

1 **On the origin and structure of haplotype blocks**

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16 **Abstract**

17 The term “haplotype block” is commonly used in the developing field of haplotype-based  
18 inference methods. We argue that the term should be defined based on the structure of the  
19 Ancestral Recombination Graph (ARG), which contains complete information on the ancestry of  
20 a sample. We use simulated examples to demonstrate key features of the relation between  
21 haplotype blocks and ancestral structure, emphasising the stochasticity of the processes that  
22 generate them. Even the simplest cases of neutrality or of a “hard” selective sweep produce a rich  
23 structure, which is missed by commonly used statistics. We highlight a number of novel methods  
24 for inferring haplotype structure as full ARG, or as a sequence of trees. While some of these new  
25 methods are computationally efficient, they still lack features to aid exploration of the haplotype  
26 blocks, as we define them, thus calling for the development of new methods. Understanding and  
27 applying the concept of the haplotype block will be essential to fully exploit long and linked-read  
28 sequencing technologies.

29

30 **Keywords**

31 haplotype block, ancestral recombination graph, haplotype-based methods, coalescent

32

33 **Introduction**

34 One of the breakthroughs of long and linked-read sequencing technologies is the  
35 emergence of new methods for obtaining reliable haplotype information for large data sets (Meier  
36 et al., 2021). Although most studies of genome-wide variation still focus on SNP data, we are  
37 approaching the stage where population-scale haplotype information will be widely available for  
38 organisms across the tree of life. In light of this shift from site-based to haplotype-based inference,  
39 this article considers one of the fundamental concepts for haplotype-based inference—the  
40 definition of the haplotype block.

41 “Haplotype” and “Haplotype block” are widely used terms in evolutionary genetics, and  
42 have increased in importance across many disciplines (Delaneau et al., 2019; International  
43 HapMap Consortium, 2005; Leitwein et al., 2020). An important, but often overlooked fact, is that  
44 populations evolve through changing frequencies of blocks of the genome, rather than of  
45 individual sites. Therefore, we should be most interested in understanding the trajectories of the  
46 underlying haplotypes, yet these are not fully reflected by the SNPs that we see (Castro et al.,

2019; Clark, 2004). Thus, disentangling the evolutionary history underlying genomic patterns can be challenging using solely site-based statistics. For example, while whole-genome scans for signatures of selection can reveal loci that affect fitness (Poelstra et al., 2014; Tavares et al., 2018), it is hard to determine the actual causes of these signals (Burri, 2017; Grossman et al., 2010; Ravinet et al., 2017; Rockman, 2012; Stankowski et al., 2019; Tavares et al., 2018; Wolf & Ellegren, 2017). For example, shifts in polygenic scores from genome-wide association studies (GWAS) can be misinterpreted to be signals of selection instead of being artifacts of population structure (Berg et al., 2019; Novembre & Barton, 2018; Sella & Barton, 2019). Similarly, methods for estimating population density and gene flow struggle to distinguish among a virtually infinite number of possible population structures (Richardson et al., 2016; Sousa et al., 2011; Whitlock & Mccauley, 1999).

By accounting for haplotype structure, it should be possible to make inferences more accurate and more efficient. Haplotypes carry information not only from *mutation* but also from *recombination*, which provides an additional ‘clock’ that can help to reveal past events. Primarily for these reasons, there has been a steady increase in analytic methods that aim to infer haplotype structure from sequence data, or that exploit haplotype structure to make inferences about selection, gene flow, and population structure.

Although there has been significant progress toward the broader use of haplotype information in empirical studies, much of this work is fragmented across many subfields, including evolutionary and conservation genetics (Leitwein et al., 2020), human and medical genetics (Crawford & Nickerson, 2005), and animal and plant breeding (Bhat et al., 2021; Mészáros et al., 2021). As a result, there is often little consensus on how haplotype blocks are defined. More practically, this disparity complicates comparison of results, and may preclude insights that may otherwise arise by combining different perspectives.

The main goal of this paper is to critically examine the fundamental definition of the haplotype block. Specifically, we propose a definition of haplotype block based on the full genealogy, represented by the Ancestral Recombination Graph (ARG). Using simulations of simple but general scenarios, we explore how the characteristics of haplotype blocks relate to the origin of the samples and segregating SNP variation. We then discuss how the proposed definition relates to practical inference methods and their applications in large-scale population studies. We consider how different methods make use of haplotype information and infer haplotype blocks, their underlying assumptions and respective limitations.

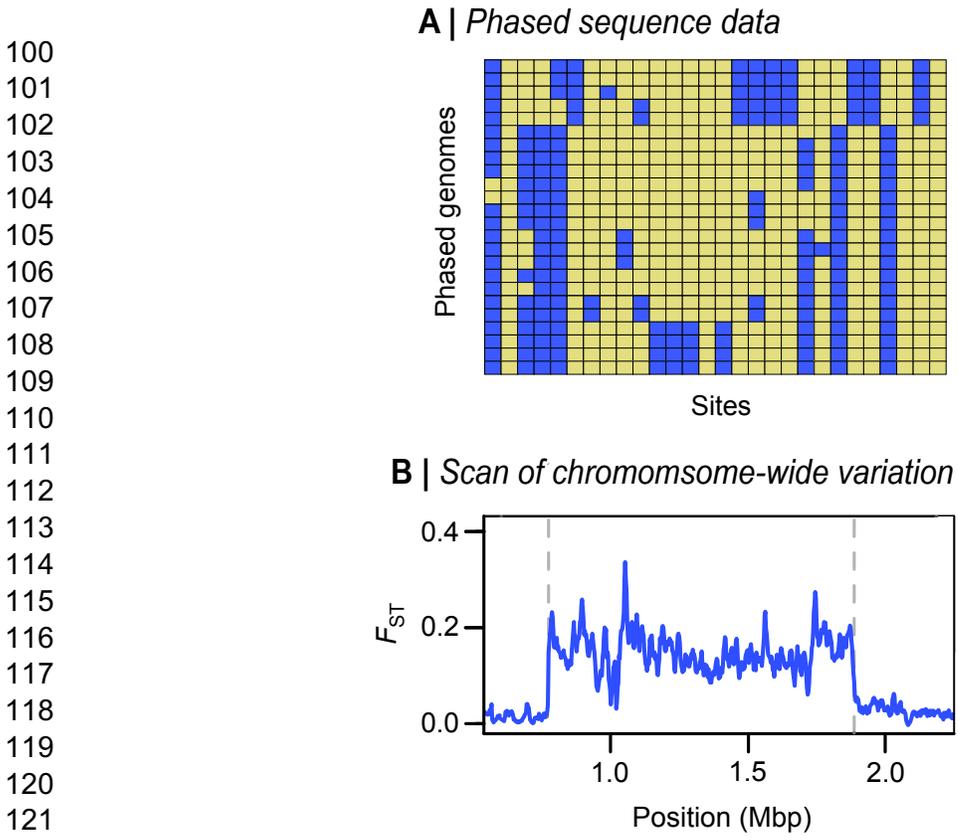
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## 80 **Defining haplotype blocks**

81 A haplotype has a clear definition: it is simply a haploid genotype (for example, the  
82 genotype of the sperm or egg). In contrast, the term “haplotype block” is used widely, but in many  
83 different ways (Al Bkhetan et al., 2019; Clark, 2004; International HapMap Consortium, 2005;  
84 Schwartz et al., 2003; Taliun et al., 2014; Zhang et al., 2002). Our understanding of this term must  
85 depend on the processes of coalescence and recombination that generate haplotype structure. With  
86 this in mind, we contrast alternative definitions, and settle on one, which is based on branches in  
87 the underlying genealogy.

