

# A power equalization RF-PWM method with third and fifth harmonic elimination

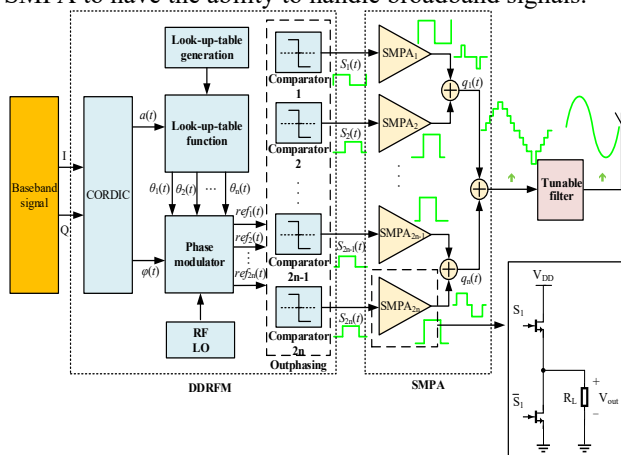
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To reduce the power loss of the SMPA unit, this paper proposes a power equalization RF-PWM method with third and fifth harmonic elimination. Based on the third and fifth harmonic cancellation, this method achieves output power equalization of SMPA by controlling the width of 3-level sub-pulses to be the same. Moreover, the equalization of each switch transistor is realized by outphasing architectures. Finally, the feasibility of the method is verified by simulation results. For QPSK and 16QAM signals with a carrier frequency of 200 MHz, the proposed method achieves the same output power of each SMPA unit.

*Introduction:* With the development of high-speed switching devices, the performance of switched-mode power amplifier (SMPA) is greatly improved. Therefore, all-digital transmitters (ADTx) can be realized, with high-efficiency SMPA. Compared with the traditional analog transmitter, the ADTx [1]-[4] technology has flexible reconfigurability and reprogrammability. Thus, ADTx can meet the needs of software-defined radio (SDR) to achieve most of its functions in the digital domain. Pulse coding [5] is the core of ADTx to achieve high efficiency and linearity. RF-PWM [6] is one of the most suitable pulse coding for ADTx, but its implementation still has challenges. There are plenty of high-order harmonic components in the RF-PWM output pulse, which not only has higher requirements on the tuning filter but also requires the modulator and SMPA to have the ability to handle broadband signals.



**Fig 1** Structure of RF-PWM based ADTx with half-bridge SMPA chip

Switch mode power amplifier (SMPA) is the key device for ADTx to realize RF power amplification in digital domain, which mainly amplifies the pulse generated by the modulator. Based on the GaN based half-bridge SMPA chip [7], the structure of ADTx is shown in Fig. 1. Outphasing architectures are applied to implement RF-PWM and generate pulses to drive half-bridge SMPA chips in Fig. 1. When multiple SMPA units work at the same time, the unbalanced transmission power of GaN devices between and within SMPA units will bring additional loss and distortion [8].

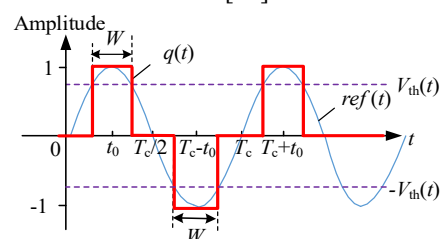
To improve the coding efficiency and dynamic range, the multilevel RF-PWM scheme have been proposed [9]. This scheme can reduce harmonic distortion, but still require high Q filters to suppress harmonics. To eliminate harmonic components and relax the requirement of output filters, a 5-level RF-PWM method has been proposed [10]. The method improves the output filter bandwidth by third harmonic elimination. Based on this 5-level RF-PWM method, a multilevel RF-PWM method with the third and fifth harmonic elimination was presented [11]. The filter bandwidth was greatly improved in this scheme. To reduce the loss caused by power imbalance of the SMPA, a sub-pulse generation method was proposed [8]. The method generated two sub-pulses with equal pulse width, with the third harmonic elimination. Based on existing methods, the proposed power equalization method with the third and fifth harmonic elimination can improve the bandwidth of the filter and realize the power equalization of SMPA.

*The third and fifth harmonic elimination for multilevel RF-PWM:* The multilevel RF-PWM signal can be obtained by the linear superposition of multiple 3-level pulses [10]. The normalized 3-level pulse  $q(t)$  with an arbitrary period of  $T_c$  and a pulse width of  $W$  is shown in Fig. 2 where  $\omega_c = 2\pi/T_c$  is the angular frequency, and  $t_0$  is the pulse center position. The  $(2m+1)$ -level RF-PWM signal can be obtained by linear superposition of  $m$  3-level sub-pulses  $q_n(t)$  ( $n=1, 2, \dots, m$ ), expressed as [10]:

$$p(t) = \frac{1}{m} \sum_{n=1}^m \sum_{k=1}^{+\infty} \frac{4 \sin(\pi k d_n)}{\pi k} \cos[k\omega_c(t - t_n)] \quad (1)$$

where  $k$  is a positive odd number,  $d_n = W_n/T_c$  is the duty cycle of the  $n$ -th 3-level sub-pulse, and  $t_n$  is the pulse center position of the  $n$ -th 3-level sub-pulse.

