTEMLAR performs very well. As
328 the HASDM assimilation system relies on radar tracking of multiple satellites to derive
329 the neutral densities, it is expected to be very accurate. But it cannot predict the re-
330 sponse of the neutral density to sudden geomagnetic storms in advance, before the track-
331 ing measurements can be obtained. On the other hand, the EXTEMLAR program can
332 use the real-time measurements of the solar wind velocity and IMF to make predictions
333 approximately 1 hr ahead of the thermosphere's response to extreme space weather events.
334 This lead provides time to issue alerts or calculate perturbations to satellite orbits.

335 The EXEMPLAR results shown here had used Level 2 science data from the ACE
 336 satellite, which had a better quality than the real-time data provided by ACE. Presently
 337 the real-time solar wind measurements are provided by the Deep Space Climate Obser-
 338 vatory (DSCOVR). The quality of the real-time DSCOVR solar wind and magnetic field
 339 measurements are just as good as the ACE Level 2 data, so this change will not degrade
 340 the performance of EXEMPLAR. The solar indices are also updated in near real time
 341 by SET.

342 Other developers of thermosphere models, either empirical or numerical, are en-
 343 couraged to compare their neutral density calculations with the SET HASDM density
 344 database in a similar manner. The total, integrated densities shown in Figure 4 are avail-
 345 able in an archive at <https://doi.org/10.5281/zenodo.3xxxxxxx> for the entire, 20
 346 year time period. As mentioned earlier, these data are of value for studying how the neu-
 347 tral density at different altitudes vary on time scales ranging from hours to solar cycles.

348 Acronyms

349 **ACE** Advanced Composition Explorer

350 **CHAMP** Challenging Mini-satellite Payload satellite

351 **DCA** Dynamic Calibration Atmosphere

352 **DSCOVR** Deep Space Climate Observatory

353 **EXEMPLAR** EXospheric TEMperatures on a PoLyhedrAl gRid

354 **GRACE** Gravity Recovery and Climate Experiment satellite

355 **HASDM** High Accuracy Satellite Drag Model

356 **JB2008** Jacchia-Bowman 2008 neutral density model

357 **MSIS** Short abbreviation referring to the either of the NRL density models

358 **NRLMSISE-00** Naval Research Laboratory Mass Spectrometer and Incoherent Scat-
 359 ter radar Extended density model 2000

360 **NRLMSIS 2.0** Naval Research Laboratory Mass Spectrometer and Incoherent Scat-
 361 ter radar model, Version 2.0

362 **SET** Space Environment Technologies

Data Availability Statement

A data archive containing the integrated neutral densities on spherical shells at altitudes of 200, 300, 400, 600, and 800 km, from both EXEMPLAR and HASDM, is available at <https://doi.org/10.5281/zenodo.5177065>. The Supporting Information document contains graphs of these integrated densities for each of the 20 years. The original SET-HASDM database access and supplementary information can be found at <https://spacewx.com/hasdm/>. The ACE level 2 data are available from the NASA archives at <ftp://cdaweb.gsfc.nasa.gov/pub/data/ace>. The solar indices are available from Space Environment Technologies at <http://sol.spacenvironment.net/JB2008/indices>.

(The reserved Zenodo DOI link noted above will become active only after this paper is accepted. A temporary copy of this archive is now at: <https://bit.ly/2X79AZ4>)

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