88 In sequence data, we usually observe the diploid genotypes; resolving them into the two  
89 haploid genotypes is termed “phasing”. With  $n$  heterozygous sites, there are  $2^n$  possible pairs of  
90 haplotypes - more than a million with just  $n = 20$ . However, there are usually just a few haplotypes,  
91 due to linkage disequilibrium (LD) across polymorphic sites, which often produces strong  
92 haplotype structure. This allows “statistical phasing”, through which one reconciles diploid

93 genotypes into the underlying haplotype pair (Browning & Browning, 2011). Looking across  
 94 individuals in larger genotype panels, the more frequent haplotypes often appear as stretches of  
 95 shared, “banded” blocks of SNPs (Fig. 1A) (Patil et al., 2001). This can be especially striking when  
 96 different haplotypes become fixed across populations, which can produce block-like patterns in  
 97 data even when individual haplotypes cannot be observed (Fig. 1B); in some cases, the outstanding  
 98 regions have been referred to as ‘haploblocks’ (Todesco et al., 2020).  
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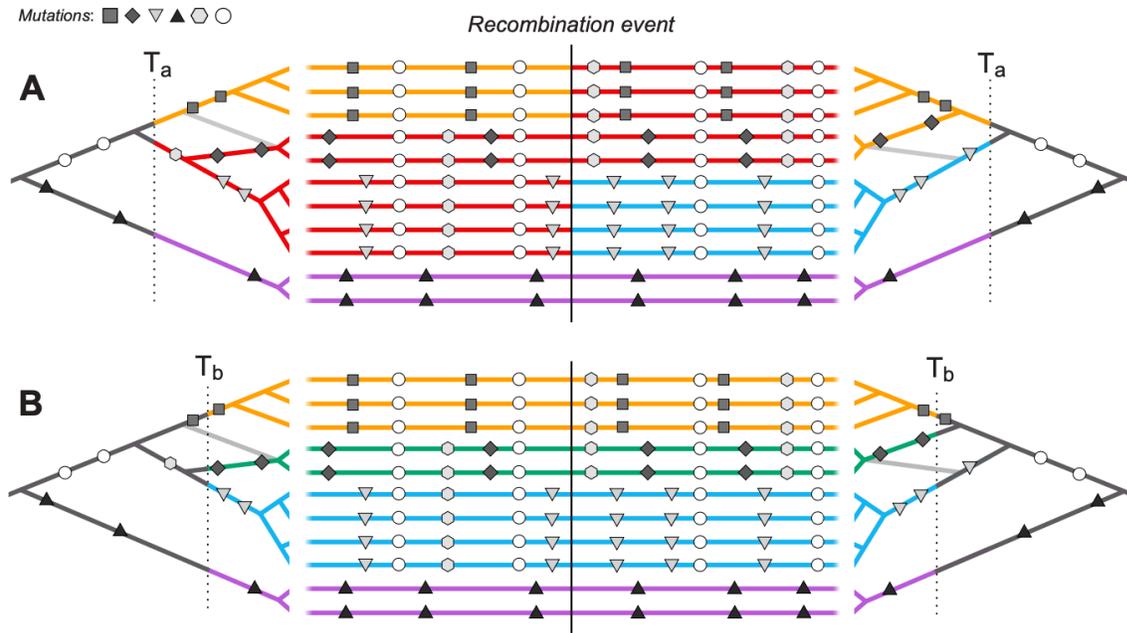


123 **Figure 1. Block-like patterns in empirical data.** Block-like patterns in phased DNA sequences  
 124 from *Mimulus auranticus* within the gene *MaMyb2* (Stankowski & Streisfeld, 2015). Rows show  
 125 24 individual haplotypes. Each column is a site with yellow and blue squares representing ancestral  
 126 and derived sites, respectively. (B) An  $F_{st}$  Scan across *Heliconius* chromosome 2 reveals a large  
 127 plateau of differentiation on chromosome 2 between races of *H. erato* (Meier et al., 2021). This  
 128 large block-like pattern coincides with a chromosomal inversion, the boundaries of which are  
 129 illustrated by the dashed line.

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131 Whilst a blocklike structure may be apparent within empirical genetic data, we argue here  
 132 that there should be a more fundamental definition of haplotype block that is based on the true  
 133 ancestry of the sequences, independent of the mutations that generated observable SNPs. Thus, we  
 134 separate the *definition* of haplotype blocks from the *estimation* of these blocks from actual data.  
 135 Haplotype blocks can be defined in a more concrete way via the classical concept of identity by  
 136 descent (Carmi et al., 2013; Hartl et al., 1997; Thompson, 2013). Imagine an initial population,  
 137 where each founder genome is labelled by a different colour. At some later time, each region of

138 the genome must derive from one or other founder, and so will appear as a mosaic of blocks of  
 139 different colours, each corresponding to their ancestors. This naturally defines blocks that descend  
 140 from a given set of founders (Fig. 2). Fisher (Fisher, 1954) showed that the junctions between IBD  
 141 blocks segregate like Mendelian variants, and used this idea to understand the distribution of runs  
 142 of homozygosity. In artificial populations, we can now sequence the founders, and thus directly  
 143 observe blocks defined in this way (Lundberg et al., 2017; Otte & Schlötterer, 2021; Wallberg et  
 144 al., 2017). Moreover, if we disregard new mutations, the evolutionary processes subsequent to the  
 145 founding of the population are entirely described by the block structure.  
 146



147 **Figure 2. Haplotype blocks defined through identity by descent (IBD).** Panels A and B show the  
 148 same 11 hypothetical DNA sequences depicted as horizontal lines. The trees on the left and right  
 149 sides show the genealogy for the set of sequences on either side of a recombination event (indicated  
 150 by the vertical black line); the light grey branch in both trees shows the effect of recombination in the  
 151 genealogy. Mutations are shown as symbols that correspond to the branches upon which they arose.  
 152 Under the IBD definition, haplotype blocks can be defined based on DNA segments that derive from  
 153 a given set of ancestors, shown here by the coloured sections of branch and DNA sequence. The only  
 154 difference between panels A and B is that these ancestors are defined at two different arbitrary  
 155 time points,  $T_a$  and  $T_b$ , yielding different haplotype structure.  
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157  
 158 Identity-by-descent is defined with respect to a specific ancestral reference population.  
 159 However, when we deal with natural populations, there is no obvious reference population, so the  
 160 block structure will vary depending on our arbitrary choice of founders at an arbitrary time point  
 161 (Figure 2). To eliminate this subjectivity, we will base our definition on the full ancestry of the  
 162 sampled genomes, namely, on the ancestral recombination graph (ARG) (Hudson, 1983). The  
 163 ARG consists of the segments of past genomes that are ancestral to our sample; looking back in  
 164 time, it is generated by a series of coalescence and of recombination events (Box 1). We emphasise  
 165 that these are real events: coalescence occurs when an actual individual leaves two or more  
 166 offspring that are each ancestral to our sample, and recombination occurs between the two haploid

167 parent genomes during meiosis in an ancestral individual. Together, these processes are embedded  
168 in the ARG (Fig. B1).