As the harmonic elimination conditions proposed in [11], the fundamental component of the multilevel RF-PWM signal  $p(t)$  can be proportional to the input RF signal  $S_{in}(t)=a(t)\cos[\omega_c t-\varphi(t)]$  and third and fifth harmonic components are cancelled. The pulse parameter satisfying the conditions are as follows [11]:



**Fig 2** *Diagram of any 3-level pulse with threshold comparison*

$$\begin{cases} \frac{1}{m} \sum_{n=1}^m \varepsilon_n \sin(\pi d_n) \cos[w_c(t-t_n)] = c\pi a(t) \cos[w_c t - \varphi(t)]/4 \\ \sum_{n=1}^m \varepsilon_n \sin(3\pi d_n) \cos[3w_c(t-t_n)] = 0 \\ \sum_{n=1}^m \varepsilon_n \sin(5\pi d_n) \cos[5w_c(t-t_n)] = 0 \end{cases} \quad (2)$$

where  $\varepsilon_n = \pm 1$  is the weighting coefficient, the value is determined by the envelope amplitude  $a(t)$  of the input signal, and  $c$  is the gain of the modulator.

In order to simplify the solution of (2), the simplified condition is given in [11] and eight parameter combinations are obtained. When  $\Delta t_1 = \Delta t_2 = \Delta t$ , the original RF-PWM method is obtained. The pulse width of sub-pulses in this method is different. Thus, it makes the output power of each SMPA unit different and brings power loss to SMPA units. To reduce the loss caused by the power imbalance between SMPA units, the sub-pulse generation method for  $d_1 = d_2 = d_3 = d_4$  is considered. Four parameter combinations of 3-level sub-pulses that satisfy the conditions of third and fifth harmonic cancellation are shown in Table 1. The 3-level sub-pulse  $q_{ij}(t)$  that meets any combination in Table 1 can be generated by threshold comparison [11]. The output waveforms of combinations 1 and 2 are denoted as WI; the waveforms of combinations 3 and 4 are denoted as WII.

**The power equalization method:** The power equalization of SMPA units is realized by sub-pulses with the same pulse width. Under the harmonic elimination conditions, the parameters of 3-level sub-pulses with equal width are shown in Table 1. The structure of SMPA unit which amplifies one 3-level pulse is shown in Fig. 3. The unit consists of two half-bridge SMPA chips [7] driven by 2-level pulses. As shown in Fig. 3, there are four identical switched transistors  $Q_1$ ,  $Q_2$ ,  $Q_3$  and  $Q_4$  driven by 2-level pulses  $S_1$ ,  $S_2$  and their inverse phase signals. To drive the SMPA chips, each 3-level sub-pulse in Table 1 generated by original threshold comparison method needs to be split into two 2-level pulses. Therefore, the threshold comparison is not suitable for 3-level sub-pulses generation.

Outphasing method can generate two 2-level pulses by zero-crossing comparator, and synthesize the two pulses into the required 3-level sub-pulse. As shown in Fig. 4, the outphasing method controls the output 3-level sub-pulses with the same width by controlling the phase shift  $\theta$ . Taking the parameter of 3-level sub-pulse  $q_1(t)$  as an example, the reference signals  $ref_1(t)$  and  $ref_2(t)$  are expressed as:

$$\begin{cases} \theta = \arccos(a(t)) \\ ref_1(t) = \sin(w_c t_1 + \theta) \\ ref_2(t) = \sin(w_c t_1 - \theta) \end{cases} \quad (3)$$

$S_1$  and  $S_2$  is generated by zero-crossing comparator with the input of  $ref_1(t)$  and  $ref_2(t)$  and  $q_1(t) = S_1 + S_2$ . Other 3-level sub-pulses are also generated by outphasing. Therefore, each switched transistor operates in the switch state of 50% duty-cycle, and the power equalization within and between SMPA units is achieved. Thus, the sub-pulses generated by this method can achieve the power equalization and harmonic elimination at the same time.

Table 1. Parameter groups of 3-level pulses when  $d_1 = d_2 = d_3 = d_4$

Parameters of sub-pulses	Simplified conditions	Parameter combination $i$			
		1	2	3	4
Pulse position	$t_1$	$\varphi(t)/w_c + 4T_c/15$	$\varphi(t)/w_c + T_c/15$	$\varphi(t)/w_c + 7T_c/15$	$\varphi(t)/w_c + 2T_c/15$
	$t_2$	$\varphi(t)/w_c + 13T_c/30$	$\varphi(t)/w_c + 7T_c/30$	$\varphi(t)/w_c + 11T_c/30$	$\varphi(t)/w_c + T_c/30$
	$t_3$	$\varphi(t)/w_c - 4T_c/15$	$\varphi(t)/w_c - T_c/15$	$\varphi(t)/w_c - 7T_c/15$	$\varphi(t)/w_c - 2T_c/15$
	$t_4$	$\varphi(t)/w_c - 13T_c/30$	$\varphi(t)/w_c - 7T_c/30$	$\varphi(t)/w_c - 11T_c/30$	$\varphi(t)/w_c - T_c/30$
Duty-cycle	$d_1 = d_2 = d_3 = d_4$	$1/2 \cdot \arcsin(a(t))/\pi$			

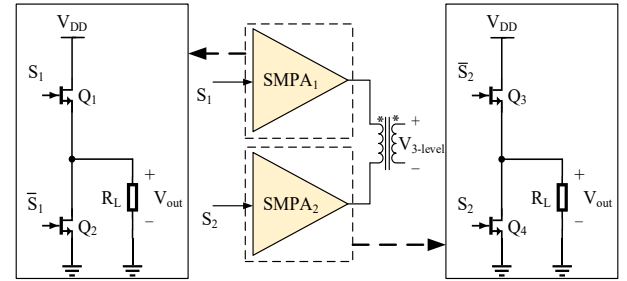


Fig 3 The SMPA unit structure that generates 3-level pulses

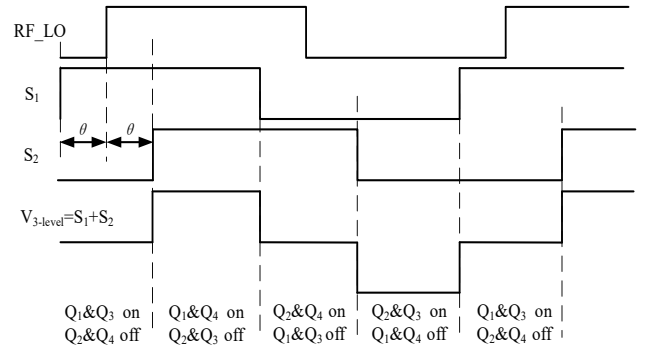
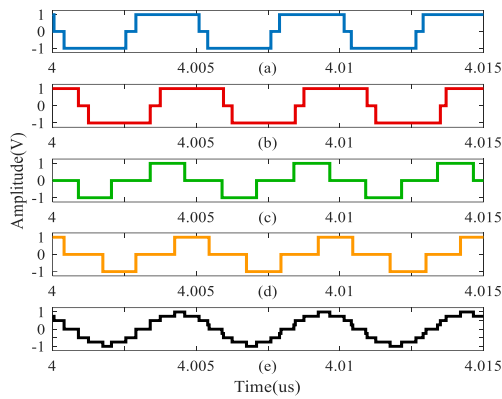


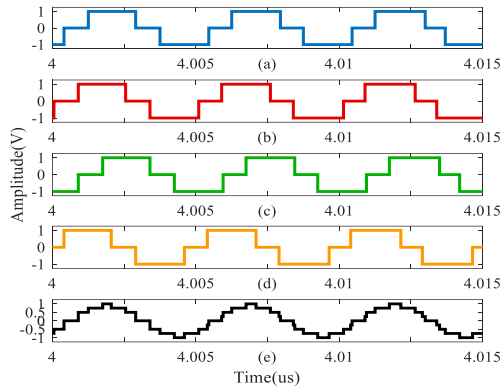
Fig 4 Diagram of 3-level pulses generated by outphasing and the states of four switched transistor in one SMPA unit

**Simulation results and analysis:** To verify the feasibility of the proposed power equalization scheme and analyze its influence on signal performance, two different methods are simulated with single tone signal and complex modulation signals as input. The original multilevel RF-PWM method in [ ] is denoted as SI and the power equalization method for multilevel RF-PWM is denoted as SII.

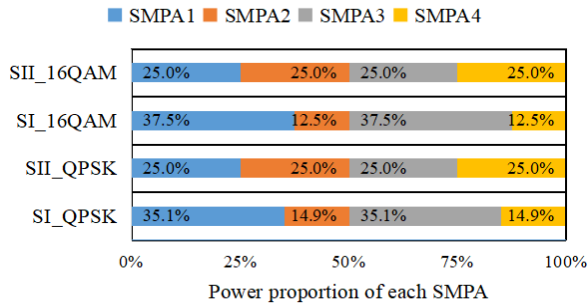
A single-tone signal with a 200-MHz carrier is used as the input signal for different schemes. Fig. 5 and Fig. 6 show the waveforms of the sub-pulses and output RF-PWM signals of SI and SII. The output multilevel RF-PWM signals of the two methods are both WII. Meanwhile, the width of each sub-pulse of the SII is the same, which realizes the control of the sub-pulse width and equalizes the transmission power of the SMPA.