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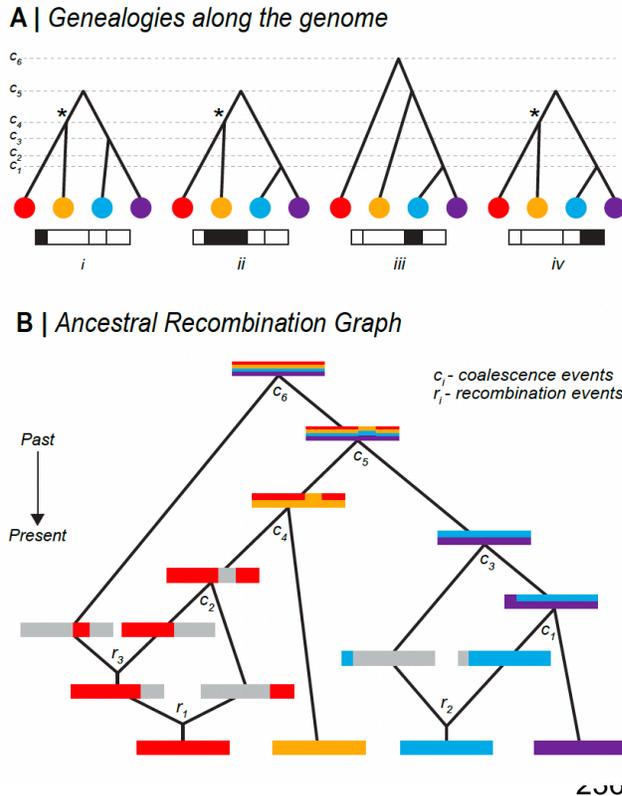
### 172 **Box 1: Ancestral Recombination Graph (ARG)**

173 The ARG describes the complete ancestry of a sample of genomes through a series of real  
174 coalescence and recombination events (Griffiths & Marjoram, 1997; Hudson, 1983). At any given  
175 site on the genome, the relationship can be described through a genealogy (Kingman, 1982); all  
176 contemporary samples coalesce and eventually trace back to one single ancestor. Moving along  
177 the genome, the relationship inevitably changes due to recombination. This leads to a series of  
178 observable genealogies along the genome (Fig B1A), which are embedded in a single structure -  
179 the ARG (Fig B1B).

180 The full ARG (Fig B1B) is a graph structure that depicts individuals (both ancestral and  
181 extant), lineage relationships in time. Each node in the ARG represents a real coalescence or  
182 recombination event, whilst branches represent the ancestry of a particular genomic segment,  
183 along a genetic lineage (depicted by coloured/grey segment for inherited/non-inherited genetic  
184 material in Fig B1B). Altogether, an ARG describes the entire ancestral history - each  
185 recombination and each coalescence event, which imply the genealogy for each non-recombined  
186 genomic block. Crucially, the ARG describes ancestry but not allelic state, so is independent of all  
187 the mutations that lead to the observed polymorphism in the present sample.

188 It is important to note that the full ARG (Fig B1B) contains more information than the  
189 series of tree sequences along the genome (Fig B1A). First, a series of tree sequences lack  
190 information on the timing of recombination events, unless these are separately stored. Second,  
191 while some recombination events lead to observable changes in genealogical trees, others might  
192 not. Figure B1A depicts such cases - some recombination events might not change the tree  
193 topologies at all (trees *ii* and *iv* are exactly the same), whereas others might only lead to temporal  
194 changes in coalescence nodes (tree *i* differs from trees *ii* and *iv* by 1 node position, but all have the  
195 same topology). Therefore, while there are 4 non-recombining genomic regions, there are only 2  
196 unique tree topologies (trees *i*, *ii* and *iv* have the same topology) and 3 distinct trees (trees *ii* and  
197 *iv* are exactly the same). Some coalescence events can also be entirely invisible and not be  
198 represented in any of the individual trees – coalescence at  $t_2$  in Fig B1B is not represented in the  
199 series of trees in Fig B1A. Furthermore, two disjunct blocks of the genome can be inherited from  
200 the same ancestor, so that a unique coalescence event (e.g. marked by \* in Fig B1A) can generate  
201 disjunct blocks of ancestry. It should also be noted that although Fig B1 shows the inevitable  
202 coalescence of the whole genome into a single common ancestor, this typically takes an  
203 astronomically long time: each non-recombining region of the genome coalesces at various time  
204 points, and the single lineages ancestral to each region then take an extremely long time to coalesce  
205 in one common ancestor, in a process which is in principle unobservable.

206 Since the ARG contains full information about the genealogy of the sample, it is in theory  
207 sufficient to infer any evolutionary process: the ARG necessarily gives more information than  
208 commonly used statistics like SFS,  $F_{st}$ , EHH, which are low-dimensional summaries of the ARG  
209 (Ralph et al., 2020). Therefore, the ARG should serve as the foundation for developing new  
210 methodologies. However, we note that whilst the ARG is a sufficient statistic, it remains an open  
211 question how much the extra information it gives can improve inference: the intrinsic variability  
212 of the evolutionary process sets a bound on the accuracy of our inferences.



**Figure B1. Relationship between Genealogies and the ARG.**

(A) Genealogical trees along the genome, corresponding to the ARG - each tree describes the ancestral relationship for each of the 4 non-recombined regions.  $c_1, c_2, \dots, c_6$  denote time points for each coalescence event. Trees can either change, have the same topology, or marginally differ by only temporal positions of coalescence nodes. Asterisk (\*) denotes a unique coalescence event that is ancestral to disjunct genomic regions. (B) Full representation of Ancestral Recombination Graph (ARG) - Tracing back ancestry of four genomes, there is either recombination splitting lineages or coalescence merging lineages. Inherited ancestral genomic regions are coloured corresponding to the contemporary genomes. Recombination is represented by splitting the genome into two; where grey denotes non-ancestral genomic region. Coalescence is represented by two

237 genomes merging, with inherited genomic regions denoted by mixed colours. There are 3  
 238 recombination and 6 coalescence events in the full ancestral history of the four genomes.  $c_1, c_2,$   
 239  $\dots, c_6$  denotes time points for each coalescence event.  $r_1, r_2, r_3$  denotes time points for each  
 240 recombination event.  
 241

242  
 243 In large populations, and over long timescales, the ARG is approximated by the coalescent  
 244 with recombination; in the simplest case, the rate of coalescence is the inverse of the effective  
 245 (haploid) population size, and the rate of recombination is just the rate of crossover (Hudson 1983,  
 246 Griffiths, Marjoram 1997). Importantly, the coalescent does not describe the entire genealogical  
 247 relationship of the whole population. Rather, it summarises how the subset of sampled individuals  
 248 are related to each other. Spatial and genetic structure can also be included: ancestral lineages carry  
 249 a particular set of selected alleles (i.e., a particular genetic background), and are at a particular  
 250 spatial location. Tracing back in time, lineages move between backgrounds by recombination, and  
 251 between locations by migration.

252 Informed by the ARG, we could define a haplotype block as a contiguous region of the  
 253 genome in which all sites share the same genealogy, i.e. a local gene tree. However, adjacent  
 254 genealogies differ by a single recombination event, and so blocks defined in this way will be  
 255 vanishingly small (especially with large samples) and will usually differ trivially (see A in Fig. 3  
 256 and Fig. B1A). Moreover, as samples get larger, blocks defined this way will become so small as  
 257 to be impractical.

258 Instead, we define a haplotype block as the set of genomic regions that descend from a  
 259 particular branch in the ARG; this branch is defined by a unique coalescence event. Crucially, such  
 260 regions should carry a shared set of derived SNP alleles that arise on the focal branch that just

261 precedes the coalescence event. With enough SNPs, the haplotype block is revealed directly by  
262 these shared SNPs.

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### 264 **Implications of the definition**

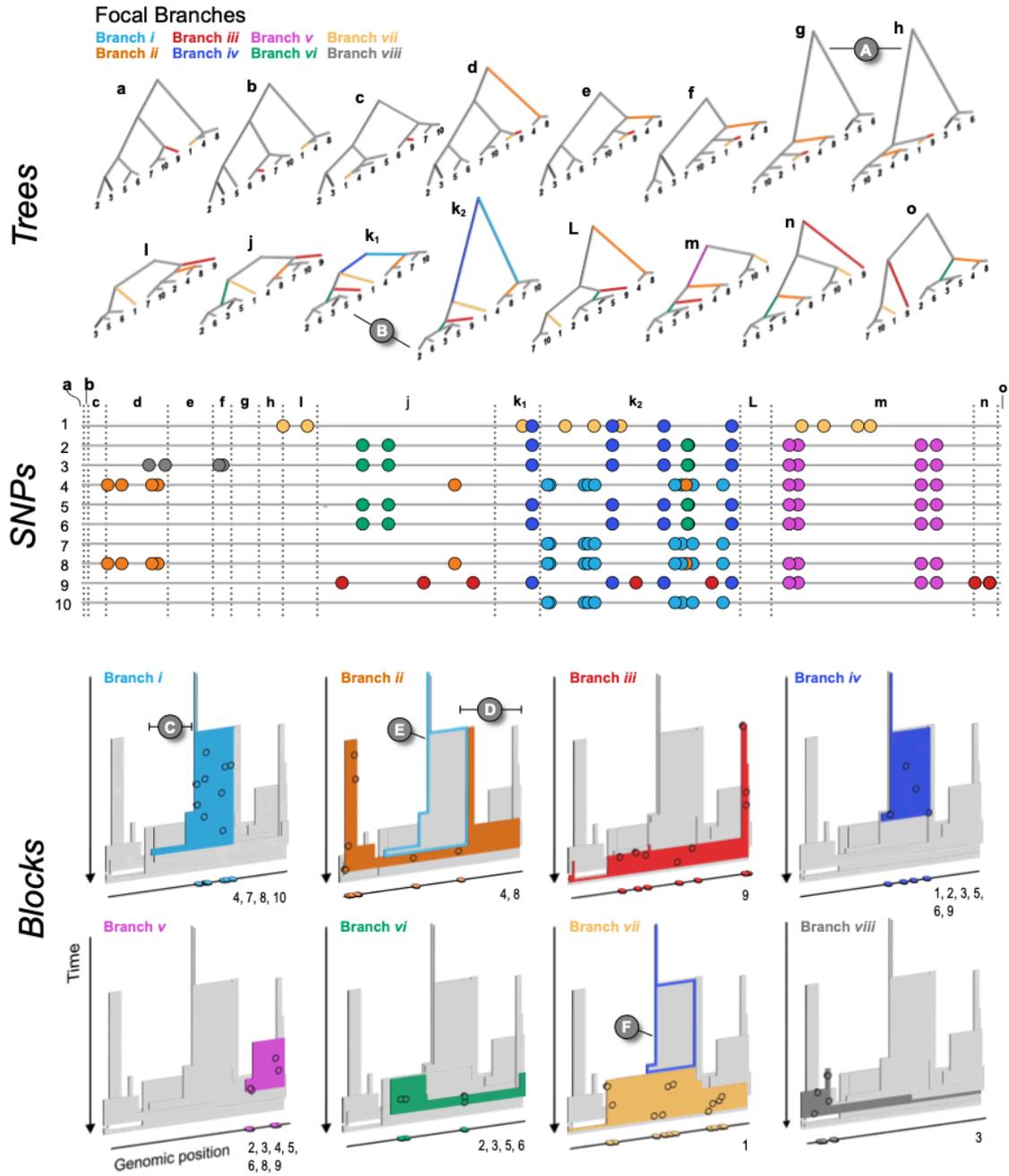
265 We next elaborate on the definition and illustrate the relationships between genealogies,  
266 SNPs and haplotype blocks using example simulations. Figure 3 shows a neutral example  
267 capturing the ancestry of 10 genomes, sampled from a population of 100 haploid individuals,  
268 across 10cM of the genetic map (Supplement 1). SNPs were generated by infinite-sites mutation  
269 with mutation at twice the rate of recombination. This simulation is general, because time and map  
270 distance both scale with population size (Hudson, 1990). Thus, the 268 generations taken for every  
271 part of the simulated genome to coalesce in a single common ancestor scales to  $2.68N$ , and the  
272 simulated map length scales to  $10/N$ . Thus rescaled, this simulation shows a generic pattern,  
273 independent of population size.

274 The central panel of Fig. 3 (middle panel, ‘SNPs’) shows the distribution of SNPs on the  
275 ten sampled genomes, coloured according to the branch on which they arose (we illustrate 8  
276 branches with four or more SNPs each, out of 55 unique branches). The genome is divided into 34  
277 non-recombining intervals, but it contains only 24 different genealogies, because some longer  
278 genealogies were split into multiple intervals by intervening recombination events (Fig. 3; top  
279 panel, ‘Trees’). This illustrates how recombination interacts with the coalescent (also see Fig. B1  
280 for schematic representation of the process). If we disregard branch lengths, the trees can be further  
281 simplified into 15 distinct topologies shown in the top panel Fig. 3 (trees and corresponding  
282 regions on the genome labelled a - o). For illustration, we show one pair of genealogies that have  
283 the same topology, but differ in depth ( $k_1$  and  $k_2$ ), B in Fig. 3).