**Fig 5** Waveform of the output RF-PWM signal and four sub-pulses at a 200-MHz carrier under SI



**Fig 6** Waveform of the output RF-PWM signal and four sub-pulses at a 200-MHz carrier under SII



**Fig 7** The power proportion of each SMPA under SI and SII

In order to analyze the influence of variable envelope on the power equalization effect of SII, the QPSK and 16QAM signal with carrier frequency of 200MHz is used as input. The power of each SMPA unit in the two schemes is calculated under the load of 50Ω. Under 3.70-dB PAPR QPSK signal and 5.27-dB PAPR 16QAM signal, the power proportion of the SMPA units of the two methods is shown in Fig 7. With the increase of PAPR, the power imbalance increases between the four SMPA units in SI and the output power proportion of the high-voltage SMPA unit decreases. Meanwhile, SII achieves power equalization among four SMPA units without the influence of PAPR.

**Conclusion:** A power equalization method for multilevel RF-PWM with third and fifth harmonic elimination is

proposed in this paper. the power equalization of the SMPA units is realized by 3-level sub-pulses with equal width. Each 3-level sub-pulse is generated by outphasing method. Meanwhile, outphasing architectures implement the equal switched time of switch transistors. For the 16QAM signal with a 200-MHz carrier and a 5.27-dB PAPR, the proposed method has a good suppression effect of third and fifth harmonics under the output waveform WII.

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## References

1. Yang, S.Y., Yang, J., Huang, L.Y., Bai, J.L., Zhang, X.Y.: "A Dual-Band RF All-Digital Transmitter Based on MPWM Encoding," *IEEE Trans. Microw. Theory and Techn.*, **70**(3), 1745-1756(2022).
2. Nuyts, P.A.J., Reynaert, P., Dehaene, W.: "Frequency-domain analysis of digital PWM-based RF modulators for flexible wireless transmitters," *IEEE Trans. Circuits Syst. I, Reg. Papers*, **61**(1), 238–246(2014).
3. Dinis, D.C., Rui, F.C., Oliveira, A.S.R.: "A fully parallel architecture for designing frequency-agile and real-time reconfigurable FPGA-based RF digital transmitters," *IEEE Trans. Microw. Theory and Techn.*, **66**(3), 1489-1499(2018).
4. P. A. J. Nuyts, P. Reynaert, and W. Dehaene, "Frequency-domain analysis of digital PWM-based RF modulators for flexible wireless transmitters," *IEEE Trans. Circuits Syst. I, Reg. Papers*, vol. 61, no. 1, pp. 238–246, Jan. 2014.
5. Chen, Z., et al.: "Mathematical Model and Reference Frequency Optimization for Digital Dual-Band Pulsewidth Modulation," in *Proc. IEEE MTT-S Int. Wirel. Symp. (IWS)*, 1-3(2020)
6. Raab, F.H.: "Radio frequency pulsewidth modulation," *IEEE Trans. Commun.*, **21**(8), 958–966(1973).
7. Lai, L., et al., "Monolithic Integrated High Frequency GaN DC-DC Buck Converters with High Power Density Controlled by Current Mode Logic Level Signal," *Electronics*, **9**(9), 1540(2020).
8. Zhou, Q., Zhu, L., Fu, H., Wei, Z., Zhang, J.: "A Sub-pulses Generation Method for Third-Harmonic Elimination of 5-level RF-PWM," in *Proc. IEEE Int. Workshop Electromagn.: Appl. Stud. Innov. Compet. (iWEM)*, 1-3(2021)
9. Francois, B., Nuyts, P.A.J., Dehaene, W., Reynaert, P.: "Extending dynamic range of RF PWM transmitters," *Electron. Lett.*, **49**(6), 430–432(2013).
10. Yao, F., Zhou, Q., Wei, Z.: "A novel multilevel RF-PWM method with active-harmonic elimination for all-digital transmitters," *IEEE Trans. Microw. Theory and Techn.*, **66**(7), 3360–3373(2018).
11. Fu, H., Zhou, Q., Zhu, L., Wei, Z., Zhang, J.: "A Pulse Waveform Control Method for Multiple Harmonic Elimination of Multilevel RF-PWM," in *Proc. IEEE MTT-S Int. Wirel. Symp. (IWS)*, 1-3(2022)