284 The coloured blocks shown in the lower panel of Fig. 3 (‘Blocks’) illustrate the extent of  
285 each branch along the genome, and through time. The mutations arising on each branch are  
286 projected onto the block at the time and genomic position that they arise. The number of SNPs  
287 arising on each branch is Poisson distributed, with the expected number proportional to the area  
288 of the block; this area is the sum of the genomic lengths that each ancestor carries, and that is  
289 ancestral to the coalescence event that defines the branch. We emphasise that this is a random  
290 process, so some regions may not carry any informative SNPs. For example, though branch  $i$  (light  
291 blue) is relatively well covered by 9 SNPs, none of them fall in the shallow region to the left (C in  
292 Fig. 3). Similarly, branch  $ii$  has only 6 SNPs, none of which happen to fall in the rightmost region  
293 (D). Ultimately, the distribution of SNPs sets a limit on what can be inferred from sequence data;  
294 branches without mutations will be invisible to us, and our ability to infer the length of a block  
295 depends entirely on where mutations happen to fall.

296 Each branch coincides with a specific coalescence event that brings together a specific set  
297 of lineages: in other words, branches are defined by both the coalescence event *and* the set of  
298 lineages. A single coalescence, i.e., a single ancestor, may generate multiple branches: the two  
299 genomes that come together in that event may carry a mosaic of ancestral material, in several  
300 combinations. A single coalescence event may even generate a branch that carries disjunct  
301 segments of the genome, ancestral to the same set of descendants (see the schematic representation  
302 on the Fig. B1). This did not occur for any of the focal branches in the example of Fig. 3, but is  
303 not unlikely, especially in a selective sweep. Conversely, two different coalescence events may  
304 happen to bring together the same sets of lineages; their branches would be hard to distinguish.

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**Figure 3. The relationship between trees (top), SNPs (middle), and haplotype blocks (bottom) in the neutral simulation** (see main text for simulation details). The trees (a - o) show all of the unique topologies that coincide with the genomic spans shown in the central panel (also labelled a - o). The 8 branches that we focus on in this example are coloured and labelled i – vii. (A) Two neighbouring topologies that differ only slightly due to recombination. (B) An example of two trees ( $k_1$  and  $k_2$ ) that have the same topologies but different branch lengths. The central panel shows 10 haploid genomes (labelled 1 – 10, top to bottom, coinciding with the tips of the trees). The SNPs that arose on the 8 focal branches are indicated by the coloured circles. The lower panel (Blocks) shows the haplotype blocks for each focal branch. The coloured block in each panel is the focal branch, with the other 7 blocks shown in grey. The mutations shown in the central panel are projected onto each block (black circles) at the genomic location and time that they arose.

317 They are also plotted onto the genomic position axis to make the connection with the centre panel mode  
318 explicit. Similarly, the numbers at the bottom right corner indicate which DNA sequences the mutations are  
319 associated with. (C & D) Examples of regions of blocks that, by chance, are revealed by mutations arising  
320 on the corresponding branch. (E & F) Examples of nested blocks, where the ancestral block is highlighted  
321 with a coloured outline.

322  
323 Because each branch is generated by a single coalescence, it begins at the same time across  
324 its whole extent (so, branches are bounded by a horizontal line at their base in the lower panel of  
325 Fig. 3). Recombination events split distal segments, thus limiting the span of the block. Tracing  
326 back in time, branches must end in coalescence events that combine them with yet more  
327 descendants. These may occur at different times if there have been recombination events.

328 Haplotype blocks overlap in their genomic extent, since multiple lineages exist at any time  
329 after the MRCA; this is shown by the overlapping 3-D blocks in Fig. 3 ('Blocks'). Haplotype  
330 blocks will also overlap in the genome (but not in time) when branches are nested in the genealogy.  
331 For example, branch *ii* (orange), which is ancestral to genomes 4 and 8 descends in the middle part  
332 of the genome from branch *i* (blue), which is ancestral to genomes 4, 7, 8 and 10. Thus, branch *i*  
333 is nested above branch *ii* in Fig. 3 (see also F for another example of nesting).

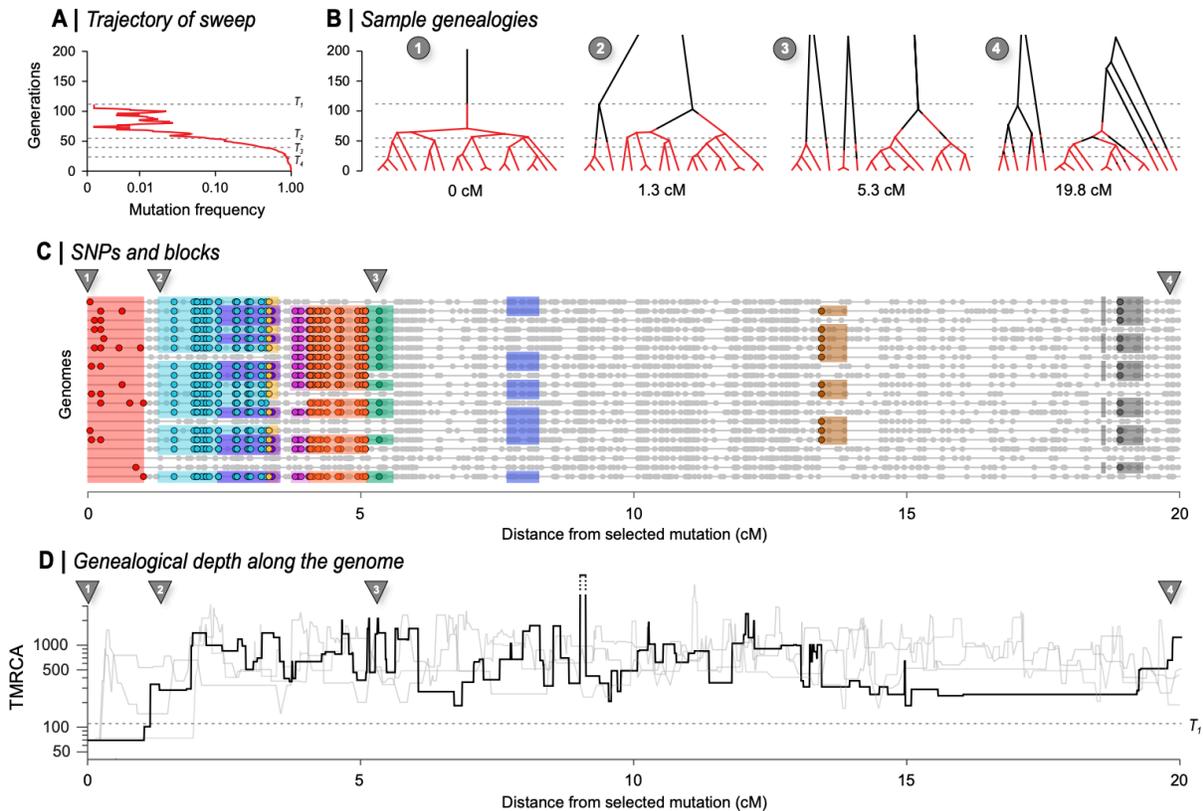
334 If we start at a particular point on the map, and work along the genome, at some point a  
335 branch will be split by a recombination event; the new lineage will trace back and eventually  
336 coalesce, most likely ending the branch. The rate of recombination is proportional to the branch  
337 length, and so we expect that if a branch traces back deep into time, it will span a short region of  
338 the genome. Conversely, shallow branches will extend over a longer genomic span. This pattern  
339 is seen clearly in Fig. 3 (lower panel, 'Blocks'), where branches consist of segments that are either  
340 deep and narrow, or shallow and wide. However, this relationship is not *precisely* inverse; if it  
341 were, blocks would tend to have the same area, whether they were deep or shallow, and hence  
342 would carry similar numbers of SNPs. In simulation, deep branches tend to be wider than expected  
343 from the naive argument given here (Supplement 1), and so most SNPs are on a few deep branches.

344 Note that under the coalescent process, large numbers of sampled lineages rapidly coalesce  
345 down to a few, which are then likely to trace back deep into the genealogy. Thus, in a given region  
346 of the genome a substantial fraction of SNPs will fall on long, deep, branches, whereas the tips of  
347 the genealogy will be hard to resolve. Moreover, in a large sample, it is unlikely that different  
348 coalescence events will bring together exactly the same set of lineages by chance, so that we can  
349 usually identify unique coalescence events as corresponding to unique sets of lineages.

350 Figure 3 illustrates the simplest case of the standard coalescent with recombination. In  
351 reality, population structure and selection complicate genealogies. For example, in the island  
352 model, lineages either coalesce quickly within a deme, or escape to coalesce much further back in  
353 time. This exaggerates the tendency for genealogies to be dominated by a few long branches  
354 (Wakeley, 2009). Selective sweeps have a somewhat similar effect. In the classic case (Maynard  
355 Smith & Haigh, 1974), all lineages at the selected locus coalesce in the individual that carries the  
356 favoured mutation. Moving out from this locus, recombination frees lineages to coalesce much  
357 further back.

358 Figure 4 illustrates such a selective sweep (Supplement 2). The sweep greatly reduces  
359 diversity around the selected locus, because all lineages must trace back to the successful mutation  
360 (Fig. 4B, 1); this region of complete coalescence is shown in red; note that it still contains some  
361 diversity, due to mutation subsequent to the sweep. As we move away from the selected locus,  
362 lineages recombine out onto the ancestral background, and coalesce with the rest of the genealogy  
363 much further back (Fig. 4B). This process can be seen in the time to the MRCA (Fig. 4D), which

364 jumps from a low value at the selected locus, through successive recombination events, back to a  
 365 time that fluctuates around  $4N_e=800$  generations, under the standard coalescent. However, the  
 366 replicates in the lower panel show that there is considerable variation in this process, which sets a  
 367 fundamental limit on our power to detect a sweep and estimate its properties.  
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 371 **Figure 4. The effects of a recent selective sweep on linked genealogies.** (A) A mutation with advantage  
 372 10% arose in a population of 400 haploid individuals, and swept to fixation in 110 generations, at which  
 373 time 20 genomes were sampled; 20cM of the genome is followed back in time, with the selected locus at  
 374 the left.; dashed lines ( $T_1 - T_4$ ) show times when the favoured allele was in 1 copy, at 10%, at 50%, and at  
 375 90% (110, 53, 38, 22 generations back). (B) shows genealogies at positions 0, 1.3cM, 5.3cM, and 20 cM,  
 376 branches are coloured in red when on the fitter background, and black when on the ancestral background.  
 377 Thus, changes in colour show recombination events that change the genomic background. Note that such  
 378 events are unlikely when the allele is near fixation (i.e., at the base of the tree, below the lower dashed  
 379 line), and conversely, become common whilst the allele is rare, simply because it will almost always meet  
 380 with the opposite background. Before the mutation occurs (i.e., above the upper dashed line) lineages must  
 381 either trace back to that mutation (top left) or recombine out into the ancestral background; thus, all lineages  
 382 must appear black above the upper dashed line (110 generations back). Note that the disjunct branches in  
 383 trees 2 - 4 all coalesce further back in time, but only 200 generations are shown for visibility. (C) shows  
 384 SNPs along the 20 sampled genomes. 9 of the most substantial branches are shown. (These have more  
 385 than 8 descendants, formed by coalescence more recently than the sweeping mutation, and have areas  
 386  $>0.5$ ). The red block at the left shows the region linked to the selected locus, which coalesces in a single  
 387 common ancestor 69 generations back, just after the sweeping mutation arose. Grey dots show those SNPs  
 388 that are not on these 9 highlighted branches. (D) shows the time back to the most recent common ancestry  
 389 (TMRCA) along the genome, on a log scale. The bold line shows the example simulated above, whilst the  
 390 three grey lines show replicates, generated conditional on the same sweep; the break in the line shows an  
 391 area where the TMRCA extends further back than the extent of the y-axis. The dashed line across the plot  
 392 corresponds to  $T_1$  in panel A.

393 At the selected locus, all lineages coalesce in the favoured mutation. Successive  
394 recombinations each free one or a few lineages from the new background, so that the exceptionally  
395 large and recent cluster gradually diminishes in size, until the genealogies follow a close to neutral  
396 distribution. Thus, branches with large numbers of descendants are associated with the sweep, and  
397 can be distinguished by the characteristic sets of SNPs that they carry; nine 9 such branches are  
398 illustrated in Fig. 4C. It remains to be seen whether the rich information contained in the structure  
399 of such branches will help us improve our inferences.

400

#### 401 **The definition in practice**

402 Having defined haplotype blocks conceptually, we next consider the problem of inferring  
403 haplotype blocks from empirical datasets. Current sequencing and genotyping technology make it  
404 straight-forward to call SNPs or indel variants, but it remains non-trivial to connect these to the  
405 haplotypes in which they are embedded. For that reason, sophisticated algorithms have been  
406 developed for phasing, genotype imputation and inference of genealogies (Browning & Browning,  
407 2009, 2013; Davies et al., 2016; Howie et al., 2011; Marchini et al., 2007). These tasks all engage  
408 different facets of the same problem, and rely to some extent on haplotype structure. However,  
409 these methods tend to focus on phasing and most stop short of inferring haplotype blocks as we  
410 define them. Given that our definition is rooted in the features of the ARG, we will focus our  
411 discussion around a selection of methods that make active use of the ARG and its approximations.  
412 We will discuss the underlying assumptions of these genealogy-based methods and highlight  
413 where they could be extended in light of our proposed haplotype block definition. Separately, in  
414 Box 2, we also outline classes of simpler methods that use fixed genomic windows or genomic  
415 segments as a proxy of the haplotype block.

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#### 419 **Box 2: Methods for haplotype detection**

420 Many methods for inferring evolutionary processes make use of haplotype structure. These can be  
421 roughly grouped into three types based on their underlying paradigm: window-based methods,  
422 segment-based methods and tree-based methods. These methods vary in complexity from simple  
423 heuristics to full statistical treatments. Here we discuss window-based and segment-based  
424 methods, but we reserve our discussion of tree-based methods to the main text.

425 Of the three classes, window-based methods tend to be the simplest, and primarily operate  
426 *across* sets of individuals. In the simplest form, haplotypes are operationally defined as the set of  
427 alleles observed at the segregating sites within a predefined window of an arbitrary length, say, 50  
428 SNPs or 100 kilobase. Ideally, window sizes should be short enough to minimize spanning  
429 recombination breakpoints. One example is  $H_{12}$ , which detects selective sweeps (Garud et al,  
430 2015). In this test, for any given window, haplotypes are rank-ordered by their frequencies; in the  
431 case of a selective sweep at a given locus, we expect the two most common haplotypes ( $H_1$  and  
432  $H_2$ ) to dominate the population. The  $H_{12}$  test features enhanced power to detect selection, especially  
433 under competing sweeps between recurring mutations. However, the test does not attempt to  
434 capture the real haplotype block length and is rather heuristic. Other fixed window-based  
435 applications include ones exploiting local genomic structures, especially ones showing  
436 geographical structure or associated with local adaptation (data-driven clustering/DDC in (Jones  
437 et al., 2012), see also (H. Li & Ralph, 2019; Todesco et al., 2020). While window-based methods  
438 do not explicitly infer or use information of haplotype block length, they sometimes do take the

439 genealogical structure into account, e.g., *Twisst* (Lohse et al., 2016; Martin & Van Belleghem,  
440 2017). Often, the simplicity of window-based methods is also their main appeal in the era of SNP  
441 genotyping.

442 Segment-based methods are more sophisticated. They operate primarily on individual  
443 sequences, with the aim to represent haplotypes as a mosaic of segments from a haplotype panel,  
444 often under some version of Li and Stephens algorithm (Box 2). These segments offer a more  
445 realistic model of recombination breakpoints and confer superior power to capture signatures due  
446 to linkage. Extended haplotypes homozygosity (EHH) (Sabeti et al., 2002) is an excellent example  
447 of such segment-based statistics for inferring selection. Along with its derivatives, such as  
448 integrated haplotype score (iHS) (Szpiech & Hernandez, 2014; Voight et al., 2006) and cross-  
449 population EHH (XP-EHH) (Sabeti et al., 2007), they have been widely used to detect selection in  
450 many systems (Cao et al., 2011; International HapMap Consortium, 2005). These methods  
451 typically seek to capture the decay of a signal, say, in the extent of haplotype sharing, from an *a*  
452 *priori* defined core SNP. More sophisticated methods based on hidden Markov models to infer the  
453 haplotype structure are especially helpful in uncovering admixture and introgression (e.g.,  
454 fineSTRUCTURE (Lawson et al., 2012). This allows for the visualization of the haplotype-specific  
455 ancestry and improved fine-scale analysis of population structure that is not obvious from unlinked  
456 markers.

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459 The full ARG contains information about branches of the genealogy and, in theory, encodes  
460 all the information needed for applying the haplotype block definition to empirical datasets.  
461 Therefore, a direct (but impractical) way to define and analyse haplotype blocks in a dataset would  
462 be to infer the full ARG from the sample of sequences. Nevertheless, as we will soon see below,  
463 the state space of every possible ancestral history of a sample of genomes is effectively infinite,  
464 so inferring the ARG in its full form is intractable. Instead, most practical methods rely on various  
465 trade-offs to simplify the problem.

466 For direct inference of ARG, ARGweaver (Rasmussen et al., 2014) and its extension  
467 ARGweaver-D (Hubisz et al., 2020) are among the most powerful, and widely used. ARGweaver  
468 solves the infinite state space issue by discretizing time, effectively making the ARG space finite  
469 by limiting recombination and coalescence events within discrete time points. Further,  
470 ARGweaver uses a coalescent-with-recombination model (Sequentially Markov Coalescent, or  
471 SMC; McVean & Cardin 2005; extended by Marjoram and Wall 2006 and McVean & Cardin,  
472 2005) to sample from an ARG distribution. While making inference more tractable, SMC  
473 precludes the inference of disjunct blocks, because only one immediately prior state is considered  
474 as one moves along the genome. Besides these limitations, inference of the “full” ARG is still  
475 computationally expensive. As such, ARGweaver is most suitable for mid-sized datasets on the  
476 order of fifty sequences.

477 Two recent methods, *tsinfer* and *Relate* (Kelleher et al., 2019; Speidel et al., 2019), have  
478 attempted to approximate the ARG in much larger populations with thousands of samples by  
479 focusing on topology (or ‘succinct tree sequences’), rather than a full inference of the ARG. They  
480 do so by representing genomes as a series of tree topologies: *Relate* as distinct trees; *tsinfer* as ‘tree  
481 sequences’ connected via ancestral haplotypes. Both achieve this remarkable speed-up by relying  
482 on the Li and Stephens’ hidden Markov model (Li & Stephens, 2003) hidden Markov model (see  
483 Box 2 for further details) to infer local pairwise distances (*Relate*) or ancestral haplotypes (*tsinfer*).  
484 As an added advantage, which doubles as an efficient, lossless compression algorithm by indexing

485 population genomic variation as SNPs-on-trees as opposed to the traditional (and highly  
486 redundant) SNP-by-individual matrix (implemented as a tskit library (Kelleher et al., 2019). Put  
487 in another way, the tree sequence encoding can fully capture the variation data in entire  
488 populations, for a fraction of the storage space. Such a representation also effectively encapsulates  
489 a number of population genetics summary statistics (Kelleher et al., 2019; Ralph et al., 2020).  
490 These developments may prove essential, as sequencing of entire national populations increasingly  
491 becomes routine.

492 Among practical methods, tsinfer and Relate represent the state-of-the-art in representing  
493 large populations. All three approaches, including ARGweaver, approximate some aspects of the  
494 ARG well, and give accurate coalescence time estimates under simulation of the standard  
495 coalescent (Brandt et al., 2021). For our purposes, they are also useful approximations of ARG  
496 that highlight some of the key advantages we wish to emphasise in our haplotype block definition.  
497 For example, Relate presents a selection statistics suite that goes beyond SNP information. One  
498 advantage of Relate is that branches are dated, as opposed to a strict encoding of topology alone  
499 in tsinfer. Having dated branches allows, among other things, the possibility of estimating temporal  
500 changes in mutation rates. Another useful feature, in our view, is tsinfer’s placement of SNPs onto  
501 branches, which is the key feature that distinguishes haplotype blocks from each other under our  
502 definition.

503 We note that efforts are already underway to bridge across methods and address limitations.  
504 For instance, tsdate now adds coalescence times estimates and branch lengths from tsinfer’s output  
505 (Wohns et al., 2021). In the context of our exploration of haplotype blocks and their overlapping  
506 structure (Fig. 3C, D), we note that they can be captured rather poorly under the Li–Stephens  
507 models in tsinfer and Relate, in a way that may bias the inferred ARG.

508 Taken together, there has been a recent spurt in innovation in genealogy/ARG-based  
509 methods. Among these, ARGweaver arguably comes closest to inferring the full ARG, but at  
510 considerable computational cost. Both tsinfer and Relate are robust and scalable to thousands of  
511 samples with minimal, reasonable tradeoffs, but infer haplotype blocks only as an incidental  
512 output. Ultimately, we hope our discussion here will encourage development of new methods to  
513 infer haplotype blocks as we define them.

514 Assuming that a method becomes available for inferring blocks as we have defined them,  
515 there are still practical considerations that we need to face. For example, we see from Fig. 3 that  
516 haplotype blocks, defined via branches in the genealogy, have a complex structure, tracing back  
517 in time for a number of generations that varies along their span (e.g., blocks ii and iii). This makes  
518 it (for example) hard to define the extent of haplotype blocks in any simple way, especially since  
519 they may be disjunct. Should this be their maximum length, or should it rather be weighted by the  
520 depth? It is not clear which description would be better for inference and this may even depend  
521 upon the specific process that we wish to infer. These kinds of issues could be investigated by  
522 estimating parameters under a variety of specific models in which case we can evaluate the strength  
523 and weaknesses of different descriptions of haplotype structure in characterizing different  
524 processes.

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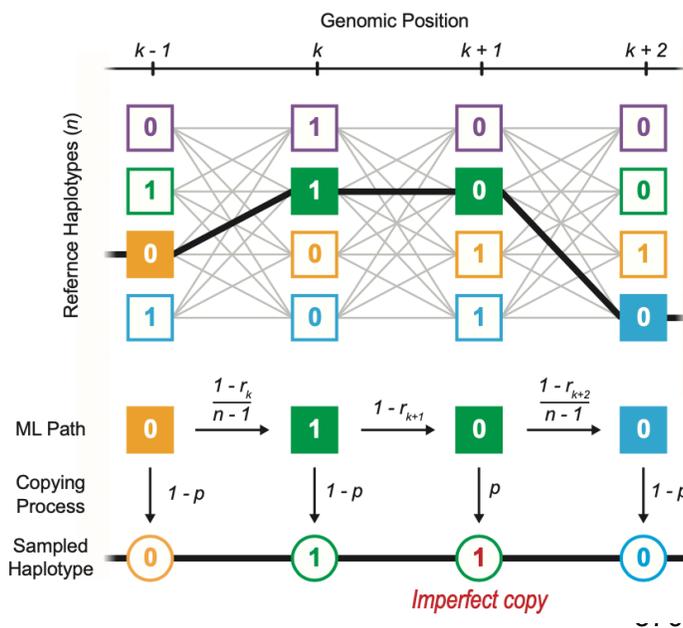
### 528 **Box 3: Application and limits of Li and Stephens Model**

529 Li and Stephens (2003) (LS) proposed a hidden Markov model (HMM) framework that underpins  
530 a large number of existing inference methods. Originally developed to model patterns of linkage

531 disequilibrium, it has since been widely applied to develop analytical tools and address empirical  
 532 problems, such as, phasing and imputation of genomic data (Browning & Browning, 2007; Howie  
 533 et al., 2009; Y. Li et al., 2010; Marchini et al., 2007; Stephens & Scheet, 2005), inference of  
 534 population structure and demographic history (Hellenthal et al., 2014; Lawson et al., 2012;  
 535 Steinrücken et al., 2019, 2018), characterisation of local admixture (Price et al., 2009; Sundquist  
 536 et al., 2008), inference of local genealogies (Kelleher et al., 2019; Rasmussen et al., 2014; Speidel  
 537 et al., 2019), and many more. The LS HMM framework is highly tractable and efficient. However,  
 538 underlying assumptions make it incompatible with the haplotype definition we propose.

539 The LS algorithm requires a reference sample of haplotypes, or if presented in a sequence,  
 540 previously observed haplotypes. It gives a framework to decide whether some focal haplotype  
 541 represents a) an entirely new haplotype or b) a mosaic of previously encountered haplotypes, and  
 542 determines the breakpoints and transitions in this mosaic. Whilst the LS model captures genetic  
 543 relatedness among chromosomes through recombination, it assumes that the reference haplotypes  
 544 are known. This would be valid in a selection experiment, if we know the founder genomes; in this  
 545 case, blocks are defined by IBD to this reference population. However, if we only have  
 546 contemporary genomes, the reference panel is an approximation. Secondly, the model assumes  
 547 that genomic states depend solely on the immediately preceding site. This is also an approximation,  
 548 since in the true ARG, recombinant lineages can coalesce back to any lineage that existed in the  
 549 preceding genome, which yields disjunct haplotype blocks.

550



**Figure B2. Schematic representation of Li and Stephens hidden Markov model.** A new haplotype can be sampled as an imperfect copy of  $n$  reference haplotypes (hidden states). To find the most likely path taken through the hidden states, the LS model works along the genome ( $k-1, k, k+1, \dots$ ), calculating the probabilities of changes in the attributed haplotype. The transition probability to continue or switch the attributed haplotype is a function of the recombination rate ( $r$ ) between adjacent sites, whilst the emission probability to copy the attributed allele with or without error is a function of the mutation rate ( $p$ ). Moving along the genome, the LS model compares the probability of every possible copying path and infers the most likely one.

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574 **Conclusions and outstanding questions**

575 In this article, we have outlined a definition of the haplotype block, explored the  
 576 implications of the definition with simple simulations, and considered how current methods can  
 577 infer such blocks from empirical data. In our view, haplotypes and haplotype blocks should be the  
 578 core concepts through which we understand population genetic processes. Under this view, it  
 579 follows that ideally, genomic datasets should come directly as resolved haplotypes, rather than

580 diploid genotypes that require phasing and further processing. We therefore welcome new  
581 developments in linked- and long-read sequencing techniques and software that are designed with  
582 sequencing and population datasets in mind (Davies et al., 2021; Meier et al., 2021).

583 Our simulations show that haplotype blocks contain rich information about the  
584 demographic and selective history of the locus. Making the most of this information will require a  
585 fundamental rethink of our linear, reference-based genome assemblies, and a move towards a  
586 graph-based assembly standard (Eggertsson et al., 2017; Hickey et al., 2020). We will also need  
587 new concepts and vocabulary to describe features in these graphs (e.g., super-graphs and  
588 “bubbles”; Cheng et al., 2021; Turner et al., 2018; Weisenfeld et al., 2017) informed by a robust  
589 understanding of the generative process discussed above, and we need to align our mental models  
590 with inference schemes and their encoding (as in, e.g., tsinfer). For that reason, we hope our  
591 discussion here can focus our effort towards this new standard, as haplotype-resolved sequencing  
592 becomes routine.

593

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### 831 **Data Accessibility Statement**

832 The Mathematica code used to generate the simulations presented in the paper are provided in  
833 the supplementary materials. The simulated data are available on Dryad under accession number  
834 xxxxxx.

835

### 836 **Benefit-Sharing Statement**

837 Benefits Generated: Benefits from this research accrue from the sharing of our simulation code  
838 as described above.

839

### 840 **Author Contributions**

841 All authors conceived the ideas and contributed to the writing of the manuscript. NHB conducted  
842 the simulations.